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# TIDAL PARAMETERS DERIVED FROM THE PERTURBATIONS IN THE ORBITAL INCLINATIONS OF THE BE-C, GEOS-I, AND GEOS-II SATELLITES

**DAVID PARRY RUBINCAM**

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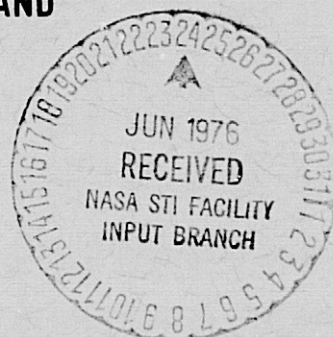
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**GODDARD SPACE FLIGHT CENTER**  
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THE ORBITAL INCLINATIONS OF THE BE-C, GEOS-I,  
AND GEOS-II SATELLITES

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April 1976

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## ABSTRACT

The tidal perturbations in the orbital inclinations of the BE-C, GEOS-I, and GEOS-II satellites are analyzed. Effective tidal Love numbers and phase angles for the  $O_1$ ,  $K_1$ ,  $M_2$ ,  $K_2$ ,  $P_1$ , and  $S_2$  tides are recovered. The effective tidal phase angles tend to be on the order of a few degrees. The effective tidal Love numbers are generally less than the solid earth Love number  $k_2$  of about 0.30. This supports the contention of Lambeck, et al. (1974) that the ocean tides give an apparent depression of the solid earth Love number. Ocean tide amplitudes and phases are calculated for the above tides assuming  $k_2 = 0.30$  and the solid earth lag angle  $\phi_2 = 0$ . The results show good agreement with Felsentreger, et al. (1976) on GEOS-I but not on GEOS-II. The  $M_2$  effective Love number and phase angle are poorly determined, but give a lunar acceleration of  $-29 \pm 15$  arc sec/(100 yr)<sup>2</sup>, an energy dissipation of  $-3.6 \pm 1.8 \times 10^{19}$  erg/sec, and a tidal function time scale of  $1.4 \times 10^9$  yr when averaged over all three satellites. This is in fair agreement with current estimates.

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TIDAL PARAMETERS DERIVED FROM THE PERTURBATIONS IN  
THE ORBITAL INCLINATIONS OF THE BE-C, GEOS-I,  
AND GEOS-II SATELLITES

INTRODUCTION

The sun and moon raise tides on the earth; the displaced mass perturbs the orbits of earth satellites. These perturbations may be analyzed in order to learn about the earth's tides.

Early analyses of the tidal perturbations performed by Kozai (1965, 1968), Newton (1965, 1968), Anderle (1971), Smith, et al. (1973), and Douglas, et al. (1974) were aimed at recovering the Love number  $k_2$  and lag angle  $\phi_2$  of the solid earth tide. The resulting Love numbers were found to be generally smaller than the well-known value for  $k_2$  of about 0.29 to 0.31 obtained from seismic studies (e.g., Longman, 1966). The discrepancy has been ascribed by Lambeck (1974) and Lambeck et al. (1974) to the corruption of the solid earth tidal signal by the ocean tides (and to a lesser extent the atmospheric tides), which Kaula (1962) showed might be significant. The ocean tides give the appearance of Love numbers and lag angles which vary from constituent to constituent. Accordingly, some satellite data have been re-analyzed (Lambeck, et al. 1974; Felsentreger, et al. 1976) in an effort to learn about the solid earth, ocean, and atmospheric tides.

We continue with such a re-analysis here by examining the tidal perturbations in the orbital inclination of three different earth satellites: BE-C (Beacon Explorer C), GEOS-I, and GEOS-II. Table 1 gives pertinent information about the satellites. Inclination perturbations are analyzed because they give a relatively clean separation of tidal effects from other disturbing forces.

#### THE DATA

The BE-C data consists of 36 laser observations, spanning a 501 day period beginning in July 1970. The amplitude of the variation in inclination is about 1.0 arc seconds (40 meters). For further details, see Smith, et al. (1973). The GEOS-I consists of 142 TRANET Doppler observations spaced over 626 days, beginning in February 1966. The amplitude of the tidal signal is about 1.2 arc second (36 meters). The GEOS-II data is composed of 113 precision reduced camera and TRANET Doppler observations taken over a 651 day period beginning in March 1968. For further details, see Felsentreger, et al. (1976).

In each case the well-known disturbing forces were modelled and removed, so that the remaining perturbations are presumably due almost entirely to the tides.

#### ANALYTICAL EXPRESSION FOR THE INCLINATION VARIATION

We now derive an analytical expression for the total tidal perturbation in the inclination of the orbit of an earth satellite by modifying the equation for the solid earth tidal potential.

The solid earth tidal potential expressed in orbital elements is given by  
(Kaula, 1964)

$$U_{\ell mpq} = k_{\ell} R_E^{2\ell+1} B_{\ell m}^* C_{\ell mpq} \sum_{h,j} C_{\ell mhj} \cdot \cos \left[ v_{\ell mpq}^* - v_{\ell mhj} - m\theta^* + m\theta + \epsilon_{\ell mpq} \right] \quad (1)$$

where

$$B_{\ell m}^* = Gm^* \frac{(\ell - m)!}{(\ell + m)!}, \quad C_{\ell mpq}^* = \frac{F_{\ell mp}(I^*) G_{\ell pq}(e^*)}{a^{*\ell+1}}$$

and

$$v_{\ell mpq}^* = (\ell - 2p)\omega^* + (\ell - 2p + q)M^* + m\Omega^*$$

The starred (\*) quantities refer to the disturbing body (sun or moon) and the unstarred refer to the satellite. The sign in front of the tidal phase angle  $\epsilon_{\ell mpq}$  had been minus in Kaula's original formulation; Lambeck, et al. (1974) changed the sign to plus, which makes the important phase angles positive quantities in the case of a frictionally-delayed solid earth tidal bulge. We follow the convention of Lambeck, et al. here.

We wish to find the total tidal potential  $T_{\ell mpq}$  caused by the solid earth, oceans, and atmosphere, since this is the potential felt by a satellite. We limit the discussion to  $\ell = 2$ , since the second degree terms dominate the motion of

the satellite and the evolution of the earth-moon system. (For a discussion of fourth degree terms, see below and Appendix 2.)

In finding the total tidal potential of degree 2 we make the following assumption: the amplitude of the potential and the phase angle become frequency-dependent. This means that the solid earth Love number  $k_2$  in eq. (1) is replaced by the effective Love number  $d_{2mpq}$  and the solid earth phase angle  $\epsilon_{2mpq}$  is replaced by the effective phase angle  $\delta_{2mpq}$ . The adjective "effective" is necessary since we now refer to the tidal response of the entire earth, and not just the solid earth. This procedure takes care of any possible frequency dependence of the solid earth Love number, the response of the oceans, and the atmosphere tides. The letters "d" and " $\delta$ " are chosen to avoid possible confusion with the solid earth tides.

The total tidal potential is now to be substituted in Lagrange's planetary equations to find the perturbation in the inclination of the orbit of an earth satellite. Before doing this, however, let us make several simplifications: (a) omit the zero sum  $-m\theta^* + m\theta$ , (b) consider only terms for which  $j = 0$  and  $\ell = 2h$ , to be rid of dependence on the satellite eccentricity and mean anomaly, and (c) consider only terms for which  $q = 0$  to be rid of small terms which depend on the eccentricity of the disturbing body. The total tidal potential now becomes

$$T_{2mp0} = d_{2mp0} \frac{Gm^*}{R_E} \frac{(2-m)!}{(2+m)!} (2 - \delta_{0m}) \left( \frac{R_E}{a^*} \right)^3 \left( \frac{R_E}{a} \right)^3$$

$$\cdot F_{2mp}(I^*) F_{2ml}(I) \cos \left\{ (2-2p)(M^* + \omega^*) + m\Omega^* - m\Omega + \delta_{2mp0} \right\}.$$



Substitution of this potential into the Lagrange equation

$$[\dot{I}]_{\ell_{mpq}} = - \frac{1}{\sqrt{GM_E a} (1 - e^2)^{1/2} \sin I} \frac{\partial T_{\ell_{mpq}}}{\partial \Omega}$$

and integration with respect to time yields

$$\begin{aligned} \Delta I_{2mp0} = & \frac{d_{2mp0}}{\sqrt{GM_E a} (1 - e^2)^{1/2} \sin I} \left[ (2 - \delta_{0m}) \frac{(2 - m)!}{(2 + m)!} m \right] \left( \frac{R_E}{a^*} \right)^3 \left( \frac{R_E}{a} \right)^3 \\ & \cdot F_{2mp}(I^*) F_{2m1}(I) \frac{\cos \left\{ (2 - 2p)(\omega^* + M^*) + m\Omega^* - m\Omega + \delta_{2mp0} \right\}}{[(2 - 2p)(\dot{\omega}^* + \dot{M}^*) + m\dot{\Omega}^* - m\dot{\Omega}]} \end{aligned} \quad (2)$$

We have assumed in the integration that the satellite elements,  $a$ ,  $e$ , and  $I$ , as well as the nodal rate  $\dot{\Omega}$  are constants. We have also assumed that  $\dot{\omega}^* + \dot{M}^*$ ,  $\dot{\Omega}^*$ , and  $I^*$  remain constant. This last set of assumptions must be removed in the case of the moon when considering periods of time longer than a few years, due principally to the motion of the lunar node on the ecliptic.

The tidal inclination perturbation is thus given by

$$\Delta I = \sum_{\substack{m,p \\ \text{Moon}}} \Delta I_{2mp0} + \sum_{\substack{m,p \\ \text{Sun}}} \Delta I_{2mp0} + \Delta I_0$$

where  $\Delta I_0$  is a constant of integration.

We note in passing several features of eq. (1). First, tides for which  $m = 0$  do not perturb the orbital inclination; thus we obtain no information on these tides. Second, the periods of the tides felt by the satellite are greatly lengthened

over their periods on the earth's surface, due to the replacement of  $\dot{\theta}$  in the frequency by  $\dot{\Omega}$ . Third, there is no way to separate the  $K_1^M$  tide from the  $K_1^S$  tide ( $\ell_{mpq} = 2110$ ), or the  $K^M$  tide from the  $K_2^S$  tide ( $\ell_{mpq} = 2210$ ), since in either case the periods are the same. A hypothesis is needed to do this.

#### ANALYSIS OF THE DATA

Eq. (2) may be conveniently written

$$\Delta I_{2mp0} = c_{2mp0} [ \quad ] \cos \left\{ (2-2p)(\omega^* + M^*) + m\Omega^* - m\Omega \right\} \\ - s_{2mp0} [ \quad ] \sin \left\{ (2-2p)(\omega^* + M^*) + m\Omega^* - m\Omega \right\}$$

for the analysis of the data. Here  $c_{2mp0} = d_{2mp0} \cos \delta_{2mp0}$ ,  $s_{2mp0} = d_{2mp0} \sin \delta_{2mp0}$ , and the empty brackets denote a factor common to both terms. The coefficients  $c_{2mp0}$  and  $s_{2mp0}$  are found from multiple linear regression, from which the effective Love numbers and phase angles may be easily computed.

The regression analyses for the three satellites were carried out with the computer program described in Appendix 3. In each case the tides with the largest expected amplitudes in eq. (2) were retained in the analysis and the smaller ones ignored. The theoretical amplitudes in the solid earth signal were conveniently used to pick out the major contributors.

Table 2 gives the regression solutions. The effective Love numbers and phase angles for the  $K_1^M$ , and  $K_1^S$  tides are assumed to be the same; likewise for the  $K_2^M$  and  $K_2^S$  tides. The resulting inclination curves and residuals are shown in Figures 1 - 6.

Another computer run was made in which the effective phase angles of all but the  $K_1$  tide in the BE-C data and the  $K_1$  and  $S_2$  tides in the GEOS-I and GEOS-II data (the major contributors in each signal) were set to zero. No major changes in the effective Love numbers (or in those effective phase angles solved for) took place. A similar computer run was made with only the first 28 points in the BE-C data and the first 72 points of the GEOS-I data retained. Also, 20 neighboring points in the GEOS-II data taken from the middle of July to the end of September in 1968 were removed and a run made. Again no major changes in the effective Love numbers and phase angles took place, indicating the stability of the solutions. However, the deleted points in the GEOS-II data were chosen not to disturb the basic signal, due to the spacing of the data.

Examination of Table 2 reveals good agreement between the BE-C and GEOS-I results, but poor agreement between GEOS-II and the other two satellites. Also, there is good agreement between our determination of ocean tide parameters and that of Felsentreger, et al. (1976) for GEOS-I, but no agreement on the ocean tide parameters for GEOS-II (see below). The cause of this discrepancy is unknown; hence the GEOS-II results must be treated with caution.

Most of the effective Love numbers given in Table 2 are smaller than the solid earth Love number  $k_2$  of 0.29 to 0.31. This is in general accord with the ocean tide models and charts given in Table 2 of Lambeck, et al. (1974). The only entry in that table which predicts an effective Love number greater than  $k_2$  is the  $O_1$  tide chart of Dietrich. (The  $S_2$  tide model of Bogdanov and Magarik

predicts an apparent increase in the effective Love number for GEOS-II due to a fourth degree term.) The phase angles are on the order of a few degrees, as expected, although some are negative and the BE-C  $K_2$  and the GEOS-II  $P_1$  effective phase angles are embarrassingly large. Also, the BE-C  $K_2$  and GEOS-II  $S_2$  effective Love numbers are rather large and the GEOS-II  $P_1$  effective Love number is rather small. These presumably reflect the inadequacies of the data. However, it will be noted that all three satellites indicate a remarkably small effective Love number for the  $P_1$  tide, apparently indicating a large ocean tide effect. If this effect is real it is highly interesting, since the  $O_1$  tide (the lunar counterpart of the  $P_1$  tide) shows no similar behavior. In fact, the  $O_1$  effective Love number should be larger than  $k_2$  according to Dietrich's chart, as mentioned above. Unfortunately, we have only one poorly determined effective Love number for the  $O_1$  tide, and no mathematical models for either the  $O_1$  or  $P_1$  tide appear to exist.

## SEPARATION OF OCEAN AND EARTH TIDES

We now solve for the ocean tide parameters from the satellite data in the manner of Felsentreger, et al. (1976). To do so, we assume that the tidal signal consists solely of the solid earth and ocean tides; this lumps the small atmospheric tides (principally an  $S_2$  tide) with the ocean tides.

Separation of the ocean from the solid earth tides requires knowledge of the solid earth tidal response. If we assume the solid earth Love number to be

frequency-independent, then from Appendix 2 we have

$$c_{2mp0} = d_{2mp0} \cos \delta_{2mp0} = k_2 \cos \epsilon_{2mp0} + Z_{mp} (1 + k'_2) \begin{bmatrix} C_{(2mp0)2m}^+ \sin \epsilon_{2m}^+ \\ C_{(2mp0)2m}^+ \cos \epsilon_{2m}^+ \end{bmatrix} \begin{matrix} m \text{ even} \\ m \text{ odd} \end{matrix} \quad (3)$$

$$s_{2mp0} = d_{2mp0} \sin \delta_{2mp0} = k_2 \sin \epsilon_{2mp0} + Z_{mp} (1 + k'_2) \begin{bmatrix} C_{(2mp0)2m}^+ \cos \epsilon_{2m}^+ \\ -C_{(2mp0)2m}^+ \sin \epsilon_{2m}^+ \end{bmatrix} \begin{matrix} m \text{ even} \\ m \text{ odd} \end{matrix} \quad (4)$$

where  $\epsilon_{2mp0} \approx m\phi_2$  (Lambeck, et al. 1974),  $\phi_2$  being the solid earth lag angle and  $k'_2$  the second degree load deformation coefficient.

The question arises as to what values to choose for  $k_2$ ,  $k'_2$ , and  $\phi_2$ . Let us pick  $k_2 = 0.30$  and  $K'_2 = -0.30$ , in accord with Longman (1966), and  $\phi_2 = 0$ , in accord with a high  $Q$  ( $\sim 230$ ) for the earth's mantle (see, e.g. Stacey, 1969).

The two rightmost columns of Table 2 give the resulting ocean tide amplitudes and phases. These are to be compared with Table 2 of Lambeck, et al. (1974) and Table 1 of Felsentreger, et al. (1976).

The ocean tide amplitudes in our Table 2 have absorbed the fourth (and higher) degree terms in the ocean tidal potential, which Lambeck, et al. (1974) showed



to be important for some tides. The fourth degree terms could be solved for from observations of two or more satellites, since these terms cause an apparent variation in the second degree effective Love number from satellite to satellite (see Appendix 2). We have chosen not to solve for them here, since the differences between the effective Love numbers tend to be several times larger than those predicted by the ocean tide models and charts; and there are no clear trends.

We may also make a rough estimate of  $k_2$  from the ocean tides charts and models, in the manner of Lambeck, et al. (1974). For this we set

$$d_2 \approx k_2 + Z_{mp} (1 + k'_2) \begin{bmatrix} C_{(2mp0)2m}^+ \sin \epsilon_{2m}^+ \\ C_{(2mp0)2m}^+ \cos \epsilon_{2m}^+ \end{bmatrix} \begin{matrix} m \text{ even} \\ m \text{ odd} \end{matrix}$$

and substitute the ocean tide amplitudes and phases in Table 2 of Lambeck, et al. (1974) into the right side of this equation and our values into the left. A simple average of all charts, models and satellites yields  $k_2 \approx 0.27$ . Performing the same calculation without the GEOS-II results gives  $k_2 \approx 0.26$ .

The effective Love numbers and phase angles of the well-determined tides permit an estimate of  $\phi_2$  as well as  $k_2$ . Using the  $K_1$  tide from BE-C and the  $K_1$  and  $S_2$  tides from GEOS-I and GEOS-II, in connection with the  $K_1$  and  $S_2$

tides from Table 2 of Lambeck, et al. (1974), we find from eqs. (3) and (4) that  $K_2 \approx 0.29$  and  $\phi_2 \approx 1.5^\circ$ . Once again an arithmetic average has been taken.

From  $\phi_2$  we determine a rough estimate of  $Q$  for the mantle, since (see, e.g., Stacey, 1969)

$$Q \approx \frac{1}{\tan \epsilon_{2200}} \approx \frac{1}{\tan 2\phi_2}$$

yielding a value of 19. Omitting the GEOS-II results yields  $k_2 \approx 0.28$ ,  $\phi_2 \approx 4.2^\circ$ , and  $Q \approx 7$ .

Only a simple arithmetic average is taken in the computations above because we have treated the ocean tide models and charts as "observations" without knowing how to weight them. Further, the quality of the satellite data prevents us from reading too much significance into the numbers (such as the extremely low  $Q$  values). Hence the values computed above indicate only the plausibility of the hypothesis that the ocean tides are responsible for the variations in the effective Love numbers and phase angles.

#### TIDAL FRICTION

The evolution of the earth-moon system is dominated by the second degree terms in the total tidal potential. In fact the secular rates of change of  $n_M$ ,  $a_M$ ,  $e_M$ ,  $J$ ,  $I_s$ ,  $\dot{\theta}$ , and  $E$  may all be written

$$\dot{X} \approx \sum_{mpq} [\dot{X}]_{2mpq}$$

where  $X$  is one of the above-mentioned quantities and the right side of the equation has the form (Appendix 1)

$$[\dot{X}]_{2mpq} = P_{2mpq} s_{2mpq}$$

The values of  $P_{2mp0}$  are given in Table 5. Note that the  $s_{2mpq}$  are determined directly from the data by the regression analysis, apart from possible corruption by the fourth degree ocean tide terms.

The  $[\dot{X}]_{2mpq}$  may be conveniently arranged in a table, with the entries to be filled in as reliable data become available. Our own tentative values are found in Table 3. These were computed from the weighted average over all three satellites of each  $s_{2mp0}$ . Table 4 is similar to Table 3, except that the GEOS-II data have been omitted.

Our value of  $\dot{n}_M \approx -29 \pm 15$  arc sec/(100 yr)<sup>2</sup>, taken from Table 3, compares favorably with Lambeck's (1975)  $-34 \pm 5$  arc sec/(100 yr)<sup>2</sup>, computed from ocean tide models and charts. It also agrees well with the astronomically determined values, which range from  $-37.5 \pm 5$  to  $-52 \pm 4$  arc sec/(100 yr)<sup>2</sup> (Lambeck, 1975). The value of  $\dot{n}_M \approx -17 \pm 20$  arc sec/(100 yr)<sup>2</sup> from Table 4 is barely half the current estimates.

Our value of  $\dot{E} \approx -3.6 \pm 1.8 \times 10^{19}$  erg/sec from Table 3 is also in good agreement with current estimates. It is bracketed by Miller's (1966) value of  $-1.7 \times 10^{19}$  ergs/sec, determined from energy dissipation in shallow seas, and Lambeck's

(1975) value of  $-5.7 \times 10^{19}$  ergs/sec, determined from ocean tide charts and models. The number quoted in Table 4 is close to Miller's value, which probably represents a lower limit on the energy dissipation.

On the whole, it would appear that Table 3 agrees better with modern estimates than Table 4. However, Table 3 indicates that the effective phase angle of the  $S_2$  tide is negative, which would speed up the earth's rotation. This is reminiscent of Holmberg's (1952) hypothesis that the atmospheric tidal torque, which tends to speed up the earth, balances the frictional torque, which tends to slow the earth down, thus keeping the earth at a steady rotation rate. The data given in Table 3 of Lambeck (1975) does not indicate a negative effective phase angle for the  $S_2$  tide, however.

Our data on the  $M_2$  tide may be used to estimate the time scale of the tidal evolution of the earth-moon system. Taking (see Appendix 1)

$$\dot{a}_M \approx \dot{a}_{2200} \cong \frac{\sqrt{G(M_E + m_M)}}{3M_E a_M^{11/2}} m_M R_E^5 [F_{220}(I_M)]^2 d_{2200} \sin \delta_{2200},$$

multiplying each side by  $a^{11/2}$  and integrating with respect to time yields

$$a^{13/2} - a_0^{13/2} = 13/6 \sqrt{G(M_E + m_M)} \frac{m_M}{M_E} R_E^5 [F_{220}(I_M)]^2 d_{2200} \sin \delta_{2200} (t - t_0)$$

assuming the inclination, Love number, and phase angle remain constant. At the early time  $t_0$  when the moon was close to the earth  $a_0 \approx 0$ . Hence the tidal friction age of the earth-moon system is approximately

$$T \approx \frac{6}{13} \frac{M_E d_M^{13/2}}{\sqrt{G(M_E + m_M)} m_M [F_{220}(I_M)]^2 d_{2200} \sin \delta_{2200}}$$

$$\approx \frac{0.0469}{d_{2200} \sin \delta_{2200}} \times 10^9 \text{ yr.}$$

The above equation gives  $T = 1.4 \times 10^9$  yr using the weighted average  $s_{2200}$  value for all the satellites, and  $T = 2.4 \times 10^9$  yr using the BE-C and GEOS-I data only. These times are obviously much shorter than the age of  $4.6 \times 10^9$  yr for the earth and moon determined by radioactive dating. A way out of this time scale difficulty has been pointed out by Lambeck (1975). He notes that the tidal torques may have been much smaller in the distant past when the oceans did not flood the continental shelves, and that the ocean basin configuration was much different than it is now, due to continental drift.

## DISCUSSION

One might wonder whether the variation in the effective Love numbers is in fact due to the ocean tides and not due to frequency-dependence of the solid earth Love number. Alterman, et al. (1959) show that  $k_2$  does vary with frequency. However, the predicted change in Love number over the tidal frequencies is much smaller than that observed here.

Another possibility is core-mantle resonance. The theories of Jeffreys and Vincente (1957) and Molodensky (1961) both predict a variation in Love number



near the diurnal frequency on the same order of magnitude as that observed here. These theories would not explain the observed differences at frequencies away from the diurnal frequency; but core-mantle resonance cannot be ruled out as a possible contributor to the Love number variation.

Our results lend support to the ocean tide hypothesis of Lambeck, et al. (1974), and indicate what can be done when more data become available. They also indicate directions for further study. Regularly spaced and densely packed laser observations, for instance, would give good information on the short-period  $M_2$  tide. Observations of a low-inclination satellite would also increase the amplitude of the  $M_2$  signal, thus determining it more reliably. If the effective Love number of the  $P_1$  tide is really as small as our data suggests, then a mathematical model of the  $P_1$  ocean tide would be of great interest.

#### NOTATION

$a^*I^*e^*M^*\Omega^*\omega^*$  orbital elements of disturbing body (sun or moon)

$aIeM\Omega\omega$  orbital elements of satellite

$C$  moment of inertia of the earth

$C_{nst}^{\pm}$  ocean amplitude

$d_{\ell mpq}$	effective tidal Love number
$G$	universal constant of gravitation
$k_2$	solid earth Love number, degree 2
$k'_s$	load deformation coefficient, degree s
$m^*$	mass of disturbing body (sun or moon)
$M_E$	mass of the earth
$2\pi n\tau$	tidal argument
$R_E$	radius of the earth
$\delta_{\ell mpq}$	effective tidal phase angle
$\epsilon_{\ell mpq}$	solid earth tidal phase angle
$\epsilon_{st}^{\pm}$	ocean tide phase angle

$\dot{\theta}$  rotational speed of the earth

$\bar{\rho}_E$  average density of the earth

$\rho_w$  density of sea water

$\phi_2$  solid earth tidal lag angle

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## APPENDIX 1

We discuss here the rates of change of the lunar orbital elements and the orientation and spin of the earth under the influence of tidal friction, and the dissipation of tidal energy.

We treat the earth-moon-sun system as two separate systems, namely earth-moon and earth-sun. Strictly speaking, this is impermissible, since we are dealing with a three body problem. However, the errors made in doing this are small compared to the uncertainties in determining the effective tidal Love numbers and phase angles.

In the following equations we follow the formalism of Kaula (1964), using the sign convention of Lambeck, et al. (1974) and the corrections for the two body problem of Rubincam (1975, Appendix 1).

The secular rate of change in time of the lunar semimajor axis is given by (Kaula, 1964)

$$\dot{a} = \sum_{\ell, m, p, q} [\dot{a}]_{\ell m p q}$$

where

$$[\dot{a}]_{\ell m p q} = 2\sqrt{G(M_E + m_M)} \frac{m_M}{M_E} \frac{R_E^{2\ell+1}}{a_M^{2\ell+3/2}} \frac{(\ell-m)!}{(\ell+m)!} (2-\delta_{0m})(\ell-2p+q) \\ \cdot [G_{\ell p q}(e_M) F_{\ell m p}(i_M)]^2 d_{\ell m p q} \sin \delta_{\ell m p q}$$

The moon's mean motion  $n_M$  is related to  $a_M$  by

$$n_M = \frac{\sqrt{G(M_E + m_M)}}{a_M^{3/2}}$$

so that 
$$\frac{dn_M}{dt} = -3/2 \sqrt{G(M_E + m_M)} a_M^{-5/2} \frac{da_M}{dt}$$

Thus 
$$[n_M]_{\ell mp q} = -3 \frac{G(M_E + m_M)}{a_M^3} \frac{m_M}{M_E} \left(\frac{R_E}{a_M}\right)^{2\ell+1} \frac{(\ell-m)!}{(\ell+m)!} (2 - \delta_{0m})$$

$$\cdot (\ell - 2p + q) [G_{\ell pq}(e_M) F_{\ell mp}(I_M)]^2 d_{\ell mp q} \sin \delta_{\ell mp q}.$$

The components of the rate of change of the lunar orbital eccentricity are given by (Kaula, 1964)

$$[\dot{e}_M]_{\ell mp q} = \sqrt{G(M_E + m_M)} \frac{m_M}{M_E} \frac{R_E^{2\ell+1}}{a_M^{2\ell+3/2}} \frac{(1 - e_M^2)^{1/2}}{e_M} \frac{(\ell-m)!}{(\ell+m)!} (2 - \delta_{0m})$$

$$\cdot [(1 - e_M^2)^{1/2} (\ell - 2p + q) - (\ell - 2p)] [G_{\ell pq}(e_M) F_{\ell mp}(I_M)]^2 d_{\ell mp q} \sin \delta_{\ell mp q}.$$



Let us call the angle between the plane of the lunar orbit and the ecliptic  $J$ .

Then we have approximately (Rubincam, 1975, Appendix 1)

$$[\dot{J}]_{\ell mpq} = \sqrt{G(M_E + m_M)} \frac{m_M}{M_E} \frac{R_E^{2\ell+1}}{a_M^{2\ell+5/2}} \frac{(\ell-m)!}{(\ell+m)!} (2 - \delta_{0m})$$

$$\cdot \frac{(\ell-2p) \cos I_M - m}{(1-e_M^2)^{1/2} \sin I_M} [G_{\ell pq}(e_M) F_{\ell mp}(I_M)]^2 d_{\ell mpq} \sin \delta_{\ell mpq}.$$

We now turn our attention to the earth. Note that both lunar and solar tidal friction disturb the earth. This is in contrast to the treatment above, where only lunar tidal friction disturbs the moon's orbit. The tidal bulge raised by the moon is geared to the lunar motion, but the solar tidal bulge is not.

From considerations of the conservation of angular momentum the rate of change of the earth's equatorial tilt to the ecliptic is given by (Rubincam, 1975, Appendix 1)

$$[\dot{I}_S]_{\ell mpq} = \frac{Gm^*{}^2}{R_E C \dot{\theta}} \left( \frac{R_E}{a^*} \right)^{2\ell+2} \frac{(\ell-m)!}{(\ell+m)!} (2 - \delta_{0m}) \left[ \frac{(\ell-2p) - m \cos I^*}{\sin I^*} \right]$$

$$\cdot [G_{\ell pq}(e^*) F_{\ell mp}(I^*)]^2 d_{\ell mpq} \sin \delta_{\ell mpq}$$

and the slowdown in the earth's rotation by

$$[\ddot{\theta}]_{\ell mpq} = - \frac{Gm^*{}^2}{R_E C} \left( \frac{R_E}{a^*} \right)^{2\ell+2} \frac{(\ell-m)!}{(\ell+m)!} (2-\delta_{0m}) m$$

$$\cdot [G_{\ell pq}(e^*) F_{\ell mp}(I^*)]^2 d_{\ell mpq} \sin \delta_{\ell mpq}.$$

Let us now derive the rate of dissipation of tidal energy in the earth.

The orbital energy in the center of mass frame is

$$E_0 = - \frac{GM_E m^*}{2a^*}$$

and the rotational energy of the earth is

$$E_r = \frac{1}{2} C \dot{\theta}^2$$

Therefore the total mechanical energy is simply

$$E = E_0 + E_r = - \frac{GM_E m^*}{2a^*} + \frac{1}{2} C \dot{\theta}^2.$$

Thus the rate of dissipation of energy is

$$\dot{E} = \frac{GM_E m^*}{2a^*} \frac{da^*}{dt} + C \dot{\theta} \frac{d\dot{\theta}}{dt}.$$

From the previous equations we derive the relatively compact expression

$$[\dot{E}]_{\ell mpq} = \frac{Gm^*2}{R_E} \left( \frac{R_E}{a^*} \right)^{2\ell+2} \frac{(\ell-m)!}{(\ell+m)!} (2 - \delta_{0m})$$

$$\cdot [(\ell - 2p + q)n^* - m\dot{\theta}] [G_{\ell pq}(e^*) F_{\ell mp}(I^*)]^2 d_{\ell mpq} \sin \delta_{\ell mpq}$$

It will be noted that the above equations all have the form

$$[\dot{X}]_{\ell mpq} = P_{\ell mpq} s_{\ell mpq}$$

where  $X$  is the quantity of interest,  $s_{\ell mpq} = d_{\ell mpq} \sin \delta_{\ell mpq}$ , and  $P_{\ell mpq}$  is a multiplicative factor whose value is easily computed. Table 5 gives the  $P_{\ell mpq}$  for  $\ell = 2$  (the degree which dominates the evolution of the earth-moon system) and  $q = 0$ . In the computations for  $P_{2mp0}$  the lunar inclination functions  $F_{\ell mp}(I_M)$ , which change with time due to the motion of the lunar mode, are assumed to take on their average values. Also,  $G_{2p0}(e^*)$  is taken to be 1.

Table 5 gives us some insight in determining which tides are important in changing what quantities. It is clear that the  $M_2$  tide governs the rates of change of  $n_M$ ,  $a_M$ ,  $\dot{\theta}$ , and  $E$ . The  $O_1$ ,  $K_1^M$ , and  $M_2$  tides appear to be about equally important in changing  $J$  and  $I_s$ . The table gives the appearance of the  $M_2$  tide governing the change in  $e_M$ ; but it is probably the  $N_2$  ( $\ell mpq = 2201$ ) and  $L_2$  ( $\ell mpq =$

220(-1) ) tides which dominate the change in the lunar orbital eccentricity. These tides are not given in the table.

## APPENDIX 2

We wish to show here how the ocean tides combine with the solid earth tides to give the total tidal potential, as explained by Lambeck, et al. (1974).

The potential of a particular ocean tide constituent  $n$  is given by (Lambeck, et al., 1974)

$$U_n = \frac{4\pi G R_E^2}{a} \rho_w \sum_{s,t,u,v} \sum_{+} \frac{1+k'_s}{1+2s} \left(\frac{R_E}{a}\right)^s C_{nst}^{\pm} F_{stu}(I) G_{suv}(e) \cdot \begin{bmatrix} \sin \\ -\cos \end{bmatrix} \begin{cases} (s-2u)\omega + (s-2u+v)M + t(\Omega - \theta) \pm 2\pi n f T + \epsilon_{st}^{\pm} & s-t \text{ even} \\ & s-t \text{ odd} \end{cases}$$

Note that a spherical harmonic in the tide-raising potential excites many spherical harmonics in the ocean tide response; hence the summations in the equation above.

We may simplify the expression above by getting rid of small terms which depend upon the satellite's mean anomaly  $M$  and eccentricity  $e$  by setting  $v = 0$ ,  $G_{su0}(e) \approx 1$ , and  $s - 2u + v = 0$  (which implies  $s$  is even and  $u = s/2$ ). The equation then becomes

$$U_n = \frac{4\pi G R_E^2}{a} \rho_w \sum_{\substack{\text{even } s \\ t}} \sum_{+} \frac{1+k'_s}{1+2s} \left(\frac{R_E}{a}\right)^s C_{nst}^{\pm} F_{st(s/2)}(I) \cdot \begin{bmatrix} \sin \\ -\cos \end{bmatrix} \begin{cases} t(\Omega - \theta) \pm 2\pi n f T + \epsilon_{st}^{\pm} & s-t \text{ even} \\ & s-t \text{ odd} \end{cases}$$

Let us now convert the tidal frequency into orbital elements with the correspondence

$$-2\pi n f T \doteq (\ell - 2p)\omega^* + (\ell - 2p + q)M^* + m(\Omega^* - \theta) - m\pi.$$

The correspondence is not exact (Lambeck, et al., 1973) and more detailed considerations must be given if the period of time under consideration is more than a few years. We now have

$$U_{\ell mpq} = \frac{4\pi G R_E^2}{a} \rho_w \sum_{\substack{\text{even } s \\ t}} \sum_{+} \frac{1 + k'_s}{1 + 2s} \left(\frac{R_E}{a}\right)^s C_{(\ell mpq)st}^{\pm} F_{st(s/2)}(I) \\ \cdot \begin{bmatrix} \sin \\ -\cos \end{bmatrix} \left\{ t(\Omega - \theta) \mp [(\ell - 2p)\omega^* + (\ell - 2p + q)M^* + m(\Omega^* - \theta) - m\pi] + \epsilon_{st}^{\pm} \right\} \begin{matrix} s-t \text{ even} \\ s-t \text{ odd} \end{matrix}$$

where the subscript  $n$  has been replaced by  $(\ell mpq)$ .

Let us now get rid of terms which depend upon the earth's rotation  $\theta$ . The only way to do this is to pick the plus (+) in  $\sum_{+}$  and set  $t = m$ . Then

$$\begin{bmatrix} \sin \\ -\cos \end{bmatrix} \left\{ -[(\ell - 2p)\omega^* + (\ell - 2p + q)M^* + m\Omega^*] - m\Omega + m\pi + \epsilon_{sm}^{+} \right\} \begin{matrix} s-m \text{ even} \\ s-m \text{ odd} \end{matrix} \\ = \begin{bmatrix} -\sin \\ \cos \end{bmatrix} \left\{ (\ell - 2p)\omega^* + (\ell - 2p + q)M^* + m\Omega^* - m\Omega - \epsilon_{sm}^{+} \right\} \begin{matrix} m \text{ even} \\ m \text{ odd} \end{matrix}$$

Also  $(4\pi/3) \bar{\rho}_E R_E^3 = M_E$ , so that we may write

$$\begin{aligned}
 U_{\ell mpq} &= \frac{3GM_E}{R_E^2} \left( \frac{\rho_w}{\bar{\rho}_E} \right) \sum_{\substack{s=2,4,\dots \\ m}} \frac{1+k'_s}{1+2s} \left( \frac{R_E}{a} \right)^{s+1} C_{(\ell mpq)sm}^+ F_{sm(s/2)} (I) \\
 &\quad \cdot \begin{bmatrix} -\sin \\ \cos \end{bmatrix} \left\{ (\ell-2p)\omega^* + (\ell-2p+q)M^* + m\Omega^* - m\Omega - \epsilon_{sm}^+ \right\} \begin{matrix} m \text{ even} \\ m \text{ odd} \end{matrix} \\
 &= \frac{3GM_E}{R_E^2} \left( \frac{\rho_w}{\bar{\rho}_E} \right) \sum_{\substack{s=2,4,\dots \\ m}} \left( \frac{1+k'_s}{1+2s} \right) \left( \frac{R_E}{a} \right)^{s+1} C_{(\ell mpq)sm}^+ F_{sm(s/2)} (I) \\
 &\quad \cdot \begin{bmatrix} C_{(\ell mpq)sm}^+ \sin \epsilon_{sm}^+ \cos \left\{ \right\} & - C_{(\ell mpq)sm}^+ \cos \epsilon_{sm}^+ \sin \left\{ \right\} \\ C_{(\ell mpq)sm}^+ \cos \epsilon_{sm}^+ \cos \left\{ \right\} & + C_{(\ell mpq)sm}^+ \sin \epsilon_{sm}^+ \sin \left\{ \right\} \end{bmatrix} \begin{matrix} m \text{ even} \\ m \text{ odd} \end{matrix}
 \end{aligned}$$

where the empty curly brackets mean

$$\left\{ \right\} = (\ell-2p)\omega^* + (\ell-2p+q)M^* + m\Omega^* - m\Omega.$$

Compare this to the solid earth tidal potential, which for  $\ell = 2$ ;  $m > 0$ ;

$q = 0$  and small eccentricities is

$$\begin{aligned}
 U_{2mp0}^{\text{solid}} &= \frac{3Gm^*}{R_E} \frac{(2-m)!}{(2+m)!} F_{2mp}(I^*) \left( \frac{R_E}{a^*} \right)^3 \left( \frac{R_E}{a} \right)^3 F_{2m1}(I) \\
 &\quad \cdot [k_2 \cos \epsilon_{2mp0} \cos \left\{ \right\} - k_2 \sin \epsilon_{2mp0} \sin \left\{ \right\}] .
 \end{aligned}$$

Assuming that the total tidal potential is composed of the solid earth and ocean tides only, one may show from the expressions for the ocean and solid earth tidal potentials that

$$d_{2mp0} \cos \delta_{2mp0} = k_2 \cos \epsilon_{2mp0} + Z_{mp} (1 + k'_2) \begin{pmatrix} C_{(2mp0)2m}^+ \sin \epsilon_{2m}^+ & m \text{ even} \\ C_{(2mp0)2m}^+ \cos \epsilon_{2m}^+ & m \text{ odd} \end{pmatrix} \\ + Z_{mp} \cdot 5/9 (1 + k'_4) \left( \frac{R_E}{a} \right)^2 \frac{F_{4m2}(I)}{F_{2m1}(I)} \begin{pmatrix} C_{(2mp0)4m}^+ \sin \epsilon_{4m}^+ & m \text{ even} \\ C_{(2mp0)4m}^+ \cos \epsilon_{4m}^+ & m \text{ odd} \end{pmatrix}$$

and

$$d_{2mp0} \sin \delta_{2mp0} = k_2 \sin \epsilon_{2mp0} + Z_{mp} (1 + k'_2) \begin{pmatrix} C_{(2mp0)2m}^+ \cos \epsilon_{2m}^+ & m \text{ even} \\ -C_{(2mp0)2m}^+ \sin \epsilon_{2m}^+ & m \text{ odd} \end{pmatrix} \\ + Z_{mp} \cdot 5/9 (1 + k'_4) \left( \frac{R_E}{a} \right)^2 \frac{F_{4m2}(I)}{F_{2m1}(I)} \begin{pmatrix} C_{(2mp0)4m}^+ \cos \epsilon_{4m}^+ & m \text{ even} \\ -C_{(2mp0)4m}^+ \sin \epsilon_{4m}^+ & m \text{ odd} \end{pmatrix}$$

where

$$Z_{mp} = 3/10 \frac{(2+m)!}{(2-m)!} \left( \frac{M_E}{m^*} \right) \left( \frac{\rho_w}{\bar{\rho}_E} \right) \left( \frac{a^*}{R_E} \right)^3 \frac{1}{F_{2mp}(I^*) R_E}$$

The term in brackets at the end of each of the above equations for  $d_{2mp0} \cos \delta_{2mp0}$  and  $d_{2mp0} \sin \delta_{2mp0}$  represents the amount by which the second degree effective



Love numbers and phase angles will be corrupted by the fourth degree ocean tides, if the fourth degree terms are not solved for.

Care must be taken when solving for the effective Love numbers and phase angles of the  $K_1^M$  and  $K_1^S$  tides. The reason is that the  $C^+$  and  $\epsilon^+$  are given for the  $K_1 = K_1^M + K_1^S$  tide, and not for the  $K_1^M$  and  $K_1^S$  tides individually. Some hypothesis is needed to decompose the  $K_1$  into the  $K_1^M$  and  $K_1^S$  tides. Similar statements hold for the  $K_2^M$  and  $K_2^S$  tides.

## APPENDIX 3

### A. PURPOSE

The computer program solves for the effective frequency-dependent tidal Love numbers and phase angles for the whole earth (solid earth + oceans + atmosphere). It does it by performing a multiple regression analysis on the observed tidal perturbation in the inclination of the orbit of an earth satellite. It also solves for ocean tide amplitudes and phases from the Love numbers and lag angles found from the regression analysis, given an assumed tidal response for the solid earth.

All tides are considered to be of second degree only, and only tides which depend on the first power of the orbital eccentricity of the disturbing body are retained; hence the subscripts on the inclination and eccentricity functions run as follows:  $l = 2$ ;  $m = 1, 2$ ;  $p = 0, 1, 2$ ; and  $q = -1, 0, 1$ . Within these limits, any combination of tidal constituents may be chosen to fit the data, giving their effective Love numbers and effective phase angles. Also, the phase angle of any constituent solved for can be set to zero, resulting in a solution for the Love number only for that constituent. There is no restriction on the number of different regression analyses that can be carried out on the data during a run of the program. For example, the sample data cards given in the listing of the main program give two regression analyses.

In practice only the few constituents which give the largest signal in the inclination are fit. If these are not known, then a call to subroutine THEORY gives the theoretical amplitudes and periods of all the constituents in the solid earth signal, given an assumed Love number for the solid earth, such as 0.30. These can be used as a guide for picking out the important constituents. The subroutine also gives a sample plot of inclination vs. time, if this is desired.

The precession of the lunar orbit around the ecliptic requires a certain amount of averaging to be done on the input data for the moon; this is explained in section D. Suffice it to say here that the motion of the lunar node and the moon in its orbit with respect to the earth's equator are average rates over the data span; the inclination of the lunar orbit to the earth's equator is assumed to be constant and equal to its average over the data span. If the data span is longer than four or five years, then a different program taking the precession of the orbit into account more exactly will be needed.

## B. THE EXPRESSION FOR THE TIDAL INCLINATION PERTURBATION

The expression for the tidal inclination perturbation is

$$\Delta I = \sum_{m,p,q} \Delta I_{2mpq} + \Delta I_0$$

where

$$\Delta I_{2mpq} = d_{2mpq} \left[ 2 \frac{(2-m)!}{(2+m)!} \right] m \left[ \frac{Gm^*}{\sqrt{GM_E}} \frac{R_E^5}{a^{*3} a^{7/2}} \right] [F_{2mp}(I^*) F_{2ml}(I)] [G_{2pq}(e^*)]$$

$$\cdot \left[ \frac{1}{\sin I_0} \right] \cos \left[ \frac{(2-2p)(\dot{\omega}^* + \dot{M}^*) + q\dot{M}^* + m\dot{\Omega}^* - m\dot{\Omega} + \delta_{2mpq}}{|(2-2p)(\dot{\omega}^* + \dot{M}^*) + q\dot{M}^* + m\dot{\Omega}^* - m\dot{\Omega}|} \right]$$

The program names of the variables in the above equation and in which subroutine they are computed are given below.

<u>Variable</u>	<u>Program Name</u>	<u>Subroutine</u>
$d_{2mpq}$	YKM(LM,LP,LQ),YKS(LM,LP,LQ)	REGRES,LOVNUM
$\delta_{2mpq}$	EPSLNM(LM,LP,LQ),EPSLNS(LM,LP,LQ)	REGRES,LOVNUM
$2 \frac{(2-m)!}{(2+m)!}$	B1(LM)	BLM
$m$	YLM	LOVNUM
$\frac{Gm^*}{\sqrt{GM_E}} \frac{R_E^5}{a^{*3}a^{7/2}}$	CFNTM,CFNTS	COEFF
$I^*$	XIMOON,XISUN	READMS
$F_{2mp}(I^*)$	A1(LM,LP),B(LM,LP)	INCL
$I$	XI	RDSAT
$F_{2mp}(I)$	C(LM,LP)	INCL
$e^*$	EMOON,ESUN	ECCFUN
$G_{2pq}(e^*)$	GLPQM(LP,LQ),GLPQS(LP,LQ)	ECCFUN
$\sin I_0$	SS	MAIN
$\dot{\omega}^* + \dot{M}^*$	XNDM,XNDS	READMS,MAIN
$\dot{M}^*$	XMDOTM,XMDOTS	READMS,MAIN

Variable	Program Name	Subroutine
$\dot{\Omega}^*$	OMGDOT	READMS
$\dot{\Omega}$	Q	RDSAT
$(2-2p)(\dot{\omega}^* + \dot{M}^*) + q\dot{M}^* + m\dot{\Omega}^* - m\dot{\Omega}$	ARGDTM(LM,LP,LQ),ARGDTS(LM,LP,LQ)	ARGDOT
$\omega^* + M^*$	XNDM*(TT-TMS)+DELMN, XNDS*(TT-TMS)+DELSUN	READMS,ARG
$M^*$	XMDOTM*(TT-TMS)+XMEANM, XMDOTS*(TT-TMS)+XMEANS	READMS,ARG
$\Omega^*$	OMGDOT*(TT-TMS)+OMEGAM, OMEGAS	READMS,ARG
$\Omega$	Q*(TT-TZERO)+XNODE	RDSAT,ARG
$\cos \left\{ \begin{array}{l} \Omega \\ \Delta I_0 \end{array} \right\}$	ARGUM(LM,LP,LQ),ARGUS(LM,LP,LQ)	ARG
$\Delta I_0$	ANS(1),XI0	REGRES,LOVNUM

The regression coefficients are found by writing

$$\Delta I_{2mpq} = d_{2mpq} \cos \delta_{2mpq} \left[ \begin{array}{l} \Omega \\ \Delta I_0 \end{array} \right] \cos \left\{ (2-2p)(\omega^* + M^*) + qM^* + m\Omega^* - m\Omega \right\} \\ - d_{2mpq} \sin \delta_{2mpq} \left[ \begin{array}{l} \Omega \\ \Delta I_0 \end{array} \right] \sin \left\{ (2-2p)(\omega^* + M^*) + qM^* + m\Omega^* - m\Omega \right\}$$

so that the data are of the form

$$y_i = \sum_j a_j x_{ij} + b$$

where the regression coefficients  $a_j$  are  $d_{2mpq} \cos \delta_{2mpq}$  and  $-d_{2mpq} \sin \delta_{2mpq}$ , and

$b$  is  $\Delta I_0$ ,  $d_{2mpq}$  and  $\delta_{2mpq}$  can obviously be solved for from the regression coefficients.

### C. BRIEF SUMMARY OF OPERATION

The program begins by reading in the satellite data; the sun and moon data; TSTART, TEND and DT; the assumed solid earth Love number and load deformation coefficient; and the solid earth tidal lag angle. Next, parts of the tidal inclination perturbation are computed. Subroutines TIME1 and CORRES are called, which are used in the plotting and printing of the inclination perturbation and residuals against time.

The program then reads in JTHORY and JPLOT; if JTHORY = 0, then the regression analysis is done without calling subroutine THEORY. If JTHORY = 1, then subroutine THEORY is called but no regression analysis is done. JTHORY = 2 does both. If subroutine THEORY is called and a sample plot of the solid earth signal is desired, then JPLOT should be 1. If no plot of the solid earth signal is desired, then set JPLOT = 0.

The regression analysis begins by calling subroutine LASDTA, which reads in the observed inclination. Subroutine REGRES is then called, which reads data cards to determine what constituents are to be solved for. The comments given in REGRES tell how to pick the constituents. Subroutine REGRES computes the regression coefficients and their errors, prints them and calls subroutine LOVNUM.

Subroutine LOVNUM computes the effective frequency-dependent Love numbers and phase angles and their errors from the regression coefficients and their errors. Then it computes the ocean tide amplitudes and phases from these

by subtracting out the solid earth tide. All of these results are then printed and the inclination and residuals vs. time are printed and plotted.

#### D. SAMPLE INPUT

The sample input is listed in the main program. Each data card (number) and each number on the data card (letter) are discussed below.

1. The satellite name and when the data were taken are given.
2. a. The semimajor axis of the orbit is  $8.07291 \times 10^8$  cm.  
b. The eccentricity of the orbit is 0.0726.  
c. The rate at which the node progresses along the earth's equator is  
-2.246536 degrees/day. This figure is obtained by noting that on Feb. 7, 1966 near the beginning of the data span the node position was -109.08202 degrees, and on Oct. 26, 1967 near the end of the data span the node position was -75.41322 degrees. (All times are 0 hours UT.) Hence the rate is

$$\frac{-1440 + 109.08202 - 75.41322}{626} = -2.246536 \text{ degrees/day}$$

where the -1440 = -4(360) indicates four complete revolutions of the node.

- d. The inclination of the orbit is 59.38053 degrees with respect to the earth's equator.

- e. TZERO is Feb. 7, 1966 12 hrs UT, so TZERO = 38.5.
- f. The node position of the satellite at time TZERO was -109.08202 degrees.

The American Ephemeris and Nautical Almanac (Nautical Almanac for short) and Figure 7 are used for obtaining the numbers on the next two data cards.

- 3. a. The positions of the moon and sun are given for Feb. 4, 1966 in the Nautical Almanac, near the beginning of the data span; hence TMS is taken as TMS = 35.0. On this day the position of the lunar node on the ecliptic was  $\Omega = 60.8500$  degrees, according to the Almanac. The position of the lunar node on the earth's equator is found from the formula

$$\tan \Omega^* = \frac{\sin J \sin \Omega}{\sin I \cos J + \cos I \sin J \cos \Omega}$$

where  $J = 5.1453964$  degrees = inclination of the lunar orbit to the ecliptic, and  $I = 23.44319$  degrees = inclination of the ecliptic to the earth's equator. Solving the equation gives  $\Omega^* = 10.1770$  degrees.

- b. DELTA1 is  $\omega^* + M^*$  (measured from the earth's equator); so

$$\text{DELTA1} = \omega^* + M^* = (( - \Omega + c$$

where  $(($  and  $\Omega$  are given by the Almanac and  $c$  is the arc shown in Figure 7.  $c$  can be found from the formula

$$\cos c = \frac{\cos I - \cos I^* \cos J}{\sin I^* \sin J}$$



where  $I^*$ , the inclination of the lunar orbit to the earth's equator is given by

$$\cos I^* = \cos I \cos J - \sin I \sin J \cos \Omega$$

We find that on Feb. 4, 1966  $I^* = 26.3140$  degrees,  $c = 51.6092$  degrees,  $(( = 115.2340$  degrees, and  $\Omega = 60.8500$  degrees. Hence  $\text{DELTA1} = 105.9932$  degrees.

- c. The nodal position of the sun is always 0.0 degrees.
- d.  $\text{DELTA2} = \omega^* + M^*$  for the sun is 313.7163 degrees, according to the Almanac.
- e. The speed at which the moon moves around in its orbit averaged over the data span is  $\text{XNDM1} = \dot{\omega}^* + \dot{M}^* = 13.183848$  degrees/day. This is found by computing the lunar position on Oct. 27, 1967 at the end of the data span. We find that  $\Omega^* = 5.0417$  degrees,  $I^* = 28.1025$  degrees,  $c = 22.9427$  degrees, and  $\omega^* + M^* = 131.8174$  degrees. Subtracting this last figure from  $\omega^* + M^*$  for Feb. 4, 1966 and making allowance for 23 revolutions of the moon gives

$$\text{XNDM1} = \frac{23(360) + 131.8174 - 105.9932}{630} = 13.183848 \text{ degrees/day.}$$

- f. The average speed of the moon's node on the equator is

$$\text{OMGDT1} = \frac{5.0417 - 10.1770}{630} = -0.00815 \text{ degrees/day.}$$

4. a. The inclination of the moon's orbit to the earth's equator averaged over the data span is

$$XID1 = \frac{26.3140 + 28.1025}{2} = 27.2082 \text{ degrees}$$

- b. The inclination of the solar orbit to the earth's equator is 23.44319 degrees.
- c. TMS is 35.0 days (Feb. 4, 1966).
- d. The position of the lunar mean anomaly on Feb. 4, 1966 is  $((-\Gamma) = 331.5588$  degrees, according to the Almanac.
- e. The solar mean anomaly on Feb. 4, 1966 is 31.3590 degrees, according to the Almanac.
5. a. TSTART is 37.0 days (Feb. 6, 1966).
- b. TEND is 666.0 days (Oct. 28, 1967).
- c. DT is 2.0 days.
6. a. The solid earth Love number is taken to be 0.30.
- b. The load deformation coefficient of the solid earth is taken to be -0.30.
7. The solid earth tidal lag angle is taken to be 0.0.
8. a. Both the theoretical amplitudes and regression analysis are wanted, so JTHORY = 2.
- b. A plot of the theoretical tidal signal is wanted, so JPLOT = 1.
9. a. There are 142 data points.
- b. TDAY is 38.5, since this is the date of the first data point and the time on the following cards is measured from the first data point.

10. a. The tidal inclination perturbation of the first data point is  $-1.1594475$  arc seconds.
- b. The time of the first data point is 0.0 days.
11. a. The tidal inclination perturbation of the second data point is  $-0.89708115$  arc seconds.
- b. The time of the second data point is 13.0 days after the first.
- 12-151. The rest of the data cards.
152. a. The name of the satellite is GEOS I.
- b. There are 142 data points.
- c. There are 68 independent variables + 1 dependent variable = 69 variables.
- d. Two subset selection cards follow.
153. a. Eight variables are chosen for this regression analysis.
- b-i. Fit the  $K_1$  tide (9 and 10), the  $K_2$  tide (27 and 28), the  $P_1$  tide (39 and 40), and the  $S_2$  tide (55 and 56) for effective Love numbers and phase angles.
154. a. Seven variables are chosen for this regression analysis.
- b-c. Fit the  $K_1$  and  $S_2'$  tides for effective Love numbers and phase angles (9 and 10, 55 and 56).
- d-g. Fit the  $M_2$ ,  $K_2$ , and  $P_1$  tides for effective Love numbers but no phase angles (which are forced to be zero).

## COMPUTER PROGRAM LISTING

# MAIN PROGRAM

THIS PROGRAM SOLVES FOR THE EFFECTIVE FREQUENCY-DEPENDENT TIDAL LOVE NUMBERS AND LAG ANGLES FOR THE WHOLE EARTH BY CARRYING OUT A MULTIPLE REGRESSION ANALYSIS ON THE TIDAL PERTURBATION IN THE INCLINATION OF THE ORBIT OF AN EARTH SATELLITE. IT ALSO SOLVES FOR OCEAN TIDE AMPLITUDES AND PHASES FROM THE LOVE NUMBERS AND LAG ANGLES FOUND, GIVEN THE TIDAL RESPONSE OF THE SOLID EARTH.

ONLY 2ND DEGREE TIDES ARE CONSIDERED, AS WELL AS ONLY TERMS WHICH DEPEND ON THE FIRST POWER OF ORBITAL ECCENTRICITY. HENCE THE SUBSCRIPTS ON THE INCLINATION AND ECCENTRICITY FUNCTIONS RUN AS FOLLOWS  $L=2$ ,  $M=1,2$ ,  $P=0,1,2$ , AND  $Q=-1,0,1$ . (SINCE THE COMPUTER CANNOT HANDLE ZERO SUBSCRIPTS, IN THIS PROGRAM THEY RUN AS FOLLOWS  $LM=0$ ,  $LP=0+1$ , AND  $LQ=0+2$ .) WITHIN THESE LIMITS, ANY COMBINATION OF TIDAL CONSTITUENTS MAY BE CHOSEN FOR FITTING TO THE DATA. IN PRACTICE, ONLY THE FEW CONSTITUENTS WHICH GIVE THE LARGEST SIGNAL IN THE INCLINATION ARE FIT. (THE IMPORTANT SIGNALS MAY BE FOUND BY CALLING SUBROUTINE THEORY.)

IMPORTANT NOTE IN THIS PROGRAM TIDAL INCLINATION PERTURBATION IS ABBREVIATED TIP.

## BRIEF DESCRIPTION OF EACH SUBROUTINE

ARG - COMPUTES THE COSINE TERM IN THE EXPRESSION FOR THE TIP  
 ARGDOT - COMPUTES THE DERIVATIVE OF THE ARGUMENT OF THE COSINE TERM IN THE TIP  
 ARGSLT - COMPUTES SINES AND COSINES TO BE USED IN SUBROUTINE DATA  
 BLM - COMPUTES THE FACTORIAL TERM IN THE TIP  
 COEFF - COMPUTES THE COEFFICIENT IN THE TIP OF THE FORM  $CONSTANT/(A^{1/2})$   
 CUPRES - USED ONLY BY SUBROUTINE PLOTTER TO DETERMINE WHETHER AN EXPERIMENTAL DATA POINT SHOULD BE PLOTTED AT A PARTICULAR TIME  
 DATA - COMPUTES VALUES TO BE USED IN REGRESSION ANALYSIS  
 ECCFUN - COMPUTES ECCENTRICITY FUNCTIONS  
 INCL - COMPUTES INCLINATION FUNCTIONS  
 LAGI - READS IN SOLID EARTH LAG ANGLE  
 LAGS - SETS THE FREQUENCY DEPENDENT LAG ANGLES INITIALLY EQUAL TO ZERO  
 LAGDTA - READS IN THE OBSERVED TIP  
 LOVE - READS IN THE SOLID EARTH LOVE NUMBER AND LOAD DEFORMATION COEFFICIENT  
 LUNUM - TAKES THE OUTPUT OF REGRES AND COMPUTES FREQUENCY-DEPENDENT LOVE NUMBERS, LAG ANGLES, AND OCEAN TIDE PARAMETERS  
 PLOTTER - PLOTS OUT THE TIP, EXPERIMENTAL DATA POINTS, AND THE RESIDUALS ON THE COMPUTER PAPER  
 POSAT - READS IN SATELLITE ELEMENTS  
 READML - READS IN SUN AND MOON POSITIONS, RATES  
 REGRES - PERFORMS REGRESSION ANALYSIS  
 THEORY - COMPUTES AMPLITUDE, PERIODS OF THE SOLID EARTH TIDAL SIGNAL  
 TIMEI - COMPUTES TIME VALUES FOR ARRAY T(I)

## NOTATION

### SATELLITE

A - SEMI-MAJOR AXIS IN  $10^8$  CM  
 C(LM,LP) - INCLINATION FUNCTIONS  
 E - ORBITAL ECCENTRICITY  
 Q - RATE OF CHANGE OF NODE POSITION  
 SAT(J) - ALPHANUMERIC INFORMATION, SUCH AS NAME OF SATELLITE  
 SS - SINE OF SATELLITE INCLINATION  
 TZERO - TIME (MEASURED FROM BEGINNING OF THE YEAR) WHEN THE NODE HAD VALUE XNODE  
 XI - SATELLITE INCLINATION  
 XNODE - POSITION OF NODE AT TIME TZERO

### MOON AND SUN

ORIGINAL PAGE IS  
 OF POOR QUALITY

C	ARGUM(LM,LP,LQ)	- COSINE TERM IN THE TIP
C	ARGUS(LM,LP,LQ)	
C	ARGUTM(LM,LP,LQ)	- RATE OF CHANGE OF ARGUMENT OF COSINE IN THE TIP
C	ARGDTS(LM,LP,LQ)	
C	A1(LM,LP)	- INCLINATION FUNCTIONS OF MOON
C	B(LM,LP)	
C	CFNTM	- TERM IN TIP OF FORM CONSTANT/( $\pi \times 7/2$ )
C	CFNTS	
C	DELMN	- (ARGUMENT OF PERIGEE + MEAN ANOMALY) OF MOON AT TIME
C	DELSUN	TMS, MEASURED WITH RESPECT TO EARTH'S EQUATOR
C	EMOON	- ECCENTRICITY OF LUNAR ORBIT
C	ESUN	
C	EPSLNM(LM,LP,LQ)	- EFFECTIVE FREQUENCY-DEPENDENT LAG ANGLE FOR LUNAR TIDES
C	EPSLNS(LM,LP,LQ)	
C	GLPQM(LP,LQ)	- ECCENTRICITY FUNCTION FOR MOON
C	GLPOS(LP,LQ)	
C	OMEGAM	- POSITION OF LUNAR NODE ON EARTH'S EQUATOR
C	OMEGAS	
C	XIMCOON	- INCLINATION OF LUNAR ORBIT TO EARTH'S EQUATOR
C	XISUN	
C	XMDOTM	- RATE OF CHANGE OF LUNAR MEAN ANOMALY
C	XMDOTS	
C	XMOON(LM,LP,LQ)	- LUNAR PART OF TIP
C	XSUN(LM,LP,LQ)	
C	XNDM	- RATE OF CHANGE OF (ARGUMENT OF PERIGEE + MEAN ANOMALY)
C	XNDS	OF MOON, WITH RESPECT TO THE EARTH'S EQUATOR
C	YKM(LM,LP,LQ)	- EFFECTIVE FREQUENCY-DEPENDENT LOVE NUMBER FOR LUNAR
C	YKS(LM,LP,LQ)	TIDES
C	TMS	- TIME OF MOON AND SUN POSITIONS
C	DATA	
C	MEXP	- NUMBER OF DATA POINTS
C	TDAY	- CORRECTION TO TEXP(J) TO GIVE IT IN DAYS FROM THE
C	TEXP(J)	BEGINNING OF THE YEAR
C	XIEXP(J)	- TIME OF OBSERVATION XIEXP(J)
C	XIEXP(J)	- OBSERVED TIP AT TIME TEXP(J)
C	MISCELLANEOUS	
C	DT	- INTERVAL BETWEEN SUCCESSIVE VALUES OF T(L)
C	MT	- TOTAL NUMBER OF VALUES IN ARRAY T(L)
C	T(L)	- TIME VALUES BETWEEN AND INCLUDING TSTART AND TEND
C	TEND	- ENDING TIME OF DATA SPAN
C	TSTART	- STARTING TIME OF DATA SPAN
C	F	- CONVERSION FACTOR FROM DEGREES TO RADIANS
C	B1(LM)	- FACTORIAL PART OF THE TIP
C	XK	- SOLID EARTH LOVE NUMBER (SECOND DEGREE)
C	XKP	- LOAD DEFORMATION COEFFICIENT (SECOND DEGREE)
C	XI	- ADDITIVE CONSTANT IN TIP
C	XLAG	- LAG ANGLE OF SOLID EARTH TIDE
C	XINCL(L)	- THE COMPUTED TIP AT TIME T(L)
C	INDEX	- INDEX WHICH KEEPS TRACK OF TIME IN SUBROUTINE DATA
C	NTRACK(L)	- DETERMINES WHETHER A DATA POINT SHOULD BE PLOTTED AT
C	TIDE(LM,LP,LQ)	TIME T(L)
C	FACTOR	- CONTAINS ALPHANUMERIC NAMES OF TIDES (K1,M2, ETC.)
C		- USED IN SUBROUTINE LOVNUM AS A CORRECTION TO THE
C		LUNAR TIDES TO GET THE PROPER AMPLITUDE OF THE
C		LUNISOLAR TIDES



```

C
C SAMPLE INPUT (COLUMN 1 OF THE INPUT STARTS IN COLUMN 3 HERE)
C
C (SAT(J), J=1,14) (FORMAT 13A6,A2)
C GEOS - 1 , 1966-1967 DATA
C
C A E Q1 X11 TZERO XNODE1 (FORMAT 9F10.5)
C 8.07291 0.0726 -2.246535 59.38053 38.5 -109.0820
C
C OMEGA1 DELTA1 OMEGA2 DELTA2 XNDM1 CMGDT1 (FORMAT 8F10.5)
C 10.1770 105.9932 0.0 313.7163 13.19385 -0.00815
C
C XID1 XID2 TMS XMEAN1 XMEAN2 (FORMAT 9F10.5)
C 27.2082 23.44315 35.0 331.5588 31.3590
C
C ISTART TEND DT (FORMAT 8F10.5)
C 37.0 666.0 2.0
C
C XK XKP (FORMAT 8F10.5)
C 0.30 -0.30
C
C XLAG (FORMAT 8F10.5)
C 0.0
C
C JTHORY JPLQT (FORMAT 2I5)
C 2 1
C
C MEXP TDAY (FORMAT 15,F10.5)
C 142 38.5
C
C XIEXP(J) TEXP(J) (FORMAT 2D14.8)
C -.1159447ED 010.0 D 02
C -.89703115D 000.13
C ETC.
C
C PR,PR1 N M NS
C GEOS 1 14207 2
C
C K (ISAVE(J), J=1,K) (FORMAT 36I2)
C 3 91027283940555c
C 7 9102127393556
C
C
C
C IMPLICIT REAL*8 (A-H,O-Z)
C DIMENSION EPSLNM(2,3,3),EPSLNS(2,3,3),ARGUM(2,3,3),ARGUS(2,3,3),
C 1 ARGCTM(2,3,3),ARGDTS(2,3,3)
C DIMENSION E1(2),XMCQN(2,3,3),XSUN(2,3,3),YKM(2,3,3),YKS(2,3,3)
C DIMENSION TEXP(200),XIEXP(200),T(700),XINCL(700),NTRACK(700)
C DIMENSION C(2,3),A1(2,3),B(2,3),GLPQM(3,3),GLPQS(3,3)
C COMMON/BLKA/EP3LNM,EP3LNS,ARGUM,ARGUS,ARGDTM,ARGDTS
C COMMON/BLKB/B1,XK,CFNTM,CFNTS,SUM,XMODN,XSUN,YKM,YKS,XKP
C COMMON/BLKC/TEXP,XIEXP,T,XINCL,NTRACK
C COMMON/BLKD/XLAG,Q,OMEGAM,DELMN,MEGAS,DELSUN,SS,XIO,XA,E,XI,XNCOE,
C 1 TZERO,XIMCQN,XISUN,TMS,XNDM,XADS,F,XMEANM,XMEANS,XMDTM,XMDOTS,
C 2 CMGDT,MEXP
C COMMON/BLKG/C,A1,B,GLPQM,GLPQS,INDEX
C F=3.141592653589793D00
C XADS=(0.94584706)*F
C XMDTM=(11.06455200)*F
C XMDOTS=(0.585600)*F
C
C READ IN THE DATA, COMPUTE PARTS OF THE TIP
C
C CALL FDSAT
C CALL READMS
C READ (5,1) TSTART,TEND,DT
C FORMAT (8F10.5)
C WRITE (6,7) TSTART,TEND,DT
C FORMAT (//////,23X,'TSTART=',F10.1,5X,'TEND=',F10.4,5X,'DT=',
C 1 F10.4,5X,'(DAYS)')
C
C CALL LOVE
C CALL LAC1
C CALL LAG2
C SS=DSIN(X1)
C CALL FCCFUN
C CALL INCL(X1,C)
C CALL INCL(XIMCQN,A1)
C CALL INCL(XISUN,B)
C CALL BLN
C CALL ARGDT
C CALL CCLFF

```

```

ISN 0033      CALL TIME1(TSTART,TEND,DT,MT)
ISN 0034      INDEX=0
ISN 0035      MEXP=0
ISN 0036      CALL CORRES(TSTART,TEND,DT,MEXP)
ISN 0037      READ (5,2) JTHORY,JPLDT
ISN 0038      2  FORMAT (2I5)
C IF JTHORY=2, CALL THEORY, READ IN DATA POINTS, DO REGRESSION ANALYSIS
C IF JTHORY=1, CALL THEORY ONLY
C IF JTHORY=0, READ IN DATA AND DO REGRESSION ANALYSIS WITHOUT CALLING THEORY
C IF JPLDT=1, THEN A SAMPLE CURVE OF THE TIP WITH SOLID EARTH LOVE NUMBER=XK AND
C ZERO LAG ANGLE IS PLOTTED BY THEORY
      IF (JTHORY.EQ. 2) GO TO 6
      IF (JTHORY.EQ. 1) GO TO 3
      GO TO 4
ISN 0039      6  CALL THEORY(JPLDT,MT)
ISN 0040      CALL LASDTA
ISN 0041      CALL CORRES(TSTART,TEND,DT,MEXP)
ISN 0042      CALL REGRES(MT)
ISN 0043      GO TO 5
ISN 0044      3  CALL THEORY(JPLDT,MT)
ISN 0045      GO TO 5
ISN 0046      4  CONTINUE
ISN 0047      CALL LASDTA
ISN 0048      CALL CORRES(TSTART,TEND,DT,MEXP)
ISN 0049      CALL REGRES(MT)
ISN 0050      5  CONTINUE
ISN 0051      STOP
ISN 0052      END

```

```

ISN 0002      SUBROUTINE ARG(TT)
C
C THIS SUBROUTINE COMPUTES THE COSINE OF THE ARGUMENT OF THE TIP (I.E. IT
C COMPUTES THE COSINE OF (L - 2*P)*(ARGUMENT OF PERIGEE+MEAN ANOMALY) + C*(MEAN
C ANOMALY) + M*(NODE OF DISTURBING BODY) - M*(NODE OF SATELLITE) + TICAL LAG
C ANGLE).
C
      IMPLICIT REAL*8(A-H,C-Z)
      DIMENSION EPSLNM(2,3,3),EPSLNS(2,3,3),ARGUM(2,3,3),ARGUS(2,3,3),
      1 ARGDTM(2,3,3),ARGDTS(2,3,3)
      COMMON/BLKA/EP,SLNM,EP,SLNS,ARGUM,ARGUS,ARGDTM,ARGDTS
      COMMON/BLKD/XLAG,0,OMEGAM,DELMN,CMEGAS,DELSUN,SS,XID,A,E,XI,XNODE,
      1 TZERO,XIMODN,XISUN,TMS,XNDM,XNDS,F,XMEANM,XMEANS,XMCDTM,XMCDTS,
      2 UMGDOT,MEXP
      DO 10 LM=1,2
      YLM=LM
      DO 10 LP=1,3
      YLP=LP - 1
      DO 10 LQ=1,3
      YLQ=LQ - 2
      A2=(2.0D0 - 2.0D0*YLP)*(XNDM*(TT-TMS)+DELMN) + YLQ*(XMCDTM*(TT-
      1 TMS)+XMEANM)+YLM*(CMGDOT*(TT-TMS)+OMEGAM) - YLM*(Q*(TT-TZERO)+
      2 XNODE) + EPSLNM(LM,LP,LQ)
      ARGUM(LM,LP,LQ)=DCOS(A2)
      A3=(2.0D0 - 2.0D0*YLP)*(XNDS*(TT-TMS)+DELSUN) + YLQ*(XMCDTS*(TT-
      1 TMS)+XMEANS)+YLM*(CMGAS - YLM*(Q*(TT-TZERO) + XNODE)
      2 EPSLNS(LM,LP,LQ)
      ARGUS(LM,LP,LQ)=DCOS(A3)
ISN 0016      10 CONTINUE
ISN 0017      RETURN
ISN 0018      END
ISN 0019

```

```

ISN 0002      SUBROUTINE ARGDOT
C
C THIS SUBROUTINE COMPUTES THE ANGULAR SPEED OF EACH CONSTITUENT (I.E. IS
C THE TIME DERIVATIVE OF THE ARGUMENT COMPUTED IN SUBROUTINE ARG).
C
      IMPLICIT REAL*8(A-H,C-Z)
      DIMENSION EPSLNM(2,3,3),EPSLNS(2,3,3),ARGUM(2,3,3),ARGUS(2,3,3),
      1 ARGDTM(2,3,3),ARGDTS(2,3,3)
      COMMON/BLKA/EP,SLNM,EP,SLNS,ARGUM,ARGUS,ARGDTM,ARGDTS
      COMMON/BLKD/XLAG,0,OMEGAM,DELMN,CMEGAS,DELSUN,SS,XID,A,E,XI,XNODE,
      1 TZERO,XIMODN,XISUN,TMS,XNDM,XNDS,F,XMEANM,XMEANS,XMCDTM,XMCDTS,
      2 UMGDOT,MEXP
      DO 10 LM=1,2
      YLM=LM
      DO 10 LP=1,3
      YLP=LP - 1
      DO 10 LQ=1,3
      YLQ=LQ - 2
      ARGDTM(LM,LP,LQ)=(2.0D0 - 2.0D0*YLP)*XNDM + YLQ*XMCDTM - YLM*Q
      1 + YLM*CMGDOT
      ARGDTS(LM,LP,LQ)=(2.0D0 - 2.0D0*YLP)*XNDS + YLQ*XMCDTS - YLM*Q
ISN 0014      10 CONTINUE
ISN 0015      RETURN
ISN 0016      END
ISN 0017

```



```

ISN 0002      SUBROUTINE ARGLEST(TT)
C
C      THIS SUBROUTINE FINDS THE SINE AND COSINE OF (L - 2*PI)*(ARGUMENT OF
C      PERIGEE*MEAN ANOMALY) + Q*(MEAN ANOMALY) + M*(NODE OF DISTURBING BODY) -
C      M*(NODE OF SATELLITE) FOR USE IN SUBROUTINE DATA.
C
ISN 0003      IMPLICIT REAL*8 (A-H,C-Z)
ISN 0004      DIMENSION CSM(2,3,3),SNM(2,3,3),CSS(2,3,3),SNS(2,3,3)
ISN 0005      COMMON/BLK1/XLAG,Q,OMEGAM,DELMN,CMEGAS,DELSUN,SS,X10,A,E,XI,XNODE,
1 TZERO,XIMODN,XISUN,TMS,XNDM,XNDS,F,XMEANM,XMEANS,XMDCM,XMDCST,
2 OMGDOT,MEXP
ISN 0006      COMMON/BLK2/CEM,FNV,CSS,SNS
ISN 0007      DO 10 LM=1,2
ISN 0008      YL4=LM
ISN 0009      DO 10 LP=1,3
ISN 0010      YLP=LP - 1
ISN 0011      DO 10 LO=1,3
ISN 0012      YLO=LO - 2
ISN 0013      AZ=(2.000 - 2.000*YLP)*(XNDM*(TT-TMS)+DELMN) + YLO*(XMDCM*(TT-
1 TMS)+XMEANM)+YLM*(OMGDOT*(TT-TMS)+OMEGAM) - YLM*(Q*(TT-TZERO) +
2 XNODE)
ISN 0014      CSM(LM,LP,LO)=DCOS(AZ)
ISN 0015      SNM(LM,LP,LO)=DSIN(AZ)
ISN 0016      A3=(2.000 - 2.000*YLP)*(XNDS*(TT-TMS)+DELSUN) + YLO*(XMDCST*(TT-
1 TMS)+XMEANS)+YLM*(OMGDOT*(TT-TMS)+OMEGAS) - YLM*(Q*(TT-TZERO) + XNODE)
ISN 0017      CSS(LM,LP,LO)=DCOS(A3)
ISN 0018      SNS(LM,LP,LO)=DSIN(A3)
ISN 0019      10 CONTINUE
ISN 0020      RETURN
ISN 0021      END

```

```

ISN 0002      SUBROUTINE BLM
C
C      THIS SUBROUTINE COMPUTES THE FACTORIAL PART OF THE TIP.
C
ISN 0003      IMPLICIT REAL*8 (A-H,C-Z)
ISN 0004      DIMENSION B1(2),XMOON(2,3,3),XSUN(2,3,3),YKM(2,3,3),YKS(2,3,3)
ISN 0005      COMMON/BLKB/B1,XK,CFNTM,CFNTS,SUM,XMOON,XSUN,YKM,YKS,XKP
ISN 0006      B1(1)=1.000/3.000
ISN 0007      B1(2)=1.000/12.000
ISN 0008      RETURN
ISN 0009      END

```

```

ISN 0002      SUBROUTINE CCEFF
C
C      THIS SUBROUTINE COMPUTES THE PART OF THE TIP WHICH HAS THE FORM
C      CONSTANT/(A**7/2).
C
ISN 0003      IMPLICIT REAL*8 (A-H,C-Z)
ISN 0004      DIMENSION B1(2),XMOON(2,3,3),XSUN(2,3,3),YKM(2,3,3),YKS(2,3,3)
ISN 0005      COMMON/BLKB/B1,XK,CFNTM,CFNTS,SUM,XMOON,XSUN,YKM,YKS,XKP
ISN 0006      COMMON/BLK1/XLAG,Q,OMEGAM,DELMN,CMEGAS,DELSUN,SS,X10,A,E,XI,XNODE,
1 TZERO,XIMODN,XISUN,TMS,XNDM,XNDS,F,XMEANM,XMEANS,XMDCM,XMDCST,
2 OMGDOT,MEXP
ISN 0007      A2=DSORT(A)
ISN 0008      CFNTM=B1(2.223200/((A**3)*A2)
ISN 0009      CFNTS=372.971900/((A**3)*A2)
ISN 0010      RETURN
ISN 0011      END

```

```

ISN 0002      SUBROUTINE CORRES(TSTART,TEND,DT,MEXP)
C
C      THIS SUBROUTINE IS USED ONLY BY SUBROUTINE PLOTTER. IT PUTS IN THE VALUES
C      OF ARRAY NTRACK(I), WHICH DETERMINES WHETHER OR NOT AN EXPERIMENTAL DATA POINT
C      SHOULD BE PRINTED AT TIME T(I) (NTRACK(N)=THE NUMBER OF THE EXPERIMENTAL
C      DATA POINT IF YES, ZERO IF NO.)
C
ISN 0003      IMPLICIT REAL*8 (A-H,C-Z)
ISN 0004      DIMENSION TEXP(200),X1EXP(200),T(700),X1NCL(700),NTRACK(700)
ISN 0005      COMMON/BLK3/TEXP,X1EXP,T,X1NCL,NTRACK
ISN 0006      MT=(TEND-TSTART)/DT + 1.100
ISN 0007      DO 10 I=1,MT
ISN 0008      NTRACK(I)=0
ISN 0009      IF (MEXP.EQ.0) GO TO 12
ISN 0010      DO 11 I=1,MEXP
ISN 0011      N=(TEXP(I)-TSTART)/DT + 1.500
ISN 0012      IF (N.GT. 1) N=1
ISN 0013      IF (N.GT. MT) N=MT
ISN 0014      NTRACK(N)=I
ISN 0015      11 CONTINUE
ISN 0016      10 CONTINUE
ISN 0017      RETURN
ISN 0018      END

```

```

ISN 0002      SUBROUTINE DATA(MM,D)
C
C
C      THIS SUBROUTINE IS USED TO FEED IN DATA FOR USE IN THE MULTIPLE
C      REGRESSION ANALYSIS CARRIED OUT BY SUBROUTINE REGRES.
C
ISN 0003      IMPLICIT REAL*8(A-H,C-Z)
ISN 0004      REAL*8 B(MM)
ISN 0005      DIMENSION EPSLNM(2,3,3),EPSLNS(2,3,3),ARGUM(2,3,3),ARGUS(2,3,3),
1 ARGDTM(2,3,3),ARGDTS(2,3,3)
ISN 0006      DIMENSION B1(2),XMOON(2,3,3),XSUN(2,3,3),YKM(2,3,3),YKS(2,3,3)
ISN 0007      DIMENSION TEXP(200),XIEXP(200),T(700),XINCL(700),NTRACK(700)
ISN 0008      DIMENSION C(2,3),A1(2,3),E(2,3),GLPQM(3,3),GLPQS(3,3)
ISN 0009      DIMENSION CSM(2,3,3),SNM(2,3,3),CSS(2,3,3),SNS(2,3,3)
ISN 0010      COMMON/BLKA/EPSLNM,EPSLNS,ARGUM,ARGUS,ARGDTM,ARGDTS
ISN 0011      COMMON/BLKB/B1,XK,CFNTM,CFNTS,SUM,XMOON,XSUN,YKM,YKS,XKP
ISN 0012      COMMON/BLKC/TEXP,XIEXP,T,XINCL,NTRACK
ISN 0013      COMMON/BLKD/XLAG,0,CMEGAM,DELMN,CMEGAS,DELSUN,SS,X10,A,E,X1,XNDE,
1 TZERT,XIMCON,XISUN,TMS,XNDM,XNDS,F,XMEANM,XMEANS,XMDOCTM,XMDOCTS,
2 CMGDOT,MEXP
ISN 0014      COMMON/BLKF/CSM,SNM,CSS,SNS
ISN 0015      COMMON/BLKG/C,A1,B,GLPQM,GLPQS,INDEX
C INDEX IS USED TO KEEP TRACK OF TIME
ISN 0016      INDEX=INDEX + 1
ISN 0017      TT=TEXP(INDEX)
ISN 0018      CALL ARGST(TT)
C DO THE LUNAR TIDES. WE LUMP THE LUNIPOLAR TIDES WITH THE LUNAR TIDES.
ISN 0019      I=0
ISN 0020      DO 70 LM=1,2
ISN 0021      YLM=LM
ISN 0022      DO 70 LP=1,3
ISN 0023      DO 70 LQ=1,3
ISN 0024      I=I + 1
ISN 0025      D(I)=CFNTM*B1(LM)*C(LM,2)*A1(LM,LP)*GLPQM(LP,LQ)*YLM*CSM(LM,LP,LQ)
1/(ARGDTM(LM,LP,LQ)*SS)
ISN 0026      I=I + 1
ISN 0027      D(I)=CFNTM*B1(LM)*C(LM,2)*A1(LM,LP)*GLPQM(LP,LQ)*YLM*SNM(LM,LP,LQ)
1/(ARGDTM(LM,LP,LQ)*SS)
ISN 0028      70 CONTINUE
C DO THE SOLAR TIDES
ISN 0029      DO 71 LM=1,2
ISN 0030      YLM=LM
ISN 0031      DO 71 LP=1,3
ISN 0032      DO 71 LQ=1,3
ISN 0033      IF (LP,LQ,2 .AND. LQ,EQ,2) GO TO 71
ISN 0034      I=I + 1
ISN 0035      D(I)=CFNTS*B1(LM)*C(LM,2)*B(LM,LP)*GLPQS(LP,LQ)*YLM*CSS(LM,LP,LQ)/
1 (ARGDTS(LM,LP,LQ)*SS)
ISN 0036      I=I + 1
ISN 0037      D(I)=CFNTS*B1(LM)*C(LM,2)*B(LM,LP)*GLPQS(LP,LQ)*YLM*SNS(LM,LP,LQ)/
1 (ARGDTS(LM,LP,LQ)*SS)
ISN 0038      71 CONTINUE
C PUT IN OBSERVED INCLINATION
ISN 0039      I=I + 1
ISN 0040      D(I)=XIEXP(INDEX)
ISN 0041      RETURN
ISN 0042      END
ISN 0043
ISN 0002      SUBROUTINE ECCFUN
C
C
C      THIS SUBROUTINE COMPUTES THE ECCENTRICITY FUNCTIONS FOR THE MOON AND SUN.
C
ISN 0003      IMPLICIT REAL*8(A-H,C-Z)
ISN 0004      DIMENSION C(2,3),A1(2,3),E(2,3),GLPQM(3,3),GLPQS(3,3)
ISN 0005      COMMON/BLKG/C,A1,B,GLPQM,GLPQS,INDEX
ISN 0006      EMCON=0.054900
ISN 0007      GLPQM(1,1)=(-0.500)*EMCON
ISN 0008      GLPQM(1,2)=1.000
ISN 0009      GLPQM(1,3)=(3.500)*EMCON
ISN 0010      GLPQM(2,1)=(1.500)*EMCON
ISN 0011      GLPQM(2,2)=1.000
ISN 0012      GLPQM(2,3)=(1.500)*EMCON
ISN 0013      GLPQM(3,1)=(3.500)*EMCON
ISN 0014      GLPQM(3,2)=1.000
ISN 0015      GLPQM(3,3)=(-0.500)*EMCON
ISN 0016      ESUN=C.016700
ISN 0017      GLPQS(1,1)=(-0.500)*ESUN
ISN 0018      GLPQS(1,2)=1.000
ISN 0019      GLPQS(1,3)=(3.500)*ESUN
ISN 0020      GLPQS(2,1)=(1.500)*ESUN
ISN 0021      GLPQS(2,2)=1.000
ISN 0022      GLPQS(2,3)=(1.500)*ESUN
ISN 0023      GLPQS(3,1)=(3.500)*ESUN
ISN 0024      GLPQS(3,2)=1.000
ISN 0025      GLPQS(3,3)=(-0.500)*ESUN
ISN 0026      RETURN
ISN 0027      END

```



```

15N 0002      SUBROUTINE INCL(XI,F)
      C
      C
      C      THIS SUBROUTINE COMPUTES THE SECOND DEGREE INCLINATION FUNCTIONS.
      C
15N 0003      IMPLICIT REAL*8(A-H,C-Z)
15N 0004      DIMENSION F(2,3)
15N 0005      S=PI*IN(XI)
15N 0006      C=DCOS(XI)
15N 0007      S2=C**2
15N 0008      C2=C**2
15N 0009      F(1,1)=(3.000/4.000)*S*(1.000 + C)
15N 0010      F(1,2)=(-3.000/2.000)*S*C
15N 0011      F(1,3)=(-3.000/4.000)*S*(1.000 - C)
15N 0012      F(2,1)=(3.000/4.000)*C*(1.000 + C)**2)
15N 0013      F(2,2)=(3.000/2.000)*S2
15N 0014      F(2,3)=(3.000/4.000)*C*(1.000 - C)**2)
15N 0015      RETURN
15N 0016      END

15N 0002      SUBROUTINE LAG1
      C
      C
      C      THIS SUBROUTINE READS IN THE SOLID EARTH LAG ANGLE XLAG AND CONVERTS IT
      C      FROM DEGREES TO RADIANS.
      C
15N 0003      IMPLICIT REAL*8(A-H,C-Z)
15N 0004      COMMON/BLKD/XLAG,0,OMEGAM,DELMN,CMEGAS,DELSUN,SS,XI0,A,E,XI,XNODE,
15N 0005      1 TZERC,XIMODN,XISUN,TMS,XNDM,XNDS,F,XMEANM,XMEANS,XMCDTM,XMCDTS,
15N 0006      2 UMGDOT,MEXP
15N 0007      1 READ (5,1) XLAG
15N 0008      1 FORMAT (BF10.5)
15N 0009      1 WRITE (6,2) XLAG
15N 0010      2 FORMAT (//////,23X,'SOLID EARTH LAG ANGLE=',F8.3,1X,'DEGREES')
15N 0011      XLAG=XLAG*F
15N 0012      RETURN
15N 0013      END

15N 0002      SUBROUTINE LAG2
      C
      C
      C      THIS SUBROUTINE SETS THE FREQUENCY DEPENDENT TIDAL LAG ANGLES INITIALLY
      C      EQUAL TO ZERO.
      C
15N 0003      IMPLICIT REAL*8(A-H,C-Z)
15N 0004      DIMENSION EPSLNM(2,3,3),EPSLNS(2,3,3),ARGUM(2,3,3),ARGUS(2,3,3),
15N 0005      1 ARGDTM(2,3,3),ARGDTS(2,3,3)
15N 0006      COMMON/BLKA/EPNLNM,EPNLNS,ARGUM,ARGUS,ARGDTM,ARGDTS
15N 0007      COMMON/BLKD/XLAG,0,OMEGAM,DELMN,CMEGAS,DELSUN,SS,XI,XNODE,
15N 0008      1 TZERC,XIMODN,XISUN,TMS,XNDM,XNDS,F,XMEANM,XMEANS,XMCDTM,XMCDTS,
15N 0009      2 UMGDOT,MEXP
15N 0010      DO 10 LM=1,2
15N 0011      DO 10 LP=1,3
15N 0012      DO 10 LQ=1,3
15N 0013      EPSLNM(LM,LP,LQ)=0.000
15N 0014      EPSLNS(LM,LP,LQ)=0.000
15N 0015      10 CONTINUE
15N 0016      RETURN
15N 0017      END

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ISN 0002      SUBROUTINE LASDTA
C
C
C THIS SUBROUTINE READS IN, THEN PRINTS OUT, THE OBSERVED TIP. X(IEXP(J)) IS
C THE OBSERVED TIP (IN ARCSECONDS) AT TIME TEXP(J) (IN DAYS).
C TDAY IS A CORRECTION FACTOR, WHICH MAKES TEXP(J) START AT THE BEGINNING OF
C THE YEAR (JAN 1 AT 0 HRS UT = 1). TDAY IS NECESSARY SINCE OFTENTIMES THE
C TIME OF EACH DATA POINT IS GIVEN IN DAYS AFTER THE FIRST OBSERVATION (I.E.
C TEXP(1)=0.0 ).
C
C
ISN 0003      IMPLICIT REAL*8(A-H,C-Z)
ISN 0004      DIMENSION TEXP(200),XIEXP(200),T(700),XINCL(700),NTRACK(700)
ISN 0005      COMMON/BLKC/TEXP,XIEXP,T,XINCL,NTRACK
ISN 0006      COMMON/BLKD/ XLAG,0,UMEGAM,DELMN,EMEGAS,DELSUN,SS,XIO,A,E,XI,XNCDE,
1 TZERO,XIMOOD,XISUN,TMS,XNDM,XNDS,F,XMEANM,XMEANS,XMDOTM,XMDOTS,
2 UMGDOT,MEXP
ISN 0007      READ (5,33) MEXP,TDAY
ISN 0008      33 FORMAT (15,F10.5)
ISN 0009      DO 32 J=1,MEXP
ISN 0010      READ (5,34) XIEXP(J),TEXP(J)
ISN 0011      TEXP(J)=TEXP(J) + TDAY
ISN 0012      32 CONTINUE
ISN 0013      34 FORMAT (2D14.6)
ISN 0014      WRITE (6,2)
ISN 0015      2 FORMAT (1H1)
ISN 0016      WRITE (6,3)
ISN 0017      3 FORMAT (//////,50X,'SATELLITE TRACKING DATA',/////)
ISN 0018      WRITE (6,15) MEXP,TDAY
ISN 0019      15 FORMAT (41X, '(1.15.' DATA POINTS, TDAY='F8.4,' DAYS)',/////)
ISN 0020      WRITE (6,4)
ISN 0021      4 FORMAT (48X, 'TIME',13X, 'INCLINATION',/)
ISN 0022      WRITE (6,5)
ISN 0023      5 FORMAT (7X, '(DAYS)',14X, '(ARCSEC)')
ISN 0024      WRITE (6,6)
ISN 0025      6 FORMAT (38X, '(JAN 1, 0 HRS UT = 1)',//)
ISN 0026      DO 10 J=1,MEXP
ISN 0027      10 WRITE (6,11) J,TEXP(J),XIEXP(J)
ISN 0028      11 FORMAT (35X,15,5X,F10.4,10X,F10.4)
ISN 0029      RETURN
ISN 0030      END

```

```

ISN 0002      SUBROUTINE LOVE
C
C
C THIS SUBROUTINE READS IN THE SECOND DEGREE LOVE NUMBER AND LOAD
C DEFORMATION COEFFICIENT OF THE SOLID EARTH.
C
C
ISN 0003      IMPLICIT REAL*8(A-H,C-Z)
ISN 0004      DIMENSION B1(2),XMOON(2,3,3),XSUN(2,3,3),YKM(2,3,3),YKS(2,3,3)
ISN 0005      COMMON/BLKB/B1,XK,CFNTM,CFNTS,SUM,XMOON,XSUN,YKM,YKS,XKP
ISN 0006      READ (5,1) XK,XKP
ISN 0007      1 FORMAT (3F10.5)
ISN 0008      WRITE (6,2) XK,XKP
ISN 0009      2 FORMAT (////////,23X,'SOLID EARTH LOVE NUMBER='F8.4,10X,'LOAD DEF
1 ORMATION COEFFICIENT='F8.4)
ISN 0010      RETURN
ISN 0011      END

```



```

ISN 0002      SUBROUTINE LCVNUM(MT)
C
C
C   THIS SUBROUTINE TAKES THE COEFFICIENTS AND THEIR ERRORS FOUND IN
C   SUBROUTINE REGRES AND SOLVES FOR THE FREQUENCY DEPENDENT LOVE NUMBERS, TIDAL
C   LAG ANGLES, AND THEIR ERRORS. IT ALSO FINDS THE OCEAN TIDE PARAMETERS.
C   ASSUMING THE SOLID EARTH LOVE NUMBER AND LAG ANGLE ARE KNOWN.
C   ****ALL TIDES ARE ASSUMED TO BE 2ND DEGREE ONLY. HENCE ALL OTHER TIDES ARE
C   ABSORBED INTO THE 2ND DEGREE TIDES.
C
C
ISN 0003      IMPLICIT REAL*8(A-H,O-Z)
ISN 0004      REAL*4 VV(70),VE(70),ANS(10)
ISN 0005      DIMENSION EPSLNM(2,3,3),EPSLNS(2,3,3),ARGUM(2,3,3),ARGUS(2,3,3),
C   ARGDTM(2,3,3),ARGDTS(2,3,3)
ISN 0006      DIMENSION B1(2),XMOON(2,3,3),XSUN(2,3,2),YKM(2,3,3),YKS(2,3,3)
ISN 0007      DIMENSION TXP(200),XIEXP(200),T(700),XINCL(700),NTRACK(700)
ISN 0008      DIMENSION C(2,3),A1(2,3),H(2,3),GLPQM(3,3),GLPQS(3,3)
ISN 0009      DIMENSION NN(70),ISAVE(70)
ISN 0010      DIMENSION TIDE(2,3,3)
ISN 0011      DIMENSION SAT(14)
ISN 0012      COMMON/BLKA/EPSLNM,EPSLNS,ARGUM,ARGUS,ARGDTM,ARGDTS
ISN 0013      COMMON/BLKB/B1,XK,CENTM,CENT3,SUM,XMOON,XSUN,YKM,YKS,XKP
ISN 0014      COMMON/BLKC/TXP,XIEXP,T,XINCL,NTRACK
ISN 0015      COMMON/BLKD/XLAG,0,CMEGAM,DELMN,CMEGAS,DELSUN,SS,X10,A,E,XI,XNCOE,
C   1 TZERO,XIMDON,XISUN,T4S,XNDM,XNDE,F,XMEANM,XMEANS,XMDCTM,XMDOTS,
C   2 XMDOT,XEXP
ISN 0016      COMMON/BLKG/C,A1,B,GLPQM,GLPQS,INDEX
ISN 0017      COMMON/BLKH/VV,VE,ANS,ISAVE,M,K
ISN 0018      COMMON/BLKI/SAT
ISN 0019      DATA BLANK/4H /
ISN 0020      DATA TM112,TM122,TM212,TM222/4H01 ,4HK1 ,4HM2 ,4HK2 /
ISN 0021      DATA TS112,TS122,TS212,TS222/4H01 ,4HK1S ,4HM2 ,4HK2S /
ISN 0022      PI=3.1415926535900
ISN 0023      YLAG=XLAG/F
C   SET THE ADDITIVE CONSTANT IN THE TIP EQUAL TO X10
ISN 0024      X10=ANS(1)
ISN 0025      WRITE (6,19)
ISN 0026      19 FORMAT (1H1)
C   PRINT OUT THE HEADINGS
ISN 0027      WRITE (6,31)
ISN 0028      31 FORMAT (25X,*****FREQUENCY DEPENDENT LOVE NUMBERS*****,10X,
C   1 *****OCEAN TIDE PARAMETERS*****)
ISN 0029      WRITE (6,32)
ISN 0030      32 FORMAT (30X,*(ASSUMING 2ND DEGREE TIDES ONLY)*17X,*(ASSUMING 2ND
C   1 DEGREE TIDES*)
ISN 0031      WRITE (6,33)
ISN 0032      33 FORMAT (79X,*(ONLY AND SOLID EARTH LOVE*)
ISN 0033      WRITE (6,34) XK
ISN 0034      34 FORMAT (79X,*(NUMBER K2=*,F5.3,1X,*(AND SOLID*)
ISN 0035      WRITE (6,35) YLAG
ISN 0036      35 FORMAT (79X,*(EARTH TIDAL LAG=*,F5.3,1X,*(DEG)*,/)
ISN 0037      WRITE (6,40)
ISN 0038      40 FORMAT (1X,*(L M P Q TIDE DIS.BODY LOVE NUMBER STD. ERROR LAG
C   1 ANGLE STD. ERROR C STD. ERROR PHASE STD. ERROR
C   2 ))
ISN 0039      WRITE (6,39)
ISN 0040      39 FORMAT (51X,*(DEGREES)*,3X,*(DEGREES)*,7X,*(CM)*,3X,*(CM)*,3X,
C   1 *(DEGREES)*,4X,*(DEGREES)*,/)
C   SET NN(J)=0 FOR TIDES NOT SOLVED FOR BY THE MULTIPLE REGRESSION IN
C   SUBROUTINE REGRES, AND NN(J)=1 FOR THOSE WHICH ARE SOLVED FOR
ISN 0041      MV=M - 1
ISN 0042      DO 20 J=1,MV
ISN 0043      20 NN(J)=0
ISN 0044      DO 21 J=1,K
ISN 0045      21 IS=ISAVE(J)
ISN 0046      21 NN(IS)=1
C
C   ****LUNAR AND LUNISOLAR TIDES****
C
C   PUT NAME OF TIDAL CONSTITUENT IN ARRAY TIDE
ISN 0047      DO 89 LM=1,2
ISN 0048      DO 89 LP=1,3
ISN 0049      DO 89 LC=1,3
ISN 0050      89 TIDE(LM,LP,LC)=BLANK
ISN 0051      TIDE(1,1,2)=TM112
ISN 0052      TIDE(1,2,2)=TM122
ISN 0053      TIDE(2,1,2)=TM212

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ISN 0054      TIDE(2,2,2)=TM22
ISN 0055      LLL=2
ISN 0056      IE=0
ISN 0057      DO 60 LM=1,2
ISN 0058      YLM=LM
ISN 0059      DO 50 LP=1,3
ISN 0060      YLP=LP - 1
ISN 0061      LPP=LP - 1
ISN 0062      DO 60 LQ=1,3
ISN 0063      LQQ=LQ - 2
ISN 0064      I=I + 1
ISN 0065      U1=VV(I)
ISN 0066      E1=VE(I)
ISN 0067      IF=1
ISN 0068      IF=1 + 1
ISN 0069      U2=-VV(I)
ISN 0070      E2=VE(I)
ISN 0071      C IF ONLY THE EFFECTIVE LOVE NUMBER IS SOLVED FOR, PUT THE EFFECTIVE LAG ANGLE
ISN 0072      C AND ITS ERROR EQUAL TO ZERO
ISN 0073      IF (NN(1) .EQ. 0) U2=0.000
ISN 0074      IF (NN(1) .EQ. 0) E2=0.000
ISN 0075      C IF THIS TIDE WAS NOT SOLVED FOR, GO TO 62
ISN 0076      IF (NN(13) .EQ. 0 .AND. NN(1) .EQ. 0) GO TO 62
ISN 0077      U3=U1**2 + U2**2
ISN 0078      C FIND THE EFFECTIVE FREQUENCY-DEPENDENT LOVE NUMBER
ISN 0079      YKM(LM,LP,LQ)=DSORT(U3)
ISN 0080      U4=U2/U1
ISN 0081      C FIND THE EFFECTIVE FREQUENCY-DEPENDENT LAG ANGLE, MAKING SURE WE KNOW WHICH
ISN 0082      C QUADRANT IT IS IN
ISN 0083      EPSLNM(LM,LP,LQ)=ATAN(U4)
ISN 0084      IF (U4) 22,25,23
ISN 0085      28 CONTINUE
ISN 0086      IF (U1) 29,27,27
ISN 0087      24 EPSLNM(LM,LP,LQ)=PI
ISN 0088      GO TO 27
ISN 0089      22 CONTINUE
ISN 0090      IF (U2) 25,24,24
ISN 0091      24 EPSLNM(LM,LP,LQ)=EPSLNM(LM,LP,LQ) + PI
ISN 0092      CONTINUE
ISN 0093      GO TO 27
ISN 0094      23 CONTINUE
ISN 0095      IF (U2) 25,27,27
ISN 0096      26 EPSLNM(LM,LP,LQ)=EPSLNM(LM,LP,LQ) + PI
ISN 0097      27 CONTINUE
ISN 0098      C EP IS THE EFFECTIVE TIDAL LAG ANGLE IN DEGREES
ISN 0099      EP=EPSLNM(LM,LP,LQ)/F
ISN 0100      SIGSOR=((E1**2)*(U1**2) + (E2**2)*(U2**2))/U3
ISN 0101      C SIGLOV IS THE STD. ERROR OF YKM(LM,LP,LQ)
ISN 0102      SIGLOV=DSORT(SIGSOR)
ISN 0103      SIGSOR=((E2**2)*(U1**2) + (E1**2)*(U2**2))/(U3**2)
ISN 0104      C SIGLAG IS THE STD. ERROR OF EPSLNM(LM,LP,LQ) IN DEGREES
ISN 0105      SIGLAG=DSORT(SIGSOR)/F
ISN 0106      C
ISN 0107      C FACTOR TAKES CARE OF THE AMPLITUDE OF THE LUNISOLAR TIDES. REMEMBER, THE
ISN 0108      C LUNISOLAR TIDES ARE LUMPED WITH THE LUNAR TIDES IN SUBROUTINE DATA. HENCE A
ISN 0109      C CORRECTION MUST BE APPLIED TO THE LUNAR TIDES WHEN THE LUNISOLAR CASE COMES
ISN 0110      C UP. SYMBOLICALLY, FACTOR=(1 + SUN/MOON)*MOON = MOON + SUN, AS IT SHOULD FOR
ISN 0111      C THE LUNISOLAR TIDES.
ISN 0112      C
ISN 0113      FACTOR=1.000 + (CFNTS*B(LM,2))/(CFNTM*A1(LM,LP))
ISN 0114      C
ISN 0115      C DO THE OCEAN TIDES
ISN 0116      C
ISN 0117      C YM*XLAGE IS THE LAG ANGLE OF THE SOLID EARTH CONVERTED TO FREQUENCY-DEPENDENT
ISN 0118      C FORM
ISN 0119      YM=LM
ISN 0120      CXLAGE=DCOS(YM*XLAGE)
ISN 0121      SXLAG=USIN(YM*XLAGE)
ISN 0122      C SUBTRACT OUT THE SOLID EARTH TIDE
ISN 0123      SEA1=U1 - XK*CXLAGE
ISN 0124      IF (LP .EQ. 2 .AND. LQ .EQ. 2) SEA1=U1 - FACTOR*XK*CXLAGE
ISN 0125      SEA2=U2 - XK*SXLAGE
ISN 0126      IF (LP .EQ. 2 .AND. LQ .EQ. 2) SEA2=U2 - FACTOR*XK*SXLAGE
ISN 0127      SEA3=SEA1**2 + SEA2**2
ISN 0128      SEA3=DSORT(SEA3)
ISN 0129      C FIND COCLAN, THE OCEAN AMPLITUDE
ISN 0130      COCLAN=(J20.0375500)*SEA3*B1(LM)*A1(LM,LP)/(1.000 + XKP)
ISN 0131      SIGSOR=((E1**2)*(SEA1**2) + (E2**2)*(SEA2**2))/SEA3
ISN 0132      SIG=DSORT(SIGSOR)
ISN 0133      C SIGC IS THE STD. ERROR OF COCLAN

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ISN 0178      TIDE(2,2,2)=TS222
ISN 0179      DO 65 LM=1,2
ISN 0180      YLM=LM
ISN 0181      DO 65 LP=1,3
ISN 0182      YLP=LP - 1
ISN 0183      LPP=LP - 1
ISN 0184      DO 65 LQ=1,3
ISN 0185      LQQ=LQ - 2
ISN 0186      IF (LP .EQ. 2 .AND. LQ .EQ. 2) GO TO 56
ISN 0188      I=I + 1
ISN 0189      U1=VV(I)
ISN 0190      E1=VE(I)
ISN 0191      I3=I
ISN 0192      I=I + 1
ISN 0193      U2=-VV(I)
ISN 0194      E2=VE(I)
ISN 0195      C IF ONLY THE EFFECTIVE LOVE NUMBER IS SOLVED FOR, PUT THE EFFECTIVE LAG ANGLE
ISN 0197      C AND ITS ERROR EQUAL TO ZERO
ISN 0197      IF (NN(I) .EQ. 0) U2=0.000
ISN 0197      IF (NN(I) .EQ. 0) E2=0.000
ISN 0199      C IF THIS TIDE WAS NOT SOLVED FOR, GO TO 66
ISN 0201      IF (NN(I3) .EQ. 0 .AND. NN(I) .EQ. 0) GO TO 66
ISN 0201      U3=U1**2 + U2**2
ISN 0202      C FIND THE EFFECTIVE FREQUENCY-DEPENDENT LOVE NUMBER
ISN 0203      YKS(LM,LP,LQ)=DSQRT(U3)
ISN 0203      U4=U2/L1
ISN 0203      C FIND THE EFFECTIVE FREQUENCY-DEPENDENT LAG ANGLE, MAKING SURE WE KNOW WHICH
ISN 0203      C QUADRANT IT IS IN
ISN 0204      EPSLNS(LM,LP,LQ)=DATAN(U4)
ISN 0205      IF (U4) 32,36,33
ISN 0206      33 CONTINUE
ISN 0207      IF (U1) 41,37,37
ISN 0208      41 EPSLNS(LM,LP,LQ)=PI
ISN 0209      GO TO 37
ISN 0210      32 CONTINUE
ISN 0211      IF (U2) 35,34,34
ISN 0212      34 EPSLNS(LM,LP,LQ)=EPSLNS(LM,LP,LQ) + PI
ISN 0213      35 CONTINUE
ISN 0214      GO TO 37
ISN 0215      33 CONTINUE
ISN 0216      IF (U2) 36,37,37
ISN 0217      36 EPSLNS(LM,LP,LQ)=EPSLNS(LM,LP,LQ) + PI
ISN 0218      37 CONTINUE
ISN 0219      C EP IS THE EFFECTIVE TIDAL LAG ANGLE IN DEGREES
ISN 0220      EP=EPSLNS(LM,LP,LQ)/F
ISN 0220      SIGLOV=((E1**2)*(U1**2) + (E2**2)*(U2**2))/U3
ISN 0221      C SIGLOV IS THE STD. ERROR OF YKS(LM,LP,LQ)
ISN 0222      SIGLOV=DSQRT(SIGLOV)
ISN 0222      SIGSQF=((E2**2)*(U1**2) + (E1**2)*(U2**2))/(U3**2)
ISN 0223      C SIGLAG IS THE STD. ERROR OF EPSLNS(LM,LP,LQ) IN DEGREES
ISN 0223      SIGLAG=DSQRT(SIGSQF)/F
ISN 0223      C
ISN 0223      C DO THE OCEAN TIDES
ISN 0223      C
ISN 0224      YM=LM
ISN 0224      C YM*XLAG IS THE LAG ANGLE OF THE SOLID EARTH CONVERTED TO FREQUENCY-DEPENDENT
ISN 0224      C FORM
ISN 0225      CXLAG=DCOS(YM*XLAG)
ISN 0226      SXLAG=DSIN(YM*XLAG)
ISN 0227      C SUBTRACT OUT THE SOLID EARTH TIDE
ISN 0228      SEA1=U1 - XK*CXLAG
ISN 0229      SEA2=U2 - XK*SXLAG
ISN 0230      SEA3=SEA1**2 + SEA2**2
ISN 0230      SEA5=DSQRT(SEA3)
ISN 0231      C FIND COCEAN, THE OCEAN AMPLITUDE
ISN 0232      COCEAN=((1+6.77500)*SEA5**31(LM)*B(LM,LP)/(1.000 + XKF)
ISN 0233      SIGSQR=((F1**2)*(SEA1**2) + (E2**2)*(SEA2**2))/SEA3
ISN 0233      SIG=DSQRT(SIGSQR)
ISN 0234      C SIGC IS THE STD. ERROR OF COCEAN
ISN 0235      SIGC=((1+6.77500)*SIG*B1(LM)*DABS(B(LM,LP))/(1.000 + XKF)
ISN 0235      SIGSQF=((E2**2)*(SEA1**2) + (E1**2)*(SEA2**2))/(SEA3**2)
ISN 0236      C SIGPHS IS THE STD. ERROR OF THE PHASE ANGLE IN DEGREES
ISN 0237      SIGPHS=DSQRT(SIGSQF)/F
ISN 0237      U44=SEA2/SEA1
ISN 0237      C FIND THE PHASE ANGLE OF THE OCEAN TIDE, MAKING SURE WE KNOW WHICH QUADRANT
ISN 0237      C IT IS IN
ISN 0238      PHASE=DATAN(U44)
ISN 0239      IF (U44) 52,55,53
ISN 0240      53 CONTINUE
ISN 0241      IF (SEA1) 59,57,57

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ISN 0309      DO 4 J=1,MEXP
ISN 0310      TT=TEXP(J)
ISN 0311      CALL ARG(TT)
ISN 0312      SUMEC=0
ISN 0313      DO 3 L=1,L
ISN 0314      YLM=LM
ISN 0315      DO 3 LP=1,3
ISN 0316      YLP=LP - 1
ISN 0317      DO 3 LQ=1,3
ISN 0318      XMDCN(LM,LP,LQ)=YKX(LM,LP,LQ)*CENTM*B1(LM)*C(LM,2)*A1(LM,LP)*GLPQM
ISN 0319      XSUM(LM,LP,LQ)=YKX(LM,LP,LQ)/(ARGCTM(LM,LP,LQ)*SS)
ISN 0320      XSUM(LM,LP,LQ)=YKX(LM,LP,LQ)*CENTS*B1(LM)*C(LM,2)*R(LM,LP)*GLPQS(L
ISN 0321      XSUM(LM,LP,LQ)=YKX(LM,LP,LQ)/(ARGDTS(LM,LP,LQ)*SS)
ISN 0322      3 CONTINUE
ISN 0323      SUMESUM = XIO
ISN 0324      RESI=XILXP(J) - SUM
ISN 0325      SUMSIGRESI=XI2 + SUMSIG
ISN 0326      4 WRITE (0,13) J,TEXP(J),RESI
ISN 0327      CONTINUE
ISN 0328      XN=MEXP - 1
ISN 0329      SIGMA=SQRT(SUMSIG/XN)
ISN 0330      100 FORMAT (//////.10X,'SIGMA = SQRT((SUM OF SQUARES)/(MEXP-1)) = ',
ISN 0331      C PLT OUT XINCL(L) VS. T(L), RESIDUALS ON COMPUTER PAPER
ISN 0332      CALL PLOT(MT,MEXP)
ISN 0333      RETURN
ISN 0334      END

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ISN 0002      SUBROUTINE PLOTTER(MT,MEXP)
C
C
C      THIS SUBROUTINE PLOTS A CONTINUOUS CURVE PLUS EXPERIMENTAL DATA POINTS
C      VS. TIME T(L). IT ALSO PLOTS THE RESIDUALS VS. TIME T(L).
C      TIME INCREASES DOWN THE PAGE AND THE WIDTH OF THE PLOT IS 101 SPACES ACROSS.
C      THERE ARE MT POINTS IN THE CURVE, WHICH IS STORED IN ARRAY XINCL(L), AND
C      MEXP EXPERIMENTAL DATA POINTS, STORED IN ARRAY XIEXP(J). THE POINTS OF THE
C      CURVE ARE PRINTED AS D'S AND THE DATA POINTS AS X'S.
C
C
ISN 0003      IMPLICIT REAL*4(A-H,C-Z)
ISN 0004      DIMENSION RESID(200)
ISN 0005      DIMENSION BINE(101)
ISN 0006      DIMENSION TEXP(200),XIEXP(200),T(700),XINCL(700),NTRACK(700)
ISN 0007      COMMON/HLK/TEXP,XIEXP,T,XINCL,NTRACK
ISN 0008      DATA DE7,EK5,HLANK/1PD,1HX,1H /
C DETERMINE THE WIDTH OF THE PLOT, BY FINDING THE MAXIMUM AND MINIMUM POINTS OF
C THE CURVE AND THE DATA POINTS
ISN 0009      XMAX1=XINCL(1)
ISN 0010      XMIN1=XINCL(1)
ISN 0011      DO 30 I=2,MT
ISN 0012      P=XINCL(I)
ISN 0013      IF (XMAX1 - P) 22,21,21
ISN 0014      22 XMAX1=P
ISN 0015      GO TO 30
ISN 0016      21 CONTINUE
ISN 0017      IF (P - XMIN1) 24,30,30
ISN 0018      24 XMIN1=P
ISN 0019      30 CONTINUE
ISN 0020      IF (MEXP .EQ. 0) GO TO 4
ISN 0021      GO TO 5
ISN 0022      XMAX=XMAX1
ISN 0023      XMIN=XMIN1
ISN 0024      GO TO 50
ISN 0025      5 CONTINUE
ISN 0026      XMAX2=XIEXP(1)
ISN 0027      XMIN2=XIEXP(1)
ISN 0028      DO 40 J=2,MEXP
ISN 0029      P=XIEXP(J)
ISN 0030      IF (XMAX2 - P) 42,41,41
ISN 0031      42 XMAX2=P
ISN 0032      GO TO 40
ISN 0033      41 CONTINUE
ISN 0034      IF (P - XMIN2) 44,40,40
ISN 0035      44 XMIN2=P
ISN 0036      40 CONTINUE
ISN 0037      IF (XMAX2 - XMAX1) 45,46,46
ISN 0038      46 XMAX=XMAX2
ISN 0039      GO TO 47
ISN 0040      45 XMAX=XMAX1
ISN 0041      47 CONTINUE
ISN 0042      IF (XMIN2 - XMIN1) 48,49,49
ISN 0043      48 XMIN=XMIN2
ISN 0044      GO TO 50
ISN 0045      49 XMIN=XMIN1
ISN 0046      50 CONTINUE
C COMPUTE FAC, SO THAT ALL OF THE POINTS FIT ON THE PAPER
ISN 0047      FAC=100.0007/(XMAX-XMIN)
ISN 0048      WRITE (6,3)
ISN 0049      3 FORMAT (1H1)
ISN 0050      SCALE=XMAX - XMIN
C WRITE THE LOWEST POINT, HIGHEST POINT, AND DISTANCE BETWEEN THEM
ISN 0051      WRITE (6,131) XMIN,XMAX,SCALE
C SET ARRAY BINE(J) INITIALLY EQUAL TO BLANK
ISN 0052      DO 20 J=1,101
ISN 0053      BINE(J)=BLANK
ISN 0054      DO 29 L=1,MT
ISN 0055      J6=1
C PUT CURVE POINT IN BINE(JJ)
ISN 0056      JJ=(XINCL(L) - XMIN)*FAC + 1.51
ISN 0057      BINE(JJ)=DEE
C SEE IF AN EXPERIMENTAL DATA POINT SHOULD BE PLOTTED, BY CHECKING THE VALUE OF
C NTRACK(L)
ISN 0058      IF (NTRACK(L) .EQ. 0) GO TO 50
ISN 0059      NN=NTRACK(L)
C PUT EXPERIMENTAL DATA POINT IN BINE(J4)
ISN 0060      J4=(XIEXP(NN) - XMIN)*FAC + 1.51

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ISN 0063      BINE(J4)=EKS
ISN 0064      60 CONTINUE
C PRINT THE NUMBER OF THE CURVE POINT, BINE, AND THE NUMBER OF THE CURVE POINT
ISN 0065      WRITE (6,25) L,(BINE(J1), J1=1,101),L
ISN 0066      25 FORMAT (3X,15,2X,101A1,1X,15)
C PUT ARRAY BINE(J) BACK TO BLANK
ISN 0067      BINE(JJ)=BLANK
ISN 0068      BINE(J4)=BLANK
ISN 0069      29 CONTINUE
ISN 0070      IF (MEXP.EQ. 0) GO TO 130
C PLOT RESIDUALS VS. TIME
ISN 0072      DO 132 J=1,MEXP
ISN 0073      RESID(J)=0.0
ISN 0074      132 CONTINUE
ISN 0075      DO 101 L=1,MT
ISN 0076      IF (NTRACK(L).EQ. 0) GO TO 101
ISN 0077      NN=NTRACK(L)
ISN 0078      RESID(NN)=XIEXP(NN) - XINCL(L)
ISN 0080      101 CONTINUE
ISN 0081      XMAX2=RESID(1)
ISN 0082      XMIN2=RESID(1)
ISN 0083      DO 140 J=2,MEXP
ISN 0084      P=RESID(J)
ISN 0085      IF (XMAX2 - P) 142,141,141
ISN 0086      142 XMAX2=P
ISN 0087      GO TO 140
ISN 0088      141 CONTINUE
ISN 0089      IF (P - XMIN2) 144,140,140
ISN 0090      144 XMIN2=P
ISN 0091      140 CONTINUE
ISN 0092      SCALE=XMAX2 - XMIN2
ISN 0093      WRITE (6,3)
ISN 0094      WRITE (6,131) XMIN2,XMAX2,SCALE
ISN 0095      131 FORMAT (//////,10X,'MINIMUM=',F10.5,10X,'MAXIMUM=',F10.5,10X,
1 'SCALE=',F10.5,//////)
ISN 0096      FAC=100.000/(XMAX2 - XMIN2)
ISN 0097      DO 129 J=1,101
ISN 0098      BINE(J)=BLANK
ISN 0099      DO 129 L=1,MT
ISN 0100      J4=1
ISN 0101      JJ=(-XMIN2)*FAC + 1.51
ISN 0102      BINE(JJ)=DEE
ISN 0103      IF (NTRACK(L).EQ. 0) GO TO 140
ISN 0104      NN=NTRACK(L)
ISN 0105      J4=(RESID(NN) - XMIN2)*FAC + 1.51
ISN 0106      BINE(J4)=EKS
ISN 0107      160 CONTINUE
ISN 0108      WRITE (6,25) L,(BINE(J1), J1=1,101),L
ISN 0109      BINE(JJ)=BLANK
ISN 0110      BINE(J4)=BLANK
ISN 0111      129 CONTINUE
ISN 0112      130 CONTINUE
ISN 0113      RETURN
ISN 0114      END
ISN 0115

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ISN 0002      SUBROUTINE RCSAT
C
C
C THIS SUBROUTINE READS IN AND PRINTS OUT THE SATELLITE ELEMENTS AND NODE
C RATE. ALL INPUT IN DEGREES (OR DEGREES PER DAY) IS IMMEDIATELY CONVERTED TO
C RADIANS (OR RADIANS PER DAY) FOR USE IN THE PROGRAM.
C
C
ISN 0003      IMPLICIT REAL*4(A-H,O-Z)
ISN 0004      DIMENSION SAT(14)
ISN 0005      COMMON/BLKD/XLAG,0,CMEGAM,DELMN,CMEGAS,DELTUN,SS,X10,A,E,X1,XNODE,
1 TZERO,XIMODN,XISUN,TMS,XNDM,XNDS,F,XMEANM,XMEANS,XNDOTM,XMOOTS,
2 OMGDUT,MEXP
ISN 0006      COMMON/BLKI/SAT
ISN 0007      READ (5,7) (SAT(J), J=1,14)
ISN 0008      7 FORMAT (13A6,A2)
ISN 0009      WRITE (6,2)
ISN 0010      2 FORMAT (1H1)
ISN 0011      WRITE (6,8) (SAT(J), J=1,14)
ISN 0012      8 FORMAT (//////,10X,'SATELLITE',1X,13A6,A2)
ISN 0013      READ (5,1) A,E,Q1,X11,TZERO,XNODE1
ISN 0014      1 FORMAT (3F10.5)
ISN 0015      X1=X11*F
ISN 0016      Q=Q1*F
ISN 0017      XNODE=XNODE1*F
ISN 0018      WRITE (6,3)
ISN 0019      3 FORMAT (//////,50X,'SATELLITE DATA',//////)
ISN 0020      WRITE (6,4)
ISN 0021      4 FORMAT (24X,'A',14X,'E',10X,'INCLINATION',4X,'NODE RATE',4X,'TZERO
1',11X,'NODE',/)
ISN 0022      WRITE (6,2)
ISN 0023      5 FORMAT (23X,'(10**5 CM)',21X,'(DEGREES)',5X,'(DEG/DAY)',8X,'(DAYS)
1',4X,'(DEGREES)',/)
ISN 0024      WRITE (6,5) A,E,X11,Q1,TZERO,XNODE1
ISN 0025      6 FORMAT (20X,5(F10.4,5X))
ISN 0026      RETURN
ISN 0027      END

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15N 0002      SUBROUTINE READMS
C
C
C   THIS SUBROUTINE READS IN AND PRINTS OUT THE POSITION AND ANGULAR SPEEDS OF
C   THE MOON AND SUN. INPUT IN DEGREES (OR DEGREES PER DAY) IS IMMEDIATELY
C   CONVERTED TO RADIANS (OR RADIANS PER DAY) FOR USE IN THE PROGRAM.
C
15N 0003      IMPLICIT REAL*8(A-H,C-Z)
15N 0004      COMMON/BLKCD/ XLAG,Q,CMEGAM,DELMN,CMEGAS,DELSUN,SS,XIO,A,F,XI,XNODE,
1          TZERO,XIMOON,XISUN,TMS,XNDM,XNDS,F,XMEANM,XMEANS,XMDTM,XMDOTS,
2          CMGDOT,MEXP
15N 0005      READ (5,1) CMESA1,DELTA1,OMEGA2,DELTA2,XNDM1,CMGDT1
15N 0006      READ (5,1) XID1,XID2,TMS,XMEAN1,XMEAN2
15N 0007      1      FORMAT (3F10.5)
15N 0008      XIMOON=XID1*F
15N 0009      XISUN=XID2*F
15N 0010      DELMN=DELTA1*F
15N 0011      DELSUN=DELTA2*F
15N 0012      CMEGAM=OMEGA1*F
15N 0013      CMEGAS=OMEGA2*F
15N 0014      XMEANM=XMEAN1*F
15N 0015      XMEANS=XMEAN2*F
15N 0016      XNDM=XNDM1*F
15N 0017      CMGDOT=CMGDT1*F
15N 0018      XNDS1=0.78547
15N 0019      WRITE (6,2)
15N 0020      2      FORMAT (10X,//////,5X,'MOON AND SUN DATA',//////)
15N 0021      WRITE (6,3)
15N 0022      3      FORMAT (23X,'OMEGA',10X,'DELTA',7X,'INCLINATION',7X,' TMS ',8X,
1          ' MEAN ANOMALY',2X,' MEAN MOTION',5X,' NODE RATE',/)
15N 0023      WRITE (6,4)
15N 0024      4      FORMAT (21X,'(DEGREES)',6X,'(DEGREES)',6X,'(DEGREES)',7X,'(DAYS)',
1          'X', '(DEGREES)' 4X,'(DEG/DAY)',6X,'(DEG/DAY)',/)
15N 0025      WRITE (6,5) CMESA1,DELTA1,XID1,TMS,XMEAN1,XNDM1,CMGDT1
15N 0026      5      FORMAT (5X,'MOON',10X,7(F10.4,5X),/)
15N 0027      WRITE (6,6) CMESA2,DELTA2,XID2,TMS,XMEAN2,XNDS1
15N 0028      6      FORMAT (5X,'SUN',11X,6(F10.4,5X))
15N 0029      RETURN
15N 0030      END

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## SUBROUTINE REGRES(MT)

C THIS SUBROUTINE CARRIES OUT THE MULTIPLE REGRESSION ANALYSIS.  
 C THIS SUBROUTINE IS A MODIFICATION OF THE PROGRAM EXPLAINED AND LISTED ON  
 C PAGES 304 - 407 OF THE IBM SYSTEM/360 SCIENTIFIC SUBROUTINE PACKAGE,  
 C VERSION III, PROGRAMMERS MANUAL, PROGRAM NUMBER 260A-CM-03X, FIFTH EDITION  
 C (AUGUST 1970).  
 C THE PURPOSE HERE IS TO (1) READ THE PROBLEM PARAMETER CARD FOR A MULTIPLE  
 C REGRESSION, (2) READ SUBSET SELECTION CARDS, (3) CALL THE SUBROUTINES TO  
 C CALCULATE MEANS, STANDARD DEVIATIONS, SIMPLE AND MULTIPLE CORRELATION  
 C COEFFICIENTS, T-VALUES, AND ANALYSIS OF VARIANCE FOR MULTIPLE REGRESSION,  
 C (4) PRINT THE RESULTS, AND (5) SAVE THE REGRESSION COEFFICIENTS AND THEIR  
 C ERRORS FOR SUBROUTINE LCVNUM.  
 C THE NUMBER OF OBSERVATIONS, MEXP, IS CALLED N IN THIS SUBROUTINE. N MUST  
 C BE GREATER THAN M+1, WHERE M IS THE NUMBER OF VARIABLES.  
 C IF SUBSET SELECTION CARDS ARE NOT PRESENT, THE PROGRAM CANNOT PERFORM  
 C MULTIPLE REGRESSION.  
 C AFTER RETURNING FROM SUBROUTINE MINV, THE VALUE OF DETERMINANT (DET) IS  
 C TESTED TO CHECK WHETHER THE CORRELATION MATRIX IS SINGULAR. IF DET IS  
 C COMPARED AGAINST A SMALL CONSTANT, THIS TEST MAY ALSO BE USED TO CHECK NEAR-  
 C SINGULARITY.  
 C THIS SUBROUTINE CALLS SUBROUTINES COJRE (WHICH, IN TURN, CALLS SUBROUTINE  
 C DATA), ORDER, MINV, MULTR. ONLY DATA IS FOUND LISTED HERE, SINCE THE OTHERS  
 C ARE STANDARD SUBROUTINES CONTAINED IN THE MACHINE.

C THE SUBSET SELECTION CARD(S) GIVES K, THE NUMBER OF COEFFICIENTS SOLVED  
 C FOR, AND (ISAVE(J), J=1,K), WHICH CONTAINS THE TIDAL CONSTITUENTS SOLVED FOR.  
 C THE TABLE BELOW GIVES THE TIDAL CONSTITUENTS AND THEIR ISAVE(J) VALUES.

L M P Q TIDE DIS.BODY ISAVE(J) VALUES

2	1	0	-1		MOON	1 AND 2
2	1	0	0	O1	MOON	3 AND 4
2	1	0	1		MOON	5 AND 6
2	1	1	-1		MOON	7 AND 8
2	1	1	0	K1	MOON+ SUN	9 AND 10
2	1	1	1		MOON	11 AND 12
2	1	2	-1		MOON	13 AND 14
2	1	2	0		MOON	15 AND 16
2	1	2	1		MOON	17 AND 18
2	2	0	-1		MOON	19 AND 20
2	2	0	0	M2	MOON	21 AND 22
2	2	0	1		MOON	23 AND 24
2	2	1	-1		MOON	25 AND 26
2	2	1	0	K2	MOON+ SUN	27 AND 28
2	2	1	1		MOON	29 AND 30
2	2	2	-1		MOON	31 AND 32
2	2	2	0		MOON	33 AND 34
2	2	2	1		MOON	35 AND 36
2	1	0	-1		SUN	37 AND 38
2	1	0	0	P1	SUN	39 AND 40
2	1	0	1		SUN	41 AND 42
2	1	1	-1		SUN	43 AND 44
2	1	1	0	K1S	SUN	-
2	1	1	1		SUN	45 AND 46
2	1	2	-1		SUN	47 AND 48
2	1	2	0		SUN	49 AND 50
2	1	2	1		SUN	51 AND 52
2	2	0	-1		SUN	53 AND 54
2	2	0	0	S2	SUN	55 AND 56
2	2	0	1		SUN	57 AND 58
2	2	1	-1		SUN	59 AND 60
2	2	1	0	K2S	SUN	-
2	2	1	1		SUN	61 AND 62
2	2	2	-1		SUN	63 AND 64
2	2	2	0		SUN	65 AND 66
2	2	2	1		SUN	67 AND 68

C EACH CONSTITUENT HAS TWO ISAVE(J) VALUES, SINCE WE SOLVE FOR TWO  
 C PARAMETERS: A LOVE NUMBER AND A LAG ANGLE. IF WE WISH TO SOLVE FOR ONLY A  
 C LOVE NUMBER (FORCING THE LAG ANGLE TO BE ZERO), THEN ONLY THE FIRST ISAVE(J)  
 C VALUE OF THAT CONSTITUENT SHOULD APPEAR ON THE SUBSET SELECTION CARD.



```

C
C THE FOLLOWING DIMENSIONS MUST BE GREATER THAN OR EQUAL TO THE NUMBER OF
C VARIABLES, M
C
ISN 0003      DIMENSION XBAR(70),STD(70),D(70),RY(70),ISAVE(70),V(70),
1 SB(70),T(70),W(70)
C THE FOLLOWING DIMENSION MUST BE GREATER THAN OR EQUAL TO THE PRODUCT OF M*M
ISN 0004      DIMENSION RX(4900)
C THE FOLLOWING DIMENSION MUST BE GREATER THAN OR EQUAL TO (M+1)*M/2
ISN 0005      DIMENSION R(2500)
C THE FOLLOWING DIMENSION MUST BE GREATER THAN OR EQUAL TO 10
ISN 0006      DIMENSION ANS(10)
ISN 0007      DIMENSION VV(70),VF(70)
ISN 0008      COMMON/BLKG/C,A1,B,GLPQM,GLPOS,INDEX
ISN 0009      COMMON/BLKH/VV,VF,ANS,ISAVE,M,K
ISN 0010      1  FORMAT (A4,A2,I5,2I2)
ISN 0011      2  FORMAT (1H0,'MULTIPLE REGRESSION',5X,A4,A2//6X,'SELECTION',12,/)
ISN 0012      3  FORMAT (1H0,'VARIABLE',5X,'MEAN',5X,'STANDARD',6X,'CORRELATION',
1 4X,'REGRESSION',4X,'STD. ERROR',5X,'COMPUTED',/, 'NL',18X,
2'DEVATION',7X,'X VS. Y',7X,'COEFFICIENT',3X,'OF REG. COEF',3X,'T
3VALUE')
ISN 0013      4  FORMAT (1H ,14,6F14.5)
ISN 0014      5  FORMAT (1H , 'DEPENDENT')
ISN 0015      5  FORMAT (1H0//,1H , 'INTERCEPT',10X,F16.5//,1H , 'MULTIPLE CORRELATI
10N',F15.5//,1H , 'STD. ERROR OF ESTIMATE',F13.5//)
ISN 0016      7  FORMAT (1H0,21X,'ANALYSIS OF VARIANCE FOR THE REGRESSION',/,5X,
1 'SOURCE OF VARIATION',7X,'DEGREES',7X,'SUM OF',10X,'MEAN',12X,
2 'F VALUE',/,30X,'OF FREEDOM',4X,'SQUARES',9X,'SQUARES')
ISN 0017      8  FORMAT (1H , 'ATTRIBUTABLE TO REGRESSION',4X,15,3F16.5//,1H ,
1 'DEVIATION FROM REGRESSION',4X,15,2F16.5)
ISN 0019      9  FORMAT (1H ,5X,'TOTAL',19X,15,F16.5)
ISN 0019      10  FORMAT (J5I2)
ISN 0020      11  FORMAT (1H ,15X,'TABLE OF RESIDUALS',/,1H , 'CASE NO.',5X,'Y VALUE
1 5X,'Y ESTIMATE',5X,'RESIDUAL')
ISN 0021      12  FORMAT (1H ,16,F15.5,2F16.5)
ISN 0022      13  FORMAT (1H1,'NUMBER OF SELECTIONS NOT SPECIFIED. JOB TERMINATED')
ISN 0023      14  FORMAT (1H0,'THE MATRIX IS SINGULAR. THIS SELECTION IS SKIPPED.')
ISN 0024      15  FORMAT (10X,7F10.3)
C READ THE PROBLEM PARAMETER CARD
C
C PR,PHI - ALPHANUMERIC NAME OF SATELLITE
C N - NUMBER OF OBSERVATIONS
C M - NUMBER OF VARIABLES
C NS - NUMBER OF SELECTIONS
C
ISN 0025      100 READ (5,1,END=300)PR,PHI,N,M,NS
ISN 0026      100 10=0
ISN 0027      100 K=0
ISN 0028      100 MV= M - 1
ISN 0029      100 DO 30 J=1,MV
ISN 0030      30  VV(J)=0
ISN 0031      CALL CDFR (N,M,10,X,XBAR,STD,RX,R,D,V,T)
C TEST NUMBER OF SELECTIONS
ISN 0032      IF (NS) 105,103,109
ISN 0033      103 WRITE (6,13)
ISN 0034      103 GO TO 300
ISN 0035      104 DO 200 I=1,NS
ISN 0036      200 WRITE (6,2) PF,PHI,I
C READ SUBSET SELECTION CARD
C
C K - NUMBER OF INDEPENDENT VARIABLES INCLUDED
C ISAVE - A VECTOR CONTAINING THE INDEPENDENT VARIABLES INCLUDED
C
ISN 0037      READ (5,1) K,(ISAVE(J), J=1,K)
C NDEP - DEPENDENT VARIABLE
ISN 0038      NDEP=0
ISN 0039      CALL UPRD (M,NDEP,K,ISAVE,RX,RY)
ISN 0040      CALL INTR (RX,K,DET,V,T)
C TEST SINGULARITY OF THE MATRIX INVERTED
ISN 0041      IF (DET) 112,110,112
ISN 0042      110 WRITE (6,14)
ISN 0043      110 GO TO 200
ISN 0044      112 CALL MULT (N,K,XBAR,STD,D,RX,RY,ISAVE,V,SB,T,ANS)
C PRINT MEANS, STANDARD DEVIATIONS, INTERCORRELATIONS BETWEEN X AND Y,
C REGRESSION COEFFICIENTS, STANDARD DEVIATIONS OF REGRESSION COEFFICIENTS, AND
C COMPUTED T-VALUES
ISN 0045      MM=K + 1
ISN 0046      WRITE (6,3)

```

```

ISN 0047      DO 115 J=1,K
ISN 0048      L=ISAVE(J)
                C SAVE REGRESSION COEFFICIENTS AND THEIR ERRORS FOR SUBROUTINE LOVNUM
ISN 0049      VV(L)=V(J)
ISN 0050      VE(L)=SE(J)
ISN 0051      115 WRITE (6,4) L,XBAR(L),STD(L),RY(J),V(J),SE(J),T(J)
ISN 0052      WRITE (6,5)
ISN 0053      L=ISAVE(MM)
ISN 0054      WRITE (6,4) L,XBAR(L),STD(L)
                C PRINT INTERCEPT, MULTIPLE CORRELATION COEFFICIENT, AND STANDARD ERROR OF
                C ESTIMATE
ISN 0055      WRITE (6,6) ANS(1),ANS(2),ANS(3)
                C PRINT ANALYSIS OF VARIANCE FOR THE REGRESSION
ISN 0056      WRITE (6,7)
ISN 0057      L=ANS(8)
ISN 0058      WRITE (6,8) K,ANS(4),ANS(6),ANS(10),L,ANS(7),ANS(9)
ISN 0059      L=N - 1
ISN 0060      SUM=ANS(4) + ANS(7)
ISN 0061      WRITE (6,9) L,SUM
                C CALL SUBROUTINE LOVNUM
ISN 0062      CALL LOVNUM(MT)
ISN 0063      200 CONTINUE
ISN 0064      GO TO 100
ISN 0065      300 CONTINUE
ISN 0066      RETURN
ISN 0067      END

```



ISN 0002

## SUBROUTINE THEORY (JPL0T,MT)

C  
C  
C THIS SUBROUTINE COMPUTES THE PERIODS AND AMPLITUDES OF THE CONSTITUENT  
C TIDES OF THE TIP FOR THE SOLID EARTH. GIVEN THE SOLID EARTH LOVE NUMBERS, THE  
C LAG ANGLE IS ASSUMED TO BE ZERO HERE. IT ALSO PLOTS THE RESULTING TIP AS A  
C SAMPLE PLOT IF DESIRED (JPL0T=1 IF YES, 0 IF NO).  
C  
C NOTE: LUNISOLAR TIDES K1 AND K2 ARE LUMPED IN WITH THE LUNAR TIDES.

## NOTATION

C PERDML(LP,LQ) - PERIOD OF LUNAR CONSTITUENT LM,LP,LQ  
C PERDS(LM,LP,LQ) - PERIOD OF SOLAR CONSTITUENT LM,LP,LQ  
C XMOON(LM,LP,LQ) - AMPLITUDE OF LUNAR CONSTITUENT LM,LP,LQ IN ARCSECONDS  
C XSUN(LM,LP,LQ) - AMPLITUDE OF SOLAR CONSTITUENT LM,LP,LQ IN ARCSECONDS  
C  
C

```

ISN 0003      IMPLICIT REAL*8(A-H,C-Z)
ISN 0004      DIMENSION EPSLNM(2,3,7),EPSLNS(2,3,3),ARGUM(2,3,3),ARGUS(2,3,3),
ISN 0005      1 ARGDTM(2,3,3),ARGDTS(2,3,1)
ISN 0006      DIMENSION B1(2),XMOON(2,3,3),XSUN(2,3,3),YKM(2,3,3),YKS(2,3,3)
ISN 0007      DIMENSION TEXP(200),XIEXP(200),T(700),XINCL(700),NTRACK(700)
ISN 0008      DIMENSION C(2,3),A1(2,3),B(2,3),GLPQM(3,3),GLPQS(3,3)
ISN 0009      DIMENSION TIDE(2,3,3)
ISN 0010      DIMENSION SAT(14)
ISN 0011      DIMENSION PERDM(2,3,1),PERDS(2,3,3)
ISN 0012      COMMON/BLKAZ/EPSLNM,EPSLNS,ARGUM,ARGUS,ARGDTM,ARGDTS
ISN 0013      COMMON/BLKBZ/B1,XK,CFNTM,CFNTS,EUM,XMOON,XSUN,YKM,YKS,XKP
ISN 0014      COMMON/BLKC/TEXP,XIEXP,T,XINCL,NTRACK
ISN 0015      COMMON/BLKD/XLAG,Q,MEGAM,DELM,CMEGAS,DELSUN,SS,XIG,A,E,XI,XNCDE,
ISN 0016      1 TZERO,XIMON,XISUN,TMS,XNDM,XNDS,F,XMEANM,XMEANS,XGDTM,XGDTTS,
ISN 0017      2 UMGDT,MEXP
ISN 0018      COMMON/BLKG/C,A1,B,GLPQM,GLPQS,INDEX
ISN 0019      COMMON/BLKI/SA
ISN 0020      DATA BLANK/4H /
ISN 0021      DATA TM112,TM122,TM212,TM222/4H01 ,4HK1 ,4HM2 ,4HK2 /
ISN 0022      DATA TS112,TS122,TS212,TS222/4H01 ,4HK1S ,4HS2 ,4HK2S /
ISN 0023      PI=3.141592653589793
ISN 0024      C FIND THE LARGEST AMPLITUDE OF ALL THE CONSTITUENTS (IGNORING ANY CONSTITUENT
ISN 0025      C WITH A PERIOD LONGER THAN 2000 DAYS. THE 2000 IS AN ARBITRARY FIGURE.)
ISN 0026      XMAX=0.0
ISN 0027      DO 50 LM=1,2
ISN 0028      YLM=LM
ISN 0029      DO 50 LP=1,3
ISN 0030      DO 50 LQ=1,3
ISN 0031      YKM(LM,LP,LQ)=XK
ISN 0032      YKS(LM,LP,LQ)=XK
ISN 0033      XMOON(LM,LP,LQ)=YKM(LM,LP,LQ)*CFNTM*B1(LM)*C(LM,2)*A1(LM,LP)*
ISN 0034      1 GLPQM(LP,LQ)+YLM/(ARGDTM(LM,LP,LQ)+55)
ISN 0035      XMOON(LM,LP,LQ)=DABS(XMOON(LM,LP,LQ))
ISN 0036      PERDM(LM,LP,LQ)=2.0*PI/(ARGDTM(LM,LP,LQ))
ISN 0037      PERDS(LM,LP,LQ)=DABS(PERDM(LM,LP,LQ))
ISN 0038      XSUN(LM,LP,LQ)=YKS(LM,LP,LQ)*CFNTS*B1(LM)*C(LM,2)*B(LM,LP)*
ISN 0039      1 GLPQS(LP,LQ)+YLM/(ARGDTS(LM,LP,LQ)+55)
ISN 0040      XSUN(LM,LP,LQ)=DABS(XSUN(LM,LP,LQ))
ISN 0041      C TAKE CARE OF THE LUNISOLAR CASE
ISN 0042      IF (LP.EQ. 2 .AND. LQ.EQ. 2) XMOON(LM,LP,LQ)=XMOON(LM,LP,LQ) +
ISN 0043      1 XSUN(LM,LP,LQ)
ISN 0044      PERDS(LM,LP,LQ)=2.0*PI/(ARGDTS(LM,LP,LQ))
ISN 0045      PERDS(LM,LP,LQ)=DABS(PERDS(LM,LP,LQ))
ISN 0046      PER=PERDM(LM,LP,LQ)
ISN 0047      IF (PER-2000.0) 54,54,62
ISN 0048      54 CONTINUE
ISN 0049      IF (XMOON(LM,LP,LQ)-XMAX) 62,62,63
ISN 0050      63 XMAX=XMOON(LM,LP,LQ)
ISN 0051      CONTINUE
ISN 0052      PER=PERDS(LM,LP,LQ)
ISN 0053      IF (PER-2000.0) 55,55,66
ISN 0054      55 CONTINUE
ISN 0055      IF (XSUN(LM,LP,LQ)-XMAX) 66,66,67
ISN 0056      67 XMAX=XSUN(LM,LP,LQ)
ISN 0057      CONTINUE
ISN 0058      60 CONTINUE
ISN 0059      WRITE (6,3)
ISN 0060      3 FORMAT (1H1,///)
ISN 0061      WRITE (6,1)
ISN 0062      C DO THE LUNAR TIDES
ISN 0063      C PRINT OUT LM,LP,LQ, CONSTITUENT NAME, DISTURBING BODY, AMPLITUDE IN ARCSEC.

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OF POOR QUALITY

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ISN 0054      C PERIOD IN DAYS, PER CENT OF LARGEST CONSTITUENT, AND ISAVE(J) VALUES
1      1      FORMAT (' L M P Q TIDE DIS.BODY AMPLITUDE PERIOD
1      1      PER CENT ISAVE(J) (FOR USE IN SUBROUTINE REGRES)')
ISN 0055      WRITE (6,2)
ISN 0056      2      FORMAT (32X,'(ARCSEC)',10X,'(DAYE)',/)
ISN 0057      DO 39 LM=1,2
ISN 0058      DO 39 LP=1,3
ISN 0059      DO 39 LQ=1,3
ISN 0060      67      TIDE(LM,LP,LQ)=BLANK
ISN 0061      TIDE(1,1,2)=TM112
ISN 0062      TIDE(1,2,2)=TM122
ISN 0063      TIDE(2,1,2)=TM212
ISN 0064      TIDE(2,2,2)=TM222
ISN 0065      LLL=2
ISN 0066      I=0
ISN 0067      DO 70 LM=1,2
ISN 0068      DO 70 LP=1,3
ISN 0069      LPP=LP - 1
ISN 0070      DO 70 LQ=1,3
ISN 0071      LQQ=LQ - 2
ISN 0072      AMP=(XMOON(LM,LP,LQ)/XMAX)*100.0
ISN 0073      I=I + 1
ISN 0074      I3=I
ISN 0075      I=I+1
ISN 0076      IF (LPP .EQ. 1 .AND. LQQ .EQ. 0) GO TO 71
ISN 0077      WRITE (6,5) LLL,LM,LPP,LQ,TIDE(LM,LP,LQ),XMOON(LM,LP,LQ),
1 PERDM(LM,LP,LQ),AMP,I3,I
ISN 0078      5      FORMAT (4I2,3X,A4,5X,'MOON',5X,D13.6,3X,F10.3,3X,F10.3,4X,I2,
1 ' AND ',I2)
ISN 0079      GO TO 70
ISN 0080      71      WRITE (6,6) LLL,LM,LPP,LQ,TIDE(LM,LP,LQ),XMOON(LM,LP,LQ),
1 PERDM(LM,LP,LQ),AMP,I3,I
ISN 0081      6      FORMAT (4I2,3X,A4,3X,'MOON+SUN',3X,D13.6,3X,F10.3,3X,F10.3,4X,I2,
1 ' AND ',I2)
ISN 0082      70      CONTINUE
ISN 0083      WRITE (6,4)
ISN 0084      4      FORMAT (10X,/)
ISN 0085      C DO THE SOLAR TIDES
C PRINT OUT L,M,P,Q, CONSTITUENT NAME, DISTURBING BODY, AMPLITUDE IN ARCSEC,
C PERIOD IN DAYS, PER CENT OF LARGEST CONSTITUENT, AND ISAVE(J) VALUES
ISN 0086      DO 38 LM=1,2
ISN 0087      DO 38 LP=1,3
ISN 0088      DO 38 LQ=1,3
ISN 0089      88      TIDE(LM,LP,LQ)=BLANK
ISN 0090      TIDE(1,1,2)=TS112
ISN 0091      TIDE(1,2,2)=TS122
ISN 0092      TIDE(2,1,2)=TS212
ISN 0093      TIDE(2,2,2)=TS222
ISN 0094      DO 80 LM=1,2
ISN 0095      DO 80 LP=1,3
ISN 0096      LPP=LP - 1
ISN 0097      DO 80 LQ=1,3
ISN 0098      LQQ=LQ - 2
ISN 0099      AMP=(XSUN(LM,LP,LQ)/XMAX)*100.0
ISN 0100      IF (LPP .EQ. 1 .AND. LQQ .EQ. 0) GO TO 81
ISN 0101      I=I + 1
ISN 0102      I3=I
ISN 0103      I=I + 1
ISN 0104      WRITE (6,7) LLL,LM,LPP,LQ,TIDE(LM,LP,LQ),XSUN(LM,LP,LQ),
1 PERDM(LM,LP,LQ),AMP,I3,I
ISN 0105      7      FORMAT (4I2,3X,A4,5X,'SUN',6X,D13.6,3X,F10.3,3X,F10.3,4X,I2,
1 ' AND ',I2)
ISN 0106      GO TO 80
ISN 0107      81      WRITE (6,8) LLL,LM,LPP,LQ,TIDE(LM,LP,LQ)
ISN 0108      8      FORMAT (4I2,3X,A4,5X,'SUN',10X,'...',14X,'...',11X,'...',5X,'...')
ISN 0109      80      CONTINUE
ISN 0110      WRITE (6,20) XK
ISN 0111      20      FORMAT (//////,10X,'THEORETICAL AMPLITUDES ASSUMING SOLID EARTH LOW
1E NUMEEF K2 = ',F7.3)
ISN 0112      WRITE (6,21) (SAT(J), J=1,14)
ISN 0113      21      FORMAT (//////,10X,13A6,A2)
ISN 0114      C PRINT OUT A PLOT OF THE SOLID EARTH TIP (IF JPLOT=1)
ISN 0115      IF (JPLOT .EQ. 1) GO TO 83
ISN 0116      GO TO 12
ISN 0117      83      CONTINUE
ISN 0118      DO 10 L=1,MT
ISN 0119      TT=T(L)
ISN 0120      CALL ARG(TT)
ISN 0121      SUM=0.0
ISN 0122      DO 90 LM=1,2
ISN 0123

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ISN 0124      YLM=LM
ISN 0125      DO 90 LP=1,3
ISN 0126      DO 90 LQ=1,3
ISN 0127      XMOCN(LM,LP,LQ)=YKM(LM,LP,LQ)*CFNTM*B1(LM)*C(LM,2)*A1(LM,LP)*GLPQM
ISN 0128      1 (LP,LQ)*YLM*ARGUM(LM,LP,LQ)/(ARGCTM(LM,LP,LQ)*SS)
ISN 0129      XSNICM(LP,LQ)=YKS(LM,LP,LQ)*CFNTS*B1(LM)*C(LM,2)*E(LM,LP)*GLPQS(L
ISN 0130      1P,LQ)*YLM*ARGLS(LM,LP,LQ)/(ARGCTS(LM,LP,LQ)*SS)
ISN 0131      SUM=SUM + XMOCN(LM,LP,LQ) + XSN(LM,LP,LQ)
ISN 0132      90 CONTINUE
ISN 0133      XINCL(L)=SUM
ISN 0134      10 CGNTINUE
ISN 0135      CALL PLOTTER (MT,MEXP)
ISN 0136      12 CONTINUE
ISN 0137      RETURN
ISN 0138      END

```

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ISN 0002      SUBROUTINE TIME1(TSTART,TEND,DT,M)
C
C
C      THIS SUBROUTINE FILLS IN THE VALUES OF ARRAY T(L), BY KNOWING THE STARTING
C      TIME (TSTART), THE ENDING TIME (TEND), AND THE TIME INTERVAL BETWEEN
C      POINTS (DT).
C
C
ISN 0003      IMPLICIT REAL*8 (A-H,O-Z)
ISN 0004      DIMENSION TEXP(200),XIEXP(200),T(700),XINCL(700),NTRACK(700)
ISN 0005      COMMON/BLKC/TEXP,XIEXP,T,XINCL,NTRACK
ISN 0006      M=(TEND-TSTART)/DT + 1.100
ISN 0007      DO 12 L=1,M
ISN 0008      XM=L-1
ISN 0009      12 T(L)=TSTART + XM*DT
ISN 0010      RETURN
ISN 0011      END

```

SATELLITE GEOS - 1 , 1966-1967 DATA

SATELLITE DATA

A (10**R CM)	E	INCLINATION (DEGREES)	NODE RATE (DEG/DAY)	TZERO (DAYS)	NODE (DEGREES)
8.0729	0.0726	59.3805	-2.2465	38.5000	-109.0820

MCCN AND SUN DATA

	OMEGA (DEGREES)	DELTA (DEGREES)	INCLINATION (DEGREES)	TMS (DAYS)	MEAN ANOMALY (DEGREES)	MEAN MOTION (DEG/DAY)	NODE RATE (DEG/DAY)
MCCN	10.1770	105.9932	27.2032	35.0000	331.5588	13.1839	-0.0082
SUN	0.0	313.7153	23.4432	35.0000	31.3590	0.9856	

TSTART= 37.0000 TEND= 665.0000 DT= 2.0000 (DAYS)

SOLID EARTH LOVE NUMBER= 0.3000 LOAD DEFORMATION COEFFICIENT= -0.3000

SOLID EARTH LAG ANGLE= 0.0 DEGREES



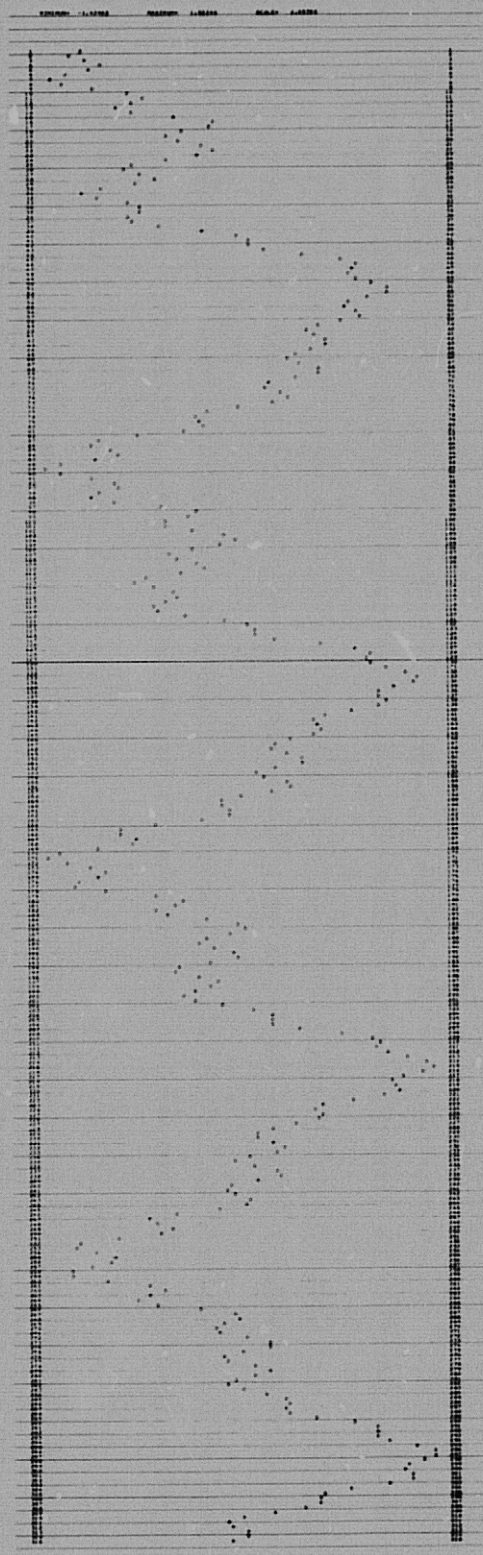
L	M	P	Q	TIDE	DIS. BODY	AMPLITUDE (ARCSEC)	PERIOD (DAYS)	PER CENT	ISAVE(J) (FOR USE IN SUBROUTINE REGRES)
---	---	---	---	------	-----------	-----------------------	------------------	----------	---

1	0	-1			MOON	0.2725120-02	23.164	0.298	1 AND 2
1	0	0		P1	MOON	0.3393450-01	12.585	5.894	3 AND 4
1	0	1			MOON	0.7114270-02	8.639	0.777	5 AND 6
1	1	-1			MOON	0.1104810-01	13.251	1.207	7 AND 8
1	1	0		K1	MOON+ SUN	0.9150730-00	160.830	100.000	9 AND 10
1	1	1			MOON	0.7816130-02	23.424	0.854	11 AND 12
1	2	-1			MOON	0.4667510-01	9.673	0.651	13 AND 14
1	2	0			MOON	0.3744690-02	14.920	0.409	15 AND 16
1	2	1			MOON	0.2341700-01	32.537	0.624	17 AND 18
1	0	-1			MOON	0.8315410-02	20.248	0.609	19 AND 20
1	0	0		M2	MOON	0.1746150-00	11.671	19.082	21 AND 22
1	0	1			MOON	0.2356510-01	8.199	2.576	23 AND 24
1	1	-1			MOON	0.5049230-03	41.918	0.661	25 AND 26
1	1	0		K2	MOON+ SUN	0.1896690-00	90.415	20.727	27 AND 28
1	1	1			MOON	0.2561530-02	20.522	0.324	29 AND 30
1	2	-1			MOON	0.1015430-01	10.699	0.011	31 AND 32
1	2	0			MOON	0.3438520-03	16.445	0.092	33 AND 34
1	2	1			MOON	0.6745230-04	50.789	0.006	35 AND 36

1	0	-1			SUN	0.1614230-02	111.375	0.176	37 AND 38
1	0	0		P1	SUN	0.1491470-00	85.352	15.190	39 AND 40
1	0	1			SUN	0.7019010-02	69.185	0.767	41 AND 42
1	1	-1			SUN	0.1137520-01	245.502	1.298	43 AND 44
1	1	0		K1S	SUN	...	...	...	...
1	1	1			SUN	0.4834330-02	111.361	0.506	45 AND 46
1	2	-1			SUN	0.2213370-02	506.786	0.242	47 AND 48
1	2	0			SUN	0.9772110-01	1307.942	10.680	49 AND 50
1	2	1			SUN	0.1781490-03	285.524	0.019	51 AND 52
1	0	-1			SUN	0.3677630-02	45.768	0.424	53 AND 54
1	0	0		S2	SUN	0.3534730-00	55.690	43.010	55 AND 56
1	1	-1			SUN	0.1595120-01	48.322	2.141	57 AND 58
1	1	0			SUN	0.1564450-02	112.638	0.171	59 AND 60
1	1	1		K2S	SUN	...	...	...	...
1	2	-1			SUN	0.1001570-02	65.703	0.109	61 AND 62
1	2	0			SUN	0.1754010-01	234.343	0.020	63 AND 64
1	2	1			SUN	0.1869730-02	142.756	0.204	65 AND 66
1	0	0			SUN	0.1122530-04	102.641	0.001	67 AND 68

THEORETICAL AMPLITUDES ASSUMING SOLID EARTH LOVE NUMBER K2 = 0.300

CEDS - 1 . 1966-1967 DATA





# SATELLITE TRACKING DATA

( 142 DATA POINTS, TDAY= 38.5000 DAYS)

TIME		INCLINATION			
(DAYS)		(ARCSEC)			
(JAN 1, 0 HRS UT = 1)					
1	39.5000	-1.1364	59	317.5000	0.1690
2	51.5000	-0.8971	60	321.5000	0.4834
3	54.5000	-0.5933	61	325.5000	-0.0566
4	62.5000	-0.6999	62	329.5000	0.1476
5	64.5000	-0.2256	63	333.5000	-0.0505
6	66.5000	0.0125	64	337.5000	0.3736
7	69.5000	-0.1465	65	341.5000	-0.0295
8	71.5000	-0.3124	66	345.5000	0.2167
9	86.5000	-0.7067	67	349.5000	0.1344
10	93.5000	-0.6178	68	351.5000	-0.1005
11	94.5000	-0.7388	69	353.5000	-0.2383
12	94.5000	-0.8415	70	353.5000	-0.7592
13	102.5000	-0.6733	71	357.5000	-0.9170
14	106.5000	-0.6051	72	371.5000	-0.7586
15	110.5000	-0.4471	73	373.5000	-0.6970
16	114.5000	0.1713	74	377.5000	-1.1079
17	118.5000	0.3472	75	381.5000	-0.8792
18	122.5000	0.5373	76	385.5000	-1.0307
19	126.5000	0.8699	77	389.5000	-1.0985
20	130.5000	0.9427	78	393.5000	-0.3035
21	134.5000	1.0141	79	397.5000	-0.3920
22	139.5000	0.9800	80	401.5000	-0.2335
23	143.5000	0.7383	81	405.5000	-0.1777
24	147.5000	0.7650	82	409.5000	-0.0055
25	151.5000	0.6338	83	413.5000	-0.3469
26	155.5000	0.3569	84	417.5000	-0.0518
27	159.5000	0.0364	85	421.5000	-0.2334
28	163.3750	0.3583	86	425.5000	-0.3919
29	168.5000	0.6175	87	430.5000	-0.1351
30	172.5000	0.6493	88	434.5000	-0.5187
31	176.5000	0.4152	89	438.5000	-0.2887
32	181.5000	0.3485	90	442.5000	0.1284
33	184.5000	0.2236	91	446.5000	0.0845
34	188.5000	-0.1095	92	450.5000	0.7752
35	192.5000	-0.1428	93	454.5000	1.1407
36	196.5000	-0.3616	94	458.5000	0.4090
37	200.5000	-0.7014	95	462.5000	1.2743
38	204.5000	-0.8355	96	466.5000	1.1251
39	207.5000	-0.8165	97	470.5000	0.9297
40	211.5000	-0.4939	98	474.5000	0.8581
41	214.5000	-1.1035	99	474.5000	0.7030
42	218.5000	-0.7276	100	482.5000	0.2595
43	222.5000	-0.7276	101	486.5000	0.3372
44	226.5000	-0.6962	102	490.5000	-0.1988
45	230.5000	-0.3618	103	494.5000	-0.2286
46	230.5000	-0.2757	104	498.5000	0.1401
47	270.5000	-0.6275	105	507.5000	0.0071
48	273.5000	-0.6399	106	521.5000	-0.0057
49	277.5000	-0.0609	107	525.5000	-0.3877
50	281.5000	-0.0321	108	529.5000	-0.5373
51	285.5000	0.6245	109	533.5000	-0.6428
52	289.5000	0.8206	110	537.5000	-0.7491
53	294.5000	1.0013	111	541.5000	-1.1432
54	297.5000	0.8364	112	545.5000	-0.8495
55	301.5000	1.2144	113	549.5000	-0.6622
56	305.5000	0.6348	114	553.5000	-0.5727
57	312.5000	0.6566	115	557.5000	-0.2525
58	317.5000	0.6481	116	561.5000	-0.6371

117	565.5000	-0.1555
118	566.5000	-0.0840
119	573.5000	0.0519
120	577.5000	0.2469
121	581.5000	0.0864
122	585.5250	0.0724
123	549.5000	-0.2413
124	593.5000	0.2322
125	597.5000	-0.3299
126	601.5000	0.1958
127	605.5000	0.1358
128	609.5000	0.3215
129	613.6250	0.5361

130	615.5000	1.1740
131	619.5000	1.0730
132	625.5000	1.1437
133	629.5000	1.2324
134	632.5000	0.6806
135	636.5000	1.2935
136	540.5000	1.0124
137	644.5000	0.3505
138	648.5000	0.3825
139	652.5000	-0.0373
140	656.5000	-0.3360
141	660.2500	-0.1353
142	664.5000	-0.1384



MULTIPLE REGRESSION GEOS 1

SELECTION 1

VARIABLE NO.	MEAN	STANDARD DEVIATION	CORRELATION X VS. Y	REGRESSION COEFFICIENT	STD. ERROR OF REG. COEF.	COMPUTED T VALUE
3	0.11462	1.57594	0.82335	0.34033	0.00905	37.66267
10	-0.02424	1.48806	-0.06838	-0.01634	0.00969	-1.47752
27	0.02810	0.33258	0.19415	0.40344	0.15922	6.91445
28	-0.01233	0.33253	0.27332	0.00298	0.06033	0.04947
36	-0.03475	0.54410	0.00175	0.19384	0.05640	3.43657
40	-0.03306	0.35337	-0.10084	0.01203	0.05716	0.21044
55	-0.06401	0.42311	0.48564	0.00293	0.01546	19.55200
58	-0.02547	0.53516	-0.02570	-0.03784	0.01530	-2.47516
DEPENDENT 69	0.00114	0.65553				

INTERCEPT -0.02420

MULTIPLE CORRELATION 0.95654

STD. ERROR OF ESTIMATE 0.16796

ANALYSIS OF VARIANCE FOR THE REGRESSION

SOURCE OF VARIATION	DEGREES OF FREEDOM	SUM OF SQUARES	MEAN SQUARES	F VALUE
ATTRIBUTABLE TO REGRESSION	8	56.83427	7.10478	251.83546
DEVIATION FROM REGRESSION	133	1.75220	0.02821	
TOTAL	141	58.58647		

\*\*\*\*\*FREQUENCY DEPENDENT LOVE NUMBERS\*\*\*\*\*  
(ASSUMING 2ND DEGREE TIDES ONLY)

\*\*\*\*\*OCEAN TIDE PARAMETERS\*\*\*\*\*  
(ASSUMING 2ND DEGREE TIDES  
ONLY AND SOLID EARTH LOVE  
NUMBER K2=0.300 AND SOLID  
EARTH TIDAL LAG=0.0 DEG)

L	M	P	Q	TIDE	DIST. BODY	LOVE NUMBER	STD. ERROR	LAG ANGLE (DEGREES)	STD. ERROR (DEGREES)	C (CM)	STD. ERROR (CM)	PHASE (DEGREES)	STD. ERROR (DEGREES)
2	1	0	-1		MOON	...	...	...	...	...	...	...	...
2	1	0	0	P1	MOON	...	...	...	...	...	...	...	...
2	1	0	1		MOON	...	...	...	...	...	...	...	...
2	1	1	-1		MOON	...	...	...	...	...	...	...	...
2	1	1	0	K1	MOON+ SUN	0.24175	0.00651	2.40751	1.62644	7.78612	0.84336	9.6549	0.6154
2	1	1	1		MOON	...	...	...	...	...	...	...	...
2	1	2	-1		MOON	...	...	...	...	...	...	...	...
2	1	2	0		MOON	...	...	...	...	...	...	...	...
2	1	2	1		MOON	...	...	...	...	...	...	...	...
2	2	0	-1	M2	MOON	...	...	...	...	...	...	...	...
2	2	0	0		MOON	...	...	...	...	...	...	...	...
2	2	0	1		MOON	...	...	...	...	...	...	...	...
2	2	1	-1		MOON	...	...	...	...	...	...	...	...
2	2	1	0	K2	MOON+ SUN	0.30395	0.04396	-0.41760	8.44130	0.07279	0.71074	119.3336	364.8974
2	2	1	1		MOON	...	...	...	...	...	...	...	...
2	2	2	-1		MOON	...	...	...	...	...	...	...	...
2	2	2	0		MOON	...	...	...	...	...	...	...	...
2	2	2	1		MOON	...	...	...	...	...	...	...	...

2	1	0	-1		SUN	...	...	...	...	...	...	...	...
2	1	0	0	P1	SUN	0.19421	0.05541	-3.55109	16.86308	4.27242	2.25596	173.5353	30.6499
2	1	0	1		SUN	...	...	...	...	...	...	...	...
2	1	1	-1		SUN	...	...	...	...	...	...	...	...
2	1	1	0	K1S	SUN	...	...	...	...	...	...	...	...
2	1	1	1		SUN	...	...	...	...	...	...	...	...
2	1	2	-1		SUN	...	...	...	...	...	...	...	...
2	1	2	0		SUN	...	...	...	...	...	...	...	...
2	1	2	1		SUN	...	...	...	...	...	...	...	...
2	2	0	-1	S2	SUN	0.30534	0.01546	7.12617	2.87214	1.83083	0.73745	4.5006	23.3091
2	2	0	0		SUN	...	...	...	...	...	...	...	...
2	2	0	1		SUN	...	...	...	...	...	...	...	...
2	2	1	-1		SUN	...	...	...	...	...	...	...	...
2	2	1	0	K2S	SUN	...	...	...	...	...	...	...	...
2	2	1	1		SUN	...	...	...	...	...	...	...	...
2	2	2	-1		SUN	...	...	...	...	...	...	...	...
2	2	2	0		SUN	...	...	...	...	...	...	...	...
2	2	2	1		SUN	...	...	...	...	...	...	...	...



## TIDAL INCLINATION

TIME  
(JAN 10 0 HRS UT = 1)INCLINATION  
(ARCSEC)

1	0.470000 02	-0.844470 00	66	0.171000 03	0.412360 00
2	0.470000 02	-0.844470 00	67	0.173000 03	0.413350 00
3	0.470000 02	-0.844470 00	68	0.175000 03	0.414340 00
4	0.470000 02	-0.844470 00	69	0.177000 03	0.415330 00
5	0.470000 02	-0.844470 00	70	0.179000 03	0.416320 00
6	0.470000 02	-0.844470 00	71	0.181000 03	0.417310 00
7	0.470000 02	-0.844470 00	72	0.183000 03	0.418300 00
8	0.470000 02	-0.844470 00	73	0.185000 03	0.419290 00
9	0.470000 02	-0.844470 00	74	0.187000 03	0.420280 00
10	0.470000 02	-0.844470 00	75	0.189000 03	0.421270 00
11	0.470000 02	-0.844470 00	76	0.191000 03	0.422260 00
12	0.470000 02	-0.844470 00	77	0.193000 03	0.423250 00
13	0.470000 02	-0.844470 00	78	0.195000 03	0.424240 00
14	0.470000 02	-0.844470 00	79	0.197000 03	0.425230 00
15	0.470000 02	-0.844470 00	80	0.199000 03	0.426220 00
16	0.470000 02	-0.844470 00	81	0.201000 03	0.427210 00
17	0.470000 02	-0.844470 00	82	0.203000 03	0.428200 00
18	0.470000 02	-0.844470 00	83	0.205000 03	0.429190 00
19	0.470000 02	-0.844470 00	84	0.207000 03	0.430180 00
20	0.470000 02	-0.844470 00	85	0.209000 03	0.431170 00
21	0.470000 02	-0.844470 00	86	0.211000 03	0.432160 00
22	0.470000 02	-0.844470 00	87	0.213000 03	0.433150 00
23	0.470000 02	-0.844470 00	88	0.215000 03	0.434140 00
24	0.470000 02	-0.844470 00	89	0.217000 03	0.435130 00
25	0.470000 02	-0.844470 00	90	0.219000 03	0.436120 00
26	0.470000 02	-0.844470 00	91	0.221000 03	0.437110 00
27	0.470000 02	-0.844470 00	92	0.223000 03	0.438100 00
28	0.470000 02	-0.844470 00	93	0.225000 03	0.439090 00
29	0.470000 02	-0.844470 00	94	0.227000 03	0.440080 00
30	0.470000 02	-0.844470 00	95	0.229000 03	0.441070 00
31	0.470000 02	-0.844470 00	96	0.231000 03	0.442060 00
32	0.470000 02	-0.844470 00	97	0.233000 03	0.443050 00
33	0.470000 02	-0.844470 00	98	0.235000 03	0.444040 00
34	0.470000 02	-0.844470 00	99	0.237000 03	0.445030 00
35	0.470000 02	-0.844470 00	100	0.239000 03	0.446020 00
36	0.470000 02	-0.844470 00	101	0.241000 03	0.447010 00
37	0.470000 02	-0.844470 00	102	0.243000 03	0.448000 00
38	0.470000 02	-0.844470 00	103	0.245000 03	0.449000 00
39	0.470000 02	-0.844470 00	104	0.247000 03	0.450000 00
40	0.470000 02	-0.844470 00	105	0.249000 03	0.451000 00
41	0.470000 02	-0.844470 00	106	0.251000 03	0.452000 00
42	0.470000 02	-0.844470 00	107	0.253000 03	0.453000 00
43	0.470000 02	-0.844470 00	108	0.255000 03	0.454000 00
44	0.470000 02	-0.844470 00	109	0.257000 03	0.455000 00
45	0.470000 02	-0.844470 00	110	0.259000 03	0.456000 00
46	0.470000 02	-0.844470 00	111	0.261000 03	0.457000 00
47	0.470000 02	-0.844470 00	112	0.263000 03	0.458000 00
48	0.470000 02	-0.844470 00	113	0.265000 03	0.459000 00
49	0.470000 02	-0.844470 00	114	0.267000 03	0.460000 00
50	0.470000 02	-0.844470 00	115	0.269000 03	0.461000 00
51	0.470000 02	-0.844470 00	116	0.271000 03	0.462000 00
52	0.470000 02	-0.844470 00	117	0.273000 03	0.463000 00
53	0.470000 02	-0.844470 00	118	0.275000 03	0.464000 00
54	0.470000 02	-0.844470 00	119	0.277000 03	0.465000 00
55	0.470000 02	-0.844470 00	120	0.279000 03	0.466000 00
56	0.470000 02	-0.844470 00	121	0.281000 03	0.467000 00
57	0.470000 02	-0.844470 00	122	0.283000 03	0.468000 00
58	0.470000 02	-0.844470 00	123	0.285000 03	0.469000 00
59	0.470000 02	-0.844470 00	124	0.287000 03	0.470000 00
60	0.470000 02	-0.844470 00	125	0.289000 03	0.471000 00
61	0.470000 02	-0.844470 00	126	0.291000 03	0.472000 00
62	0.470000 02	-0.844470 00	127	0.293000 03	0.473000 00
63	0.470000 02	-0.844470 00	128	0.295000 03	0.474000 00
64	0.470000 02	-0.844470 00	129	0.297000 03	0.475000 00
65	0.470000 02	-0.844470 00	130	0.299000 03	0.476000 00
66	0.470000 02	-0.844470 00	131	0.301000 03	0.477000 00
67	0.470000 02	-0.844470 00	132	0.303000 03	0.478000 00
68	0.470000 02	-0.844470 00	133	0.305000 03	0.479000 00
69	0.470000 02	-0.844470 00	134	0.307000 03	0.480000 00
70	0.470000 02	-0.844470 00	135	0.309000 03	0.481000 00

135	0.050000	03	0.104720	01	207	0.453000	03	0.802070	00
136	0.070000	07	0.078090	00	210	0.455000	03	0.722730	00
137	0.090000	03	0.095260	00	211	0.457000	03	0.102510	01
138	0.110000	03	0.303040	00	212	0.459000	03	0.110560	01
139	0.130000	03	0.703900	00	213	0.461000	03	0.116140	01
140	0.150000	03	0.604280	00	214	0.463000	03	0.119080	01
141	0.170000	03	0.514280	00	215	0.465000	03	0.119310	01
142	0.190000	03	0.427570	00	216	0.467000	03	0.116890	01
143	0.210000	03	0.351120	00	217	0.469000	03	0.111960	01
144	0.230000	07	0.237100	00	218	0.471000	03	0.104800	01
145	0.250000	03	0.236800	00	219	0.473000	03	0.097340	00
146	0.270000	03	0.200560	00	220	0.475000	03	0.085170	00
147	0.290000	03	0.177800	00	221	0.477000	03	0.073590	00
148	0.310000	03	0.157070	00	222	0.479000	03	0.061460	00
149	0.330000	03	0.136610	00	223	0.481000	03	0.049280	00
150	0.350000	03	0.117200	00	224	0.483000	03	0.037500	00
151	0.370000	03	0.101660	00	225	0.485000	03	0.026560	00
152	0.390000	03	0.171260	07	226	0.487000	03	0.168090	00
153	0.410000	03	0.197280	00	227	0.489000	03	0.352470	-01
154	0.430000	03	0.196260	03	228	0.491000	03	0.149730	-01
155	0.450000	03	0.185160	00	229	0.493000	03	-0.298480	-01
156	0.470000	03	0.161460	00	230	0.495000	03	-0.613420	-01
157	0.490000	03	0.123390	00	231	0.497000	03	-0.766120	-01
158	0.510000	03	0.099700	-01	232	0.499000	03	-0.676570	-01
159	0.530000	03	0.116250	-02	233	0.501000	03	-0.672480	-01
160	0.550000	03	-0.021670	-01	234	0.503000	03	-0.487600	-01
161	0.570000	03	-0.178250	00	235	0.505000	03	-0.259780	-01
162	0.590000	03	-0.284500	00	236	0.507000	03	-0.288060	-02
163	0.610000	03	-0.397620	00	237	0.509000	03	0.155830	-01
164	0.630000	03	-0.513780	00	238	0.511000	03	0.287140	-01
165	0.650000	03	-0.628790	00	239	0.513000	03	0.302700	-01
166	0.670000	03	-0.738820	00	240	0.515000	03	0.186480	-01
167	0.690000	03	-0.838110	00	241	0.517000	03	-0.797220	-02
168	0.710000	03	-0.924210	03	242	0.519000	03	-0.505200	-01
169	0.730000	03	-0.993150	00	243	0.521000	03	-0.108980	00
170	0.750000	03	-0.104210	01	244	0.523000	03	-0.182370	00
171	0.770000	03	-0.106930	01	245	0.525000	03	-0.258820	00
172	0.790000	03	-0.107350	01	246	0.527000	03	-0.365600	00
173	0.810000	03	-0.105640	01	247	0.529000	03	-0.469340	00
174	0.830000	03	-0.101810	01	248	0.531000	03	-0.576120	00
175	0.850000	03	-0.095350	00	249	0.533000	03	-0.681710	00
176	0.870000	03	-0.075860	00	250	0.535000	03	-0.781780	00
177	0.890000	03	-0.057840	00	251	0.537000	03	-0.872120	00
178	0.910000	03	-0.038400	00	252	0.539000	03	-0.948860	00
179	0.930000	03	-0.017850	00	253	0.541000	03	-0.100960	01
180	0.950000	03	-0.004720	00	254	0.543000	03	-0.104890	01
181	0.970000	03	-0.007150	00	255	0.545000	03	-0.106770	01
182	0.990000	03	-0.027930	00	256	0.547000	03	-0.106430	01
183	0.010000	03	-0.019860	00	257	0.549000	03	-0.103890	01
184	0.030000	03	-0.133740	00	258	0.551000	03	-0.092460	00
185	0.050000	03	-0.086370	-01	259	0.553000	03	-0.027160	00
186	0.070000	03	-0.057710	-01	260	0.555000	03	-0.045810	00
187	0.090000	03	-0.047880	-01	261	0.557000	03	-0.075190	00
188	0.110000	03	-0.055960	-01	262	0.559000	03	-0.049670	00
189	0.130000	03	-0.000390	-01	263	0.561000	03	-0.343290	00
190	0.150000	03	-0.117290	00	264	0.563000	03	-0.437250	00
191	0.170000	03	-0.154120	00	265	0.565000	03	-0.335910	00
192	0.190000	03	-0.216370	00	266	0.567000	03	-0.242890	00
193	0.210000	03	-0.269490	00	267	0.569000	03	-0.161840	00
194	0.230000	03	-0.318820	00	268	0.571000	03	-0.052690	-01
195	0.250000	03	-0.355770	00	269	0.573000	03	-0.049260	-01
196	0.270000	03	-0.388100	00	270	0.575000	03	-0.116100	-01
197	0.290000	03	-0.400150	00	271	0.577000	03	0.489970	-02
198	0.310000	03	-0.392970	00	272	0.579000	03	0.567760	-02
199	0.330000	03	-0.364580	00	273	0.581000	03	-0.710970	-02
200	0.350000	03	-0.313970	00	274	0.583000	03	-0.306180	-01
201	0.370000	03	-0.241260	00	275	0.585000	03	-0.013270	-01
202	0.390000	03	-0.147650	00	276	0.587000	03	-0.052640	-01
203	0.410000	03	-0.035410	-01	277	0.589000	03	-0.128210	00
204	0.430000	03	0.022150	-01	278	0.591000	03	-0.155940	00
205	0.450000	03	0.231200	00	279	0.593000	03	-0.174420	00
206	0.470000	03	0.376850	00	280	0.595000	03	-0.130090	00
207	0.490000	03	0.524020	00	281	0.597000	03	-0.170000	00
208	0.510000	03	0.667540	00	282	0.599000	03	-0.142010	00



283	0.601000 03	-0.949110-01
284	0.603000 03	-0.235180-01
285	0.605000 03	0.553080-01
286	0.607000 03	0.157680 00
287	0.609000 03	0.272750 00
288	0.611000 03	0.397540 00
289	0.613000 03	0.523510 00
290	0.615000 03	0.650240 00
291	0.617000 03	0.787690 00
292	0.619000 03	0.905300 00
293	0.621000 03	0.101000 01
294	0.623000 03	0.103580 01
295	0.625000 03	0.115950 01
296	0.627000 03	0.119820 01
297	0.629000 03	0.121030 01
298	0.631000 03	0.119500 01
299	0.633000 03	0.115270 01

300	0.635000 03	0.103490 01
301	0.637000 03	0.094070 00
302	0.639000 03	0.983820 00
303	0.641000 03	0.758320 00
304	0.643000 03	0.522370 00
305	0.645000 03	0.481070 00
306	0.647000 03	0.334660 00
307	0.649000 03	0.203170 00
308	0.651000 03	0.752870-01
309	0.653000 03	-0.769300-01
310	0.655000 03	-0.133200 00
311	0.657000 03	-0.210170 00
312	0.659000 03	-0.266510 00
313	0.661000 03	-0.301920 00
314	0.663000 03	-0.317380 00
315	0.665000 03	-0.314540 00

## RESIDUALS

TIME  
(JAN 1, 0 HRS UT = 1)RESIDUAL  
(ARCSEC)

1	0.385000 02	-0.250850 00	68	0.731500 03	-0.154630 00
2	0.515000 02	0.117330 -02	69	0.859500 03	0.734230 -01
3	0.555000 02	-0.300580 -01	70	0.363500 03	-0.215430 00
4	0.625000 02	-0.343450 00	71	0.267500 03	-0.152570 00
5	0.645000 02	0.394030 -01	72	0.371500 03	0.144530 00
6	0.665000 02	0.149370 00	73	0.273500 03	0.110340 00
7	0.685000 02	-0.173240 -01	74	0.277500 03	-0.235410 00
8	0.705000 02	-0.225620 00	75	0.331500 03	0.167440 00
9	0.865000 02	-0.260290 00	76	0.345500 03	-0.061370 -01
10	0.905000 02	-0.932530 -02	77	0.393500 03	-0.238310 00
11	0.945000 02	-0.147030 -01	78	0.333470 03	0.241720 00
12	0.945000 02	-0.313480 -01	79	0.337500 03	-0.445360 -01
13	0.122500 03	0.243030 -01	80	0.401500 03	-0.525000 -01
14	0.125500 03	-0.715630 -01	81	0.405500 03	-0.100260 00
15	0.110300 03	-0.160050 00	82	0.409500 03	0.428720 -01
16	0.114500 03	0.156870 00	83	0.413500 03	-0.259670 00
17	0.118500 03	0.168070 -01	84	0.417500 03	0.125000 00
18	0.122500 03	-0.316480 -01	85	0.422500 03	0.736510 -01
19	0.126500 03	0.220920 -01	86	0.426500 03	-0.446620 -02
20	0.110500 03	-0.454010 -01	87	0.430500 03	0.261360 00
21	0.134500 03	-0.217870 -01	88	0.434500 03	-0.183950 00
22	0.139500 03	0.252520 -02	89	0.438500 03	-0.115770 00
23	0.143500 03	-0.125770 00	90	0.442500 03	-0.693040 -01
24	0.147500 03	0.123300 -01	91	0.446500 03	-0.254560 00
25	0.151500 03	0.433250 -01	92	0.450500 03	0.142370 00
26	0.155500 03	-0.125180 00	93	0.454500 03	0.249540 00
27	0.159500 03	0.221560 00	94	0.458500 03	-0.278590 00
28	0.163380 03	-0.376270 -01	95	0.462500 03	0.883290 -01
29	0.168500 03	0.121910 -01	96	0.466500 03	-0.522220 -01
30	0.172500 03	0.235130 00	97	0.470500 03	-0.133150 00
31	0.176500 03	0.197820 -01	98	0.474500 03	-0.212500 -01
32	0.180500 03	0.216020 -01	99	0.478500 03	0.577500 -01
33	0.184500 03	0.276520 -01	100	0.482500 03	-0.144430 00
34	0.188500 03	-0.113280 00	101	0.486500 03	0.165980 00
35	0.192500 03	0.071710 -01	102	0.490500 03	-0.073270 00
36	0.196500 03	0.130230 00	103	0.494500 03	-0.173590 00
37	0.200500 03	-0.572500 -01	104	0.498500 03	0.018650 00
38	0.204500 03	0.071170 -01	105	0.502500 03	0.246450 -01
39	0.207500 03	0.204620 00	106	0.506500 03	0.116310 00
40	0.211500 03	0.723440 -01	107	0.510500 03	-0.255610 -01
41	0.214500 03	-0.667430 -01	108	0.514500 03	-0.011410 -01
42	0.218500 03	0.194000 00	109	0.518500 03	0.645900 -01
43	0.222500 03	0.137950 -01	110	0.522500 03	0.143640 00
44	0.226500 03	-0.165930 00	111	0.526500 03	-0.172580 00
45	0.230500 03	-0.346580 -01	112	0.530500 03	0.219460 00
46	0.234500 03	-0.145710 -01	113	0.534500 03	0.069460 -01
47	0.238500 03	-0.167290 00	114	0.538500 03	-0.644750 -01
48	0.242500 03	-0.326310 00	115	0.542500 03	0.474480 00
49	0.246500 03	-0.786180 -02	116	0.546500 03	-0.120530 00
50	0.250500 03	-0.283510 00	117	0.550500 03	0.156120 00
51	0.254500 03	-0.717790 -02	118	0.554500 03	0.597680 -01
52	0.258500 03	-0.795270 -02	119	0.558500 03	0.959250 -01
53	0.262500 03	-0.228450 -01	120	0.562500 03	0.243410 00
54	0.266500 03	-0.238620 00	121	0.566500 03	0.494560 -01
55	0.270500 03	0.006540 -01	122	0.570500 03	0.104540 00
56	0.274500 03	-0.969550 -01	123	0.574500 03	-0.105470 00
57	0.310500 03	0.301560 -01	124	0.578500 03	0.409460 00
58	0.313500 03	0.266720 00	125	0.582500 03	-0.165130 00
59	0.317500 03	-0.323820 00	126	0.586500 03	0.270860 00
60	0.321500 03	0.149510 00	127	0.590500 03	0.106060 00
61	0.325500 03	-0.281690 00	128	0.594500 03	0.183920 -01
62	0.329500 03	-0.264700 -01	129	0.598500 03	-0.337520 -01
63	0.333500 03	-0.217550 00	130	0.602500 03	0.417510 00
64	0.337500 03	0.189430 00	131	0.606500 03	0.133540 00
65	0.341500 03	-0.227360 00	132	0.610500 03	-0.279220 -01
66	0.345500 03	0.352390 -01	133	0.614500 03	0.624940 -01
67	0.349500 03	0.228960 -01	134	0.618500 03	-0.185040 00



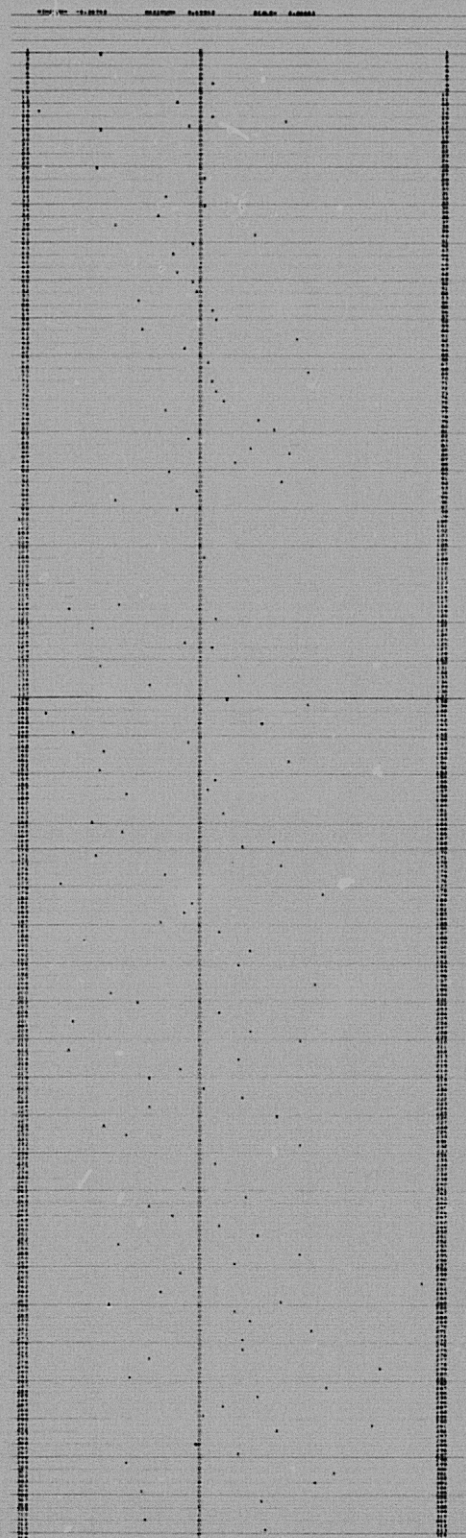
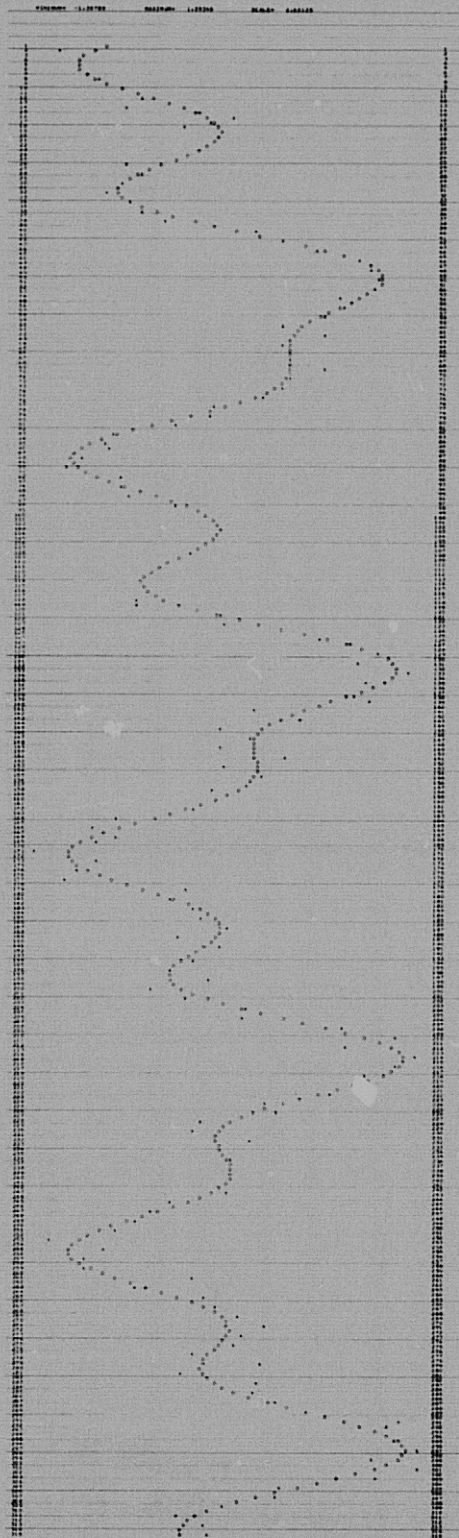
135 0.616500 03  
 136 0.640500 03  
 137 0.644500 03  
 138 0.648500 03

0.274720 00  
 0.221510 00  
 -0.165070 00  
 0.103950 00

139 0.652500 03  
 140 0.655500 03  
 141 0.660250 03  
 142 0.664500 03

-0.272370-01  
 -0.143150 00  
 0.135770 00  
 0.173430 00

SIGMA = SQR((SUM OF SQUARE)/(NEXP-1)) = 0.16314





## MULTIPLE REGRESSION GEOS 1

## SELECTION 2

VARIABLE NO.	MEAN	STANDARD DEVIATION	CORRELATION X VS. Y	REGRESSION COEFFICIENT	STD. ERROR OF REG. COEFF.	COMPUTED T VALUE
9	0.11462	1.57594	0.83835	0.33968	0.00699	48.57646
10	-0.02424	1.48800	-0.06838	-0.01588	0.00746	-2.12973
21	0.00860	0.41027	0.27756	0.25014	0.02680	9.33432
27	0.02810	0.33259	0.19415	0.38970	0.03493	11.15683
49	-0.03470	0.34410	0.00175	0.18491	0.03360	5.50297
55	-0.06401	0.02311	0.48554	0.29684	0.01200	24.73010
56	-0.02547	0.63616	-0.02570	-0.03398	0.01184	-2.87070
DEPENDENT 60	0.00114	0.65553				

INTERCEPT -0.02673

MULTIPLE CORRELATION 0.98108

STD. ERROR OF ESTIMATE 0.13028

## ANALYSIS OF VARIANCE FOR THE REGRESSION

SOURCE OF VARIATION	DEGREE OF FREEDOM	SUM OF SQUARES	MEAN SQUARES	F VALUE
ATTRIBUTABLE TO REGRESSION	7	58.31595	8.33085	430.79956
DEVIATION FROM REGRESSION	134	2.27452	0.01697	
TOTAL	141	60.59047		

\*\*\*\* FREQUENCY DEPENDENT LOVE NUMBERS \*\*\*\*  
(ASSUMING 2ND DEGREE TIDES ONLY)

\*\*\*\* OCEAN TIDE PARAMETERS \*\*\*\*  
(ASSUMING 2ND DEGREE TIDES  
ONLY AND SOLID EARTH LOVE  
NUMBER K2=0.300 AND SOLID  
EARTH TIDAL LAG=0.0 DEG)

L	M	P	O	TIDE	DIST. BODY	LOVE NUMBER	STD. ERROR	LAG ANGLE (DEGREES)	STD. ERROR (DEGREES)	C (CM)	STD. ERROR (CM)	PHASE (DEGREES)	STD. ERROR (DEGREES)
2	1	0	-1		MOON	...	...	...	...	...	...	...	...
2	1	0	0	P1	MOON	...	...	...	...	...	...	...	...
2	1	0	1		MOON	...	...	...	...	...	...	...	...
2	1	1	-1		MOON	...	...	...	...	...	...	...	...
2	1	1	0	K1	MOON+ SUN	0.24082	0.00495	2.67743	1.25557	7.92093	0.65155	10.7300	4.9983
2	1	1	1		MOON	...	...	...	...	...	...	...	...
2	1	2	-1		MOON	...	...	...	...	...	...	...	...
2	1	2	0		MOON	...	...	...	...	...	...	...	...
2	1	2	1		MOON	...	...	...	...	...	...	...	...
2	2	0	-1	M2	MOON	0.25014	0.02580	0.0	0.0	5.03832	2.73349	270.0000	0.0
2	2	0	0		MOON	...	...	...	...	...	...	...	...
2	2	0	1		MOON	...	...	...	...	...	...	...	...
2	2	1	-1		MOON	...	...	...	...	...	...	...	...
2	2	1	0	K2	MOON+ SUN	0.24926	0.02593	0.0	0.0	0.17294	0.41731	270.0000	0.0
2	2	1	1		MOON	...	...	...	...	...	...	...	...
2	2	2	-1		MOON	...	...	...	...	...	...	...	...
2	2	2	0		MOON	...	...	...	...	...	...	...	...
2	2	2	1		MOON	...	...	...	...	...	...	...	...
2	1	0	-1		SUN	...	...	...	...	...	...	...	...
2	1	0	0	P1	SUN	0.18491	0.03360	0.0	0.0	4.60221	1.34373	180.0000	0.0
2	1	0	1		SUN	...	...	...	...	...	...	...	...
2	1	1	-1		SUN	...	...	...	...	...	...	...	...
2	1	1	0	K1S	SUN	...	...	...	...	...	...	...	...
2	1	1	1		SUN	...	...	...	...	...	...	...	...
2	1	2	-1		SUN	...	...	...	...	...	...	...	...
2	1	2	0		SUN	...	...	...	...	...	...	...	...
2	1	2	1		SUN	...	...	...	...	...	...	...	...
2	2	0	-1	S2	SUN	0.25978	0.01200	0.52989	2.27010	1.64422	0.57037	354.6859	20.1514
2	2	0	0		SUN	...	...	...	...	...	...	...	...
2	2	0	1		SUN	...	...	...	...	...	...	...	...
2	2	1	-1		SUN	...	...	...	...	...	...	...	...
2	2	1	0	K2S	SUN	...	...	...	...	...	...	...	...
2	2	1	1		SUN	...	...	...	...	...	...	...	...
2	2	2	-1		SUN	...	...	...	...	...	...	...	...
2	2	2	0		SUN	...	...	...	...	...	...	...	...
2	2	2	1		SUN	...	...	...	...	...	...	...	...

08



## TIDAL INCLINATION

TIME  
(JAN 1, 0 HRS UT = 1)INCLINATION  
(ARCSEC)

1	0.370000 02	-0.332850 00	58	0.171000 03	0.418530 00
2	0.370000 02	-0.104790 01	59	0.173000 03	0.539240 00
3	0.410000 02	-0.995360 00	60	0.175000 03	0.432510 00
4	0.410000 02	-0.891870 00	71	0.177000 03	0.270780 00
5	0.450000 02	-0.883450 00	72	0.179000 03	0.204030 00
6	0.470000 02	-0.991170 00	73	0.181000 03	0.269670 00
7	0.470000 02	-0.103920 01	74	0.183000 03	0.351430 00
8	0.510000 02	-0.103940 01	75	0.185000 03	0.300660 00
9	0.510000 02	-0.835050 00	76	0.187000 03	0.924400 -01
10	0.510000 02	-0.817830 00	77	0.189000 03	-0.147400 00
11	0.570000 02	-0.525110 00	78	0.191000 03	-0.272990 00
12	0.570000 02	-0.557910 00	79	0.193000 03	-0.263310 00
13	0.570000 02	-0.575940 00	80	0.195000 03	-0.254820 00
14	0.510000 02	-0.460950 00	81	0.197000 03	-0.392580 00
15	0.510000 02	-0.235240 00	82	0.199000 03	-0.646220 00
16	0.670000 02	-0.505380 -01	83	0.201000 03	-0.882250 00
17	0.670000 02	-0.283510 -01	84	0.203000 03	-0.965560 00
18	0.710000 02	-0.138170 00	85	0.205000 03	-0.911370 00
19	0.710000 02	-0.228400 00	86	0.207000 03	-0.858650 00
20	0.710000 02	-0.190850 00	87	0.209000 03	-0.927820 00
21	0.770000 02	-0.724590 -01	88	0.211000 03	-0.108790 01
22	0.770000 02	-0.252300 -01	89	0.213000 03	-0.118880 01
23	0.810000 02	-0.145100 00	90	0.215000 03	-0.111880 01
24	0.810000 02	-0.367360 00	91	0.217000 03	-0.922570 00
25	0.810000 02	-0.531320 00	92	0.219000 03	-0.736110 00
26	0.870000 02	-0.544650 00	93	0.221000 03	-0.725160 00
27	0.870000 02	-0.475560 00	94	0.223000 03	-0.777550 00
28	0.870000 02	-0.475000 00	95	0.225000 03	-0.762090 00
29	0.930000 02	-0.616750 00	96	0.227000 03	-0.592160 00
30	0.930000 02	-0.403270 00	97	0.229000 03	-0.341540 00
31	0.970000 02	-0.800550 00	98	0.231000 03	-0.171680 00
32	0.970000 02	-0.797840 00	99	0.233000 03	-0.145000 00
33	0.101000 03	-0.625140 00	100	0.235000 03	-0.245000 00
34	0.101000 03	-0.326590 00	101	0.237000 03	-0.263050 00
35	0.101000 03	-0.553270 00	102	0.239000 03	-0.144790 00
36	0.107000 03	-0.595440 00	103	0.241000 03	-0.130310 -01
37	0.107000 03	-0.316030 00	104	0.243000 03	-0.553340 -01
38	0.111000 03	-0.269980 00	105	0.245000 03	-0.711770 -01
39	0.111000 03	-0.175920 -01	106	0.247000 03	-0.250490 00
40	0.115000 03	0.194400 00	107	0.249000 03	-0.356270 00
41	0.117000 03	0.231790 00	108	0.251000 03	-0.312940 00
42	0.119000 03	0.250370 00	109	0.253000 03	-0.239500 00
43	0.121000 03	0.337580 00	110	0.255000 03	-0.280390 00
44	0.123000 03	0.648270 00	111	0.257000 03	-0.458730 00
45	0.123000 03	0.894380 00	112	0.259000 03	-0.547120 00
46	0.127000 03	0.988510 00	113	0.261000 03	-0.696890 00
47	0.129000 03	0.931020 00	114	0.263000 03	-0.590130 00
48	0.131000 03	0.861500 00	115	0.265000 03	-0.454910 00
49	0.131000 03	0.908280 00	116	0.267000 03	-0.427770 00
50	0.135000 03	0.105380 01	117	0.269000 03	-0.608340 00
51	0.137000 03	0.115380 01	118	0.271000 03	-0.558960 00
52	0.139000 03	0.109070 01	119	0.273000 03	-0.449720 00
53	0.141000 03	0.899620 00	120	0.275000 03	-0.196580 00
54	0.143000 03	0.734660 00	121	0.277000 03	0.529790 -01
55	0.145000 03	0.710530 00	122	0.279000 03	0.171580 00
56	0.147000 03	0.785760 00	123	0.281000 03	0.181660 00
57	0.149000 03	0.810360 00	124	0.283000 03	0.227140 00
58	0.151000 03	0.687350 00	125	0.285000 03	0.416880 00
59	0.153000 03	0.475210 00	126	0.287000 03	0.704980 00
60	0.155000 03	0.341220 00	127	0.289000 03	0.333840 00
61	0.157000 03	0.367310 00	128	0.291000 03	0.393740 00
62	0.159000 03	0.488950 00	129	0.293000 03	0.919210 00
63	0.161000 03	0.540000 00	130	0.295000 03	0.919050 00
64	0.163000 03	0.450560 00	131	0.297000 03	0.102640 01
65	0.165000 03	0.295400 00	132	0.299000 03	0.119390 01
66	0.167000 03	0.240410 00	133	0.301000 03	0.126550 01
67	0.169000 03	0.335090 00	134	0.303000 03	0.116070 01

133	0.305000	03	0.961090	03	209	0.453000	03	0.934060	03
135	0.317000	03	0.825870	00	210	0.455000	03	0.959850	00
137	0.306000	03	0.831580	00	211	0.457000	03	0.914140	00
138	0.311000	03	0.888680	00	212	0.459000	03	0.947790	00
139	0.313000	03	0.846750	00	213	0.461000	03	0.110660	01
140	0.315000	03	0.653130	00	214	0.463000	03	0.128040	01
141	0.317000	03	0.413580	00	215	0.465000	03	0.131710	01
142	0.319000	03	0.235740	00	216	0.467000	03	0.118210	01
143	0.321000	03	0.314360	00	217	0.469000	03	0.994730	00
144	0.323000	03	0.393030	00	218	0.471000	03	0.904680	00
145	0.325000	03	0.370770	00	219	0.473000	03	0.936740	00
146	0.327000	03	0.213150	00	220	0.475000	03	0.958220	00
147	0.329000	03	0.558100	-01	221	0.477000	03	0.861900	00
148	0.331000	03	0.277170	-01	222	0.479000	03	0.614850	00
149	0.333000	03	0.148410	00	223	0.481000	03	0.365210	00
150	0.335000	03	0.135600	00	224	0.483000	03	0.255750	00
151	0.337000	03	0.296540	00	225	0.485000	03	0.281420	00
152	0.339000	03	0.174300	00	226	0.487000	03	0.305750	00
153	0.341000	03	0.518740	-01	227	0.489000	03	0.203910	00
154	0.343000	03	0.430250	-01	228	0.491000	03	-0.219800	-02
155	0.345000	03	0.187930	00	229	0.493000	03	-0.165090	00
156	0.347000	03	0.283300	00	230	0.495000	03	-0.165830	00
157	0.349000	03	0.222460	00	231	0.497000	03	-0.321320	-01
158	0.351000	03	0.292180	-01	232	0.499000	03	0.621300	-01
159	0.353000	03	-0.147380	00	233	0.501000	03	0.257780	-01
160	0.355000	03	-0.132330	00	234	0.503000	03	-0.104260	00
161	0.357000	03	-0.141470	00	235	0.505000	03	-0.177800	00
162	0.359000	03	-0.145140	00	236	0.507000	03	-0.932640	-01
163	0.361000	03	-0.305100	00	237	0.509000	03	0.672460	-01
164	0.363000	03	-0.665420	00	238	0.511000	03	0.161920	00
165	0.365000	03	-0.759990	00	239	0.513000	03	0.235720	-01
166	0.367000	03	-0.916260	00	240	0.515000	03	-0.576500	-01
167	0.369000	03	-0.765650	00	241	0.517000	03	-0.166610	00
168	0.371000	03	-0.773820	00	242	0.519000	03	-0.128030	00
169	0.373000	03	-0.912420	00	243	0.521000	03	-0.366550	-01
170	0.375000	03	-0.111020	-01	244	0.523000	03	-0.480880	-01
171	0.377000	03	-0.120550	01	245	0.525000	03	-0.224280	00
172	0.379000	03	-0.112710	01	246	0.527000	03	-0.446540	00
173	0.381000	03	-0.961240	00	247	0.529000	03	-0.616700	00
174	0.383000	03	-0.865850	00	248	0.531000	03	-0.620110	00
175	0.385000	03	-0.902120	00	249	0.533000	03	-0.579280	00
176	0.387000	03	-0.972930	00	250	0.535000	03	-0.641950	00
177	0.389000	03	-0.927750	00	251	0.537000	03	-0.841530	00
178	0.391000	03	-0.724410	00	252	0.539000	03	-0.105780	01
179	0.393000	03	-0.477480	00	253	0.541000	03	-0.113950	01
180	0.395000	03	-0.342230	00	254	0.543000	03	-0.106910	01
181	0.397000	03	-0.355930	00	255	0.545000	03	-0.943180	00
182	0.399000	03	-0.403180	00	256	0.547000	03	-0.910460	00
183	0.401000	03	-0.341410	00	257	0.549000	03	-0.103220	01
184	0.403000	03	-0.154500	00	258	0.551000	03	-0.111640	01
185	0.405000	03	0.272710	-01	259	0.553000	03	-0.104850	01
186	0.407000	03	0.620920	-01	260	0.555000	03	-0.835240	00
187	0.409000	03	-0.554870	-01	261	0.557000	03	-0.619890	00
188	0.411000	03	-0.188990	00	262	0.559000	03	-0.635440	00
189	0.413000	03	-0.202570	00	263	0.561000	03	-0.568560	00
190	0.415000	03	-0.102430	00	264	0.563000	03	-0.577910	00
191	0.417000	03	-0.268720	-01	265	0.565000	03	-0.447120	00
192	0.419000	03	-0.781070	-01	266	0.567000	03	-0.211370	00
193	0.421000	03	-0.289290	00	267	0.569000	03	-0.242490	-01
194	0.423000	03	-0.448140	00	268	0.571000	03	0.302300	-03
195	0.425000	03	-0.453350	00	269	0.573000	03	-0.744360	-01
196	0.427000	03	-0.136830	00	270	0.575000	03	-0.155900	00
197	0.429000	03	-0.248960	00	271	0.577000	03	-0.828150	-01
198	0.431000	03	-0.288900	00	272	0.579000	03	0.600000	-01
199	0.433000	03	-0.405240	00	273	0.581000	03	0.132610	00
200	0.435000	03	-0.448360	00	274	0.583000	03	0.537890	-01
201	0.437000	03	-0.318070	00	275	0.585000	03	-0.124510	00
202	0.439000	03	-0.778880	-01	276	0.587000	03	-0.231390	00
203	0.441000	03	0.113600	00	277	0.589000	03	-0.184730	00
204	0.443000	03	0.167300	00	278	0.591000	03	-0.627450	-01
205	0.445000	03	0.154120	00	279	0.593000	03	-0.182820	-01
206	0.447000	03	0.226480	00	280	0.595000	03	-0.113770	00
207	0.449000	03	0.453470	00	281	0.597000	03	-0.232180	00
208	0.451000	03	0.743140	00	282	0.599000	03	-0.276120	00



283	0.601000 03	-0.131200 00
284	0.603000 03	0.779510-01
285	0.605000 03	0.197970 00
286	0.607000 03	0.187190 00
287	0.609000 03	0.157640 00
288	0.611000 03	0.254490 00
289	0.613000 03	0.499840 00
290	0.615000 03	0.765250 00
291	0.617000 03	0.902070 00
292	0.619000 03	0.892800 00
293	0.621000 03	0.864530 00
294	0.623000 03	0.950560 00
295	0.625000 03	0.114590 01
296	0.627000 03	0.130010 01
297	0.629000 03	0.130770 01
298	0.631000 03	0.115640 01
299	0.633000 03	0.100000 01

300	0.635000 03	0.362330 00
301	0.637000 03	0.101670 01
302	0.639000 03	0.101710 01
303	0.641000 03	0.834440 00
304	0.643000 03	0.573980 00
305	0.645000 03	0.339860 00
306	0.647000 03	0.254010 00
307	0.649000 03	0.267770 00
308	0.651000 03	0.230100 00
309	0.653000 03	0.530200-01
310	0.655000 03	-0.191870 00
311	0.657000 03	-0.345390 00
312	0.659000 03	-0.325810 00
313	0.661000 03	-0.213410 00
314	0.663000 03	-0.165760 00
315	0.665000 03	-0.252760 00



## RESIDUALS

TIME  
(JAN 1, 0 HRS UT = 1)RESIDUAL  
(ARCSEC)

1	0.395000 02	-0.123340 00	67	0.359500 03	-0.691830 -01
2	0.515000 02	-0.131030 00	70	0.363500 03	-0.130320 00
3	0.535000 02	-0.048300 -01	71	0.367500 03	-0.109900 00
4	0.625000 02	-0.195680 00	72	0.371500 03	0.352290 -01
5	0.645000 02	0.090440 -01	73	0.373500 03	0.657490 -01
6	0.655000 02	0.066340 -01	74	0.377500 03	-0.105540 00
7	0.685000 02	-0.128630 00	75	0.381500 03	0.445100 -01
8	0.705000 02	-0.206300 00	76	0.385500 03	-0.107850 00
9	0.865000 02	-0.152000 00	77	0.389500 03	-0.208940 00
10	0.905000 02	-0.155010 00	78	0.393500 03	0.114450 00
11	0.945000 02	0.259940 -01	79	0.397500 03	-0.209230 -01
12	0.985000 02	-0.697620 -02	80	0.401500 03	0.597310 -01
13	0.102500 03	-0.134590 00	81	0.405500 03	-0.219700 00
14	0.106500 03	-0.109450 -01	82	0.409500 03	0.486350 -01
15	0.110500 03	-0.105030 00	83	0.413500 03	-0.162510 00
16	0.114500 03	0.011740 -02	84	0.417500 03	-0.229040 -01
17	0.118500 03	0.103620 00	85	0.422500 03	0.187030 00
18	0.122500 03	0.103480 -01	86	0.426500 03	-0.218650 -01
19	0.126500 03	-0.113610 00	87	0.430500 03	0.128520 00
20	0.130500 03	0.716180 -01	88	0.434500 03	-0.461290 -01
21	0.134500 03	-0.101720 -02	89	0.438500 03	-0.149000 00
22	0.138500 03	-0.099900 -01	90	0.442500 03	-0.371050 -01
23	0.143500 03	-0.242460 -01	91	0.446500 03	-0.109310 00
24	0.147500 03	-0.177040 -01	92	0.450500 03	0.101050 00
25	0.151500 03	-0.366640 -02	93	0.454500 03	0.174620 00
26	0.155500 03	0.244860 -01	94	0.458500 03	-0.117520 00
27	0.159500 03	0.128480 00	95	0.462500 03	0.234410 -01
28	0.163500 03	-0.064030 -01	96	0.466500 03	-0.102240 00
29	0.168500 03	0.116780 00	97	0.470500 03	0.159860 -01
30	0.172500 03	0.107290 00	98	0.474500 03	-0.111300 00
31	0.176500 03	0.107930 00	99	0.478500 03	0.133550 -01
32	0.180500 03	0.103170 00	100	0.482500 03	-0.737720 -02
33	0.184500 03	-0.106560 00	101	0.486500 03	0.286650 -01
34	0.188500 03	-0.157080 -01	102	0.490500 03	-0.230790 00
35	0.192500 03	0.133960 00	103	0.494500 03	-0.457520 -01
36	0.196500 03	-0.160390 -01	104	0.498500 03	0.324950 -01
37	0.200500 03	0.427050 -01	105	0.502500 03	0.872300 -01
38	0.204500 03	0.959790 -01	106	0.506500 03	0.150600 -01
39	0.207500 03	0.461820 -01	107	0.510500 03	-0.402580 00
40	0.211500 03	0.131200 00	108	0.514500 03	0.923880 -01
41	0.214500 03	0.491350 -01	109	0.518500 03	-0.617840 -01
42	0.218500 03	0.391200 -01	110	0.522500 03	0.151710 00
43	0.222500 03	0.371140 -01	111	0.526500 03	-0.612320 -01
44	0.226500 03	-0.484820 -01	112	0.530500 03	0.773400 -01
45	0.230500 03	-0.162520 00	113	0.534500 03	0.992870 -01
46	0.235000 03	0.561120 -01	114	0.538500 03	0.321040 -01
47	0.239500 03	-0.595480 -01	115	0.542500 03	0.331470 00
48	0.243500 03	-0.244350 00	116	0.546500 03	-0.576540 -01
49	0.247500 03	-0.157880 00	117	0.550500 03	0.237520 00
50	0.251500 03	-0.215630 00	118	0.554500 03	-0.824170 -01
51	0.255500 03	-0.742990 -02	119	0.558500 03	0.180090 00
52	0.259500 03	-0.145170 00	120	0.562500 03	0.296780 00
53	0.263500 03	0.758600 -01	121	0.566500 03	-0.487940 -01
54	0.267500 03	-0.182050 00	122	0.570500 03	0.205210 00
55	0.271500 03	-0.409360 -01	123	0.574500 03	-0.859490 -01
56	0.275500 03	0.135700 -01	124	0.578500 03	0.262540 00
57	0.279500 03	-0.214200 -01	125	0.582500 03	-0.561080 -01
58	0.283500 03	0.117250 00	126	0.586500 03	0.269170 00
59	0.287500 03	-0.198400 00	127	0.590500 03	-0.195450 -01
60	0.291500 03	0.146940 00	128	0.594500 03	0.175460 00
61	0.295500 03	-0.397720 00	129	0.598500 03	-0.527500 -01
62	0.299500 03	0.114970 00	130	0.602500 03	0.293100 00
63	0.303500 03	-0.239430 00	131	0.606500 03	0.191990 00
64	0.307500 03	0.995450 -01	132	0.610500 03	-0.528280 -01
65	0.311500 03	-0.711240 -01	133	0.614500 03	-0.333370 -01
66	0.315500 03	-0.451860 -02	134	0.618500 03	-0.501590 -01
67	0.319500 03	-0.475740 -01	135	0.622500 03	0.291720 00
68	0.323500 03	-0.775110 -01	136	0.626500 03	0.101710 00

137  
138  
139

0.644500 C3  
0.645000 C3  
0.645200 C3

-0.30223D-01  
0.79508D-01  
-0.14542D 00

140  
141  
142

0.656500 C3  
0.660200 C3  
0.664500 C3

-0.13216D-01  
0.10345D 00  
0.82349D-01

SIGMA = Sqrt((SUM OF SQUARES)/(NEXP-1)) = 0.12702



Table 1

Orbital Data for the BE-C, GEOS-I, and  
GEOS-II Satellites

Satellite	Semimajor Axis ( $10^8$ cm)	Inclination (degrees)	Eccentricity	Nodal Rate (degrees/day)
BE-C	7.5022	41.1667	0.025	-4.2535
GEOS-I	8.0729	59.3805	0.073	-2.2465
GEOS-II	7.7052	105.7896	0.033	1.3997

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Table 2

Tidal Parameters Derived from the Multiple Linear Regression Analyses of the Tidal Perturbations  
in the Orbital Inclinations of the BE-C, GEOS-I, and GEOS-II Satellites  
(The errors indicated are the formal statistical errors.)

Satellite	Tide	$\ell_{mpq}$	Period (days)	Amplitude (arc sec)	$c_{2mp0}$	$s_{2mp0}$	$d_{2mp0}$	$\delta_{2mp0}$ (deg)	$C_{2m}^+$ (cm)	$\epsilon_{2m}^+$ (deg)
BE-C	$O_1$	2100	11.8	0.09	$0.276 \pm 0.077$	$-0.018 \pm 0.088$	$0.28 \pm 0.08$	$-3.6 \pm 18.1$	$3.0 \pm 8.1$	$144 \pm 163$
	$K_1$	2110	84.8	0.80	$0.254 \pm 0.010$	$0.025 \pm 0.007$	$0.26 \pm 0.01$	$5.7 \pm 1.6$	$6.9 \pm 1.2$	$29 \pm 8$
	$M_2$	2200	10.3	0.11	$0.204 \pm 0.053$	$0.030 \pm 0.054$	$0.21 \pm 0.05$	$8.4 \pm 15.1$	$10.3 \pm 5.4$	$287 \pm 31$
	$K_2$	2210	42.4	0.12	$0.322 \pm 0.065$	$0.128 \pm 0.072$	$0.35 \pm 0.06$	$21.7 \pm 11.6$	$2.1 \pm 1.2$	$10 \pm 28$
	$P_1$	2100	57.8	0.13	$0.205 \pm 0.036$	$-0.016 \pm 0.041$	$0.21 \pm 0.04$	$-4.5 \pm 11.4$	$3.8 \pm 1.5$	$170 \pm 24$
	$S_2$	2200	34.4	0.20	$0.253 \pm 0.030$	$0.025 \pm 0.030$	$0.25 \pm 0.03$	$5.6 \pm 6.8$	$2.5 \pm 1.4$	$298 \pm 33$
GEOS-I	$O_1$	2100	12.6	—	—	—	—	—	—	—
	$K_1$	2110	160.8	0.73	$0.241 \pm 0.005$	$0.011 \pm 0.005$	$0.24 \pm 0.01$	$2.7 \pm 1.3$	$7.9 \pm 0.7$	$11 \pm 5$
	$M_2$	2200	11.7	0.15	$0.251 \pm 0.027$	$0.017 \pm 0.027$	$0.25 \pm 0.03$	$3.9 \pm 6.1$	$5.3 \pm 2.8$	$289 \pm 29$
	$K_2$	2210	80.4	0.18	$0.284 \pm 0.034$	$0.000 \pm 0.035$	$0.28 \pm 0.03$	$0.0 \pm 7.1$	$0.3 \pm 0.6$	$270 \pm 122$
	$P_1$	2100	85.4	0.09	$0.181 \pm 0.044$	$0.010 \pm 0.045$	$0.18 \pm 0.04$	$3.3 \pm 14.2$	$4.8 \pm 1.8$	$185 \pm 22$
	$S_2$	2200	55.7	0.39	$0.297 \pm 0.012$	$0.034 \pm 0.012$	$0.30 \pm 0.01$	$6.6 \pm 2.3$	$1.7 \pm 0.6$	$355 \pm 20$
GEOS-II	$O_1$	2100	14.4	—	—	—	—	—	—	—
	$K_1$	2110	255.4	0.81	$0.257 \pm 0.021$	$-0.046 \pm 0.013$	$0.26 \pm 0.02$	$-10.2 \pm 2.7$	$8.4 \pm 2.2$	$313 \pm 16$
	$M_2$	2200	15.3	0.25	$0.242 \pm 0.025$	$0.050 \pm 0.025$	$0.25 \pm 0.02$	$11.7 \pm 5.7$	$7.8 \pm 2.5$	$311 \pm 18$
	$K_2$	2210	127.7	0.44	$0.306 \pm 0.023$	$0.012 \pm 0.029$	$0.31 \pm 0.02$	$2.2 \pm 5.3$	$0.2 \pm 0.5$	$28 \pm 105$
	$P_1$	2100	629.8	0.28	$0.050 \pm 0.022$	$-0.107 \pm 0.037$	$0.12 \pm 0.03$	$-65.0 \pm 12.3$	$10.9 \pm 1.0$	$157 \pm 7$
	$S_2$	2200	434.7	4.58	$0.340 \pm 0.007$	$-0.015 \pm 0.004$	$0.34 \pm 0.01$	$-2.5 \pm 0.6$	$2.1 \pm 0.3$	$111 \pm 6$



Table 3

Secular Changes in the Moon's Orbit and the Earth's Orientation  
and Spin, and the Dissipation of Energy for Selected Tides  
(The entries are a weighted average over all three satellites  
The errors indicated are the formal statistical errors )

$\dot{X}$ $\ell_{mpq}$	$[X]_{\ell_{mpq}}$ (Moon)				$[X]_{\ell_{mpq}}$ (Sun)			
	2100	2110	2200	2210	2100	2110	2200	2210
$\dot{n}_M$ (arc sec/(100 yr) <sup>2</sup> )	3 ± 13	0	-29 ± 15	0	—	—	—	—
$\dot{a}_M$ (cm/yr)	-0.4 ± 1.9	0	4.3 ± 2.2	0	—	—	—	—
$\dot{e}_M$ (/10 <sup>9</sup> yr)	0.0 ± 0.001	0	-0.002 ± 0.001	0	—	—	—	—
$\dot{j}$ (deg/10 <sup>9</sup> yr)	-0.3 ± 1.5	-0.2 ± 0.1	-0.7 ± 0.3	-0.0 ± 0.1	—	—	—	—
$\dot{i}_s$ (deg/10 <sup>9</sup> yr)	-1.9 ± 9.2	-0.7 ± 0.3	3.2 ± 1.6	-0.1 ± 0.2	-1.0 ± 0.5	-0.2 ± 0.1	-0.2 ± 0.1	-0.0 ± 0.1
$\dot{\theta}$ (10 <sup>-22</sup> rad/sec <sup>2</sup> )	0.3 ± 1.4	-0.1 ± 0.1	-6.3 ± 3.2	-0.0 ± 0.1	0.1 ± 0.1	-0.0 ± 0.1	+0.4 ± 0.2	-0.0 ± 0.1
$\dot{E}$ (10 <sup>19</sup> erg/sec)	0.1 ± 0.7	-0.1 ± 0.1	-3.6 ± 1.8	-0.0 ± 0.1	0.1 ± 0.1	-0.0 ± 0.1	+0.2 ± 0.1	-0.0 ± 0.1

Table 4

Secular Changes in the Moon's Orbit and the Earth's Orientation  
and Spin, and the Dissipation of Energy for Selected Tides  
(The entries are a weighted average over the BE-C and GEOS-I satellites  
The errors indicated are the formal statistical errors)

$\dot{X}$ $\ell_{mpq}$	$[X]_{\ell_{mpq}}$ (Moon)				$[X]_{\ell_{mpq}}$ (Sun)			
	2100	2110	2200	2210	2100	2110	2200	2210
$\dot{n}_M$ (arc sec/(100 yr) <sup>2</sup> )	$3 \pm 13$	0	$-17 \pm 20$	0	—	—	—	—
$\dot{a}_M$ (cm/yr)	$-0.4 \pm 1.9$	0	$2.4 \pm 3.0$	0	—	—	—	—
$\dot{e}_M$ (/10 <sup>9</sup> yr)	$0.0 \pm 0.001$	0	$-0.001 \pm 0.001$	0	—	—	—	—
$\dot{j}$ (deg/10 <sup>9</sup> yr)	$-0.3 \pm 1.5$	$-0.3 \pm 0.1$	$-0.4 \pm 0.5$	$-0.0 \pm 0.1$	—	—	—	—
$\dot{i}_s$ (deg/10 <sup>9</sup> yr)	$-1.9 \pm 9.2$	$-1.3 \pm 0.3$	$1.8 \pm 2.3$	$-0.2 \pm 0.2$	$-0.1 \pm 0.7$	$-0.3 \pm 0.1$	$0.7 \pm 0.2$	$-0.0 \pm 0.1$
$\ddot{\theta}$ (10 <sup>-22</sup> rad/sec <sup>2</sup> )	$0.3 \pm 1.4$	$-0.2 \pm 0.1$	$-3.6 \pm 4.4$	$-0.0 \pm 0.1$	$0.0 \pm 0.1$	$-0.0 \pm 0.1$	$-1.3 \pm 0.4$	$-0.0 \pm 0.1$
$\dot{E}$ (10 <sup>19</sup> erg/sec)	$0.1 \pm 0.7$	$-0.1 \pm 0.1$	$-2.0 \pm 2.5$	$-0.0 \pm 0.1$	$0.0 \pm 0.1$	$-0.0 \pm 0.1$	$-0.7 \pm 0.3$	$-0.0 \pm 0.1$



Table 5

$P_{\ell mpq}$  for  $\ell = 2$ ,  $q = 0$  for the Quantities Shown in the Left-Hand Column

$\dot{X}$	$\ell mpq$	$P_{\ell mpq}$ (Moon)						$P_{\ell mpq}$ (Sun)					
		2100	2110	2120	2200	2210	2220	2100	2110	2120	2200	2210	2220
$\dot{n}_M$ (arc sec/(100 yr) <sup>2</sup> )		-144.6	0	+0.3	-847.1	0	+0.0	-	-	-	-	-	-
$\dot{a}_M$ (cm/yr)		+ 21.4	0	-0.0	+125.1	0	-0.0	-	-	-	-	-	-
$\dot{e}_M$ (/10 <sup>9</sup> yr)		- 0.0076	0	+0.0	- 0.0447	0	+0.0	-	-	-	-	-	-
$\dot{j}$ (deg/10 <sup>9</sup> yr)		+ 16.7	-18.2	-0.1	- 19.4	-1.9	-0.0	-	-	-	-	-	-
$\dot{i}_s$ (deg/10 <sup>9</sup> yr)		+105.3	-81.0	-0.6	+ 94.0	-8.4	-0.0	+22.5	-17.5	-0.1	+19.9	-1.6	-0.0
$\ddot{\theta}$ (10 <sup>-22</sup> rad/sec <sup>2</sup> )		- 15.6	-14.2	-0.0	-182.8	-1.5	-0.0	- 3.3	- 3.1	-0.0	-38.7	-0.3	-0.0
$\dot{E}$ (10 <sup>19</sup> erg/sec)		- 8.5	- 8.3	-0.0	-103.6	-0.9	-0.0	- 2.0	- 1.8	-0.0	-22.8	-0.2	-0.0

C.2

92

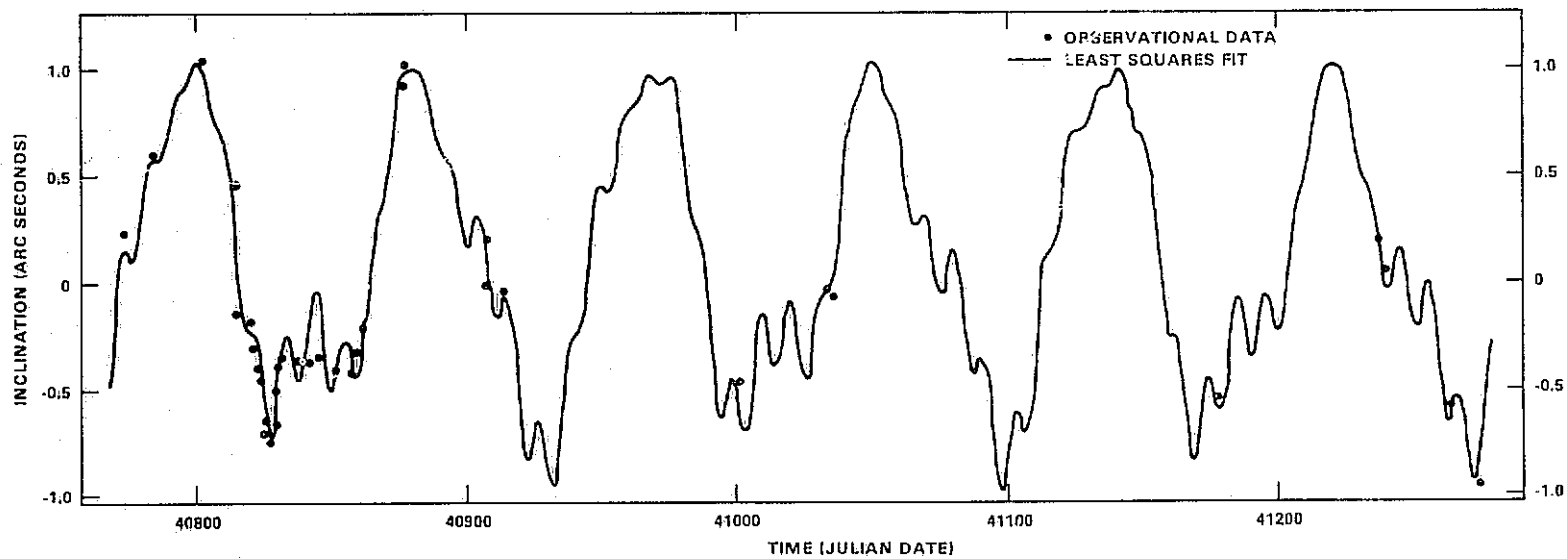


Figure 1. Inclination Data and Regression Curve for BE-C



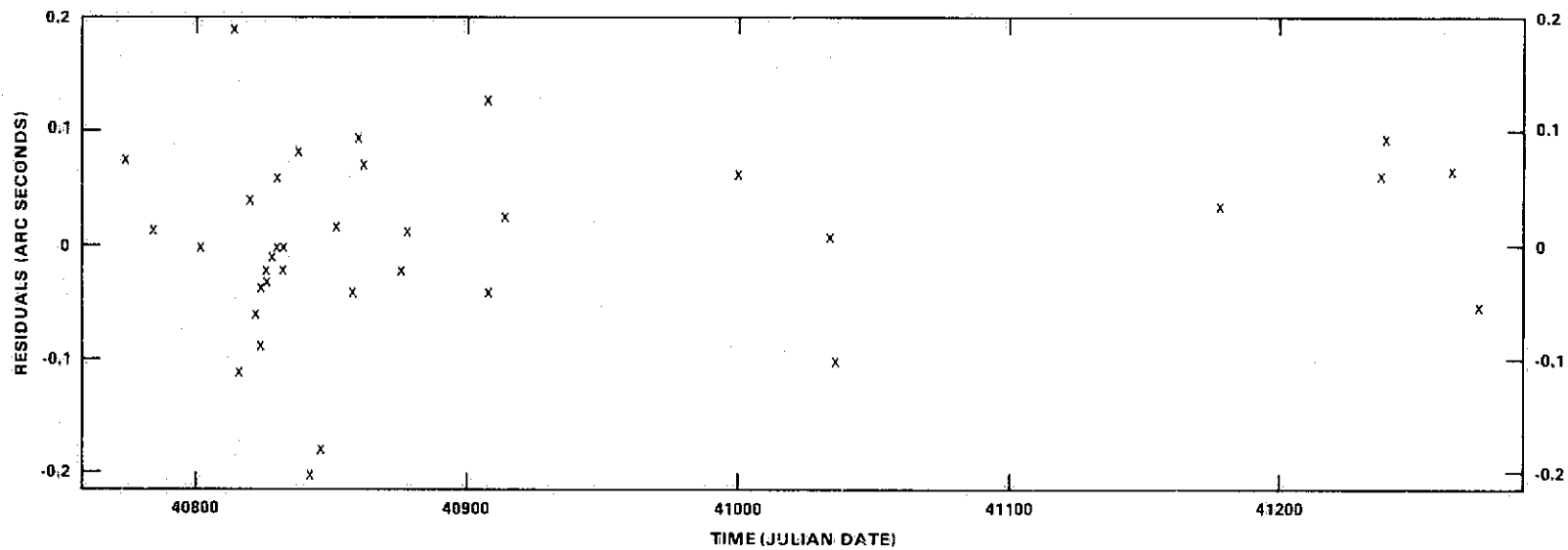


Figure 2. Residuals for Regression Curve Shown in Figure 1.  
Standard Error of Estimate: 0.0626

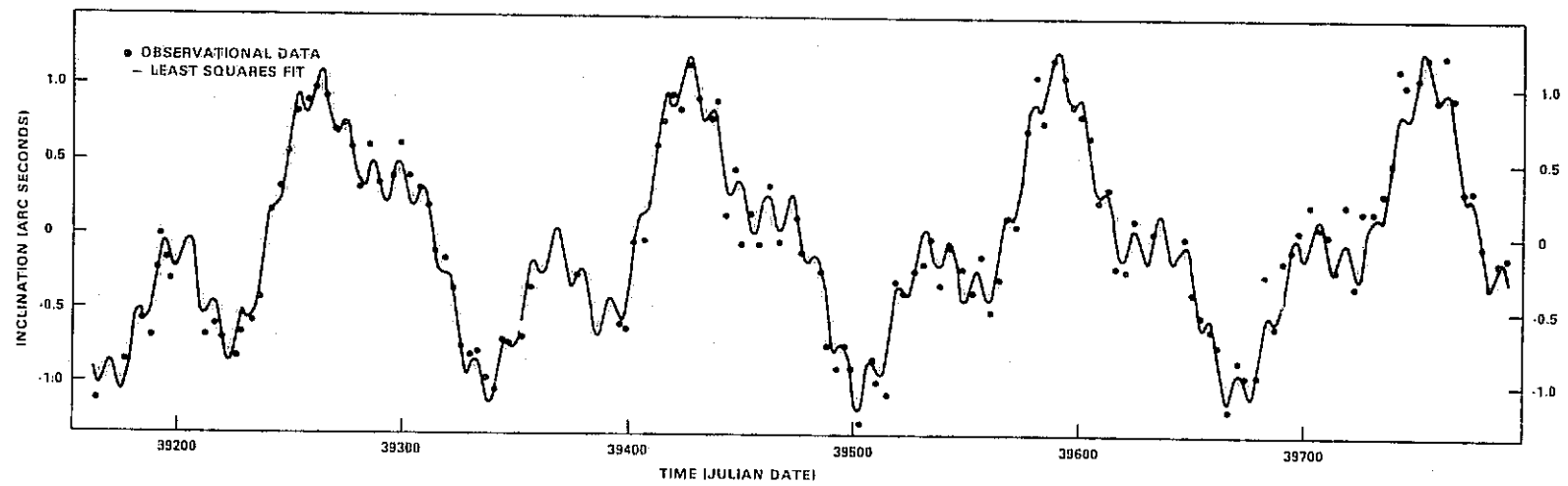


Figure 3. Inclination Data and Regression Curve for GEOS-I

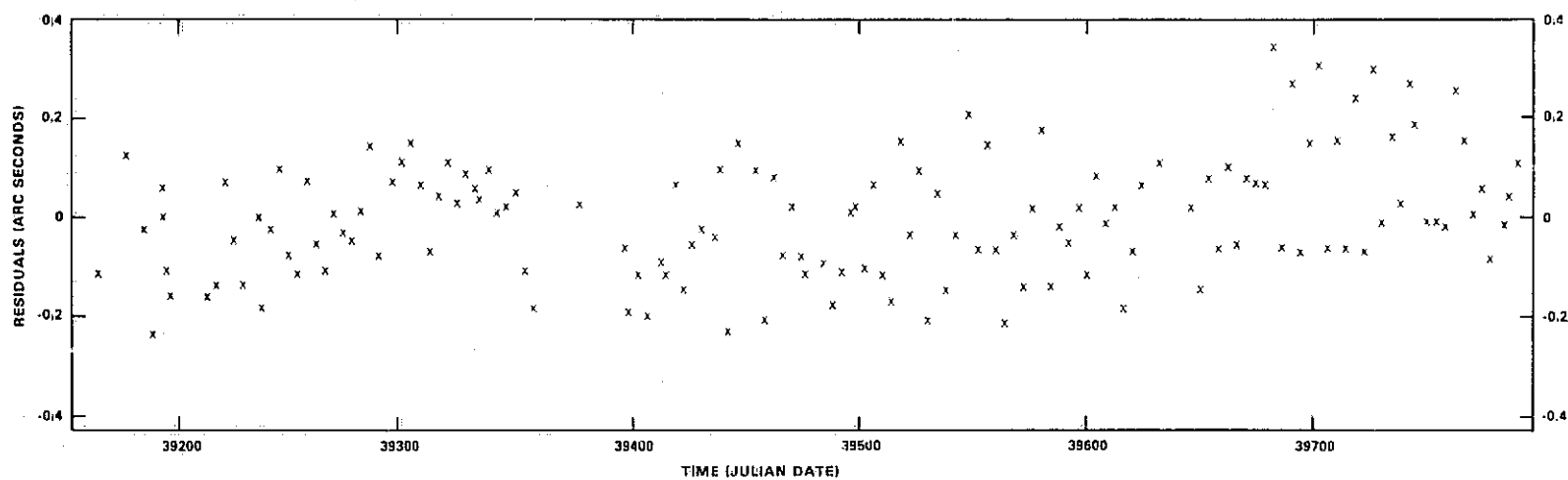


Figure 4. Residuals for Regression Curve Shown in Figure 3.  
Standard Error of Estimate: 0.132

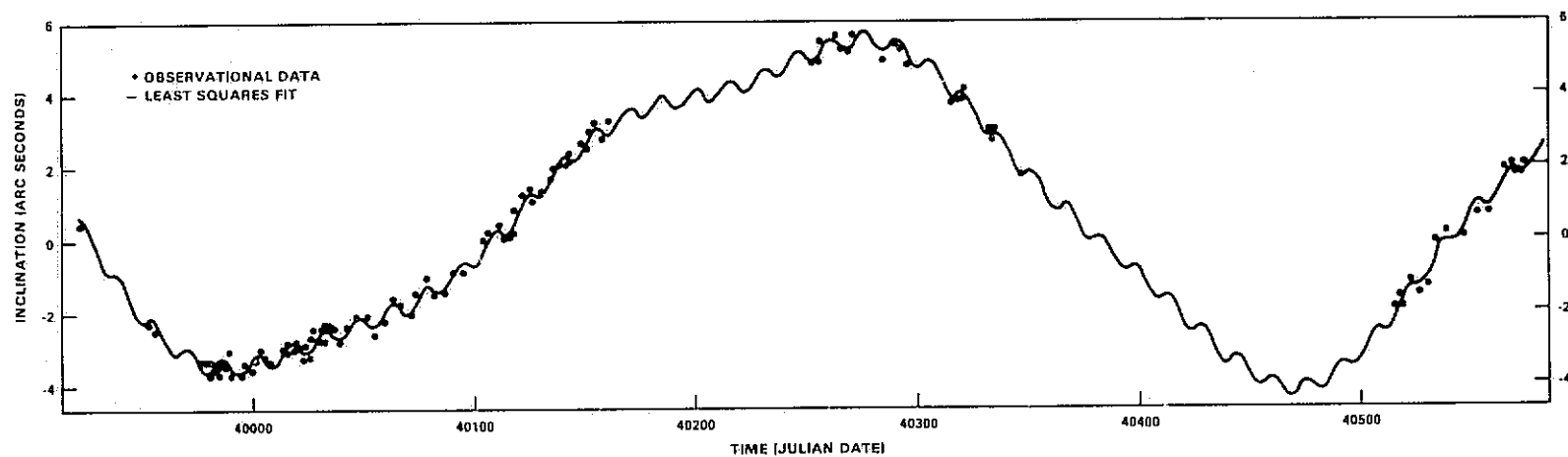


Figure 5. Inclination Data and Regression Curve for GEOS-II



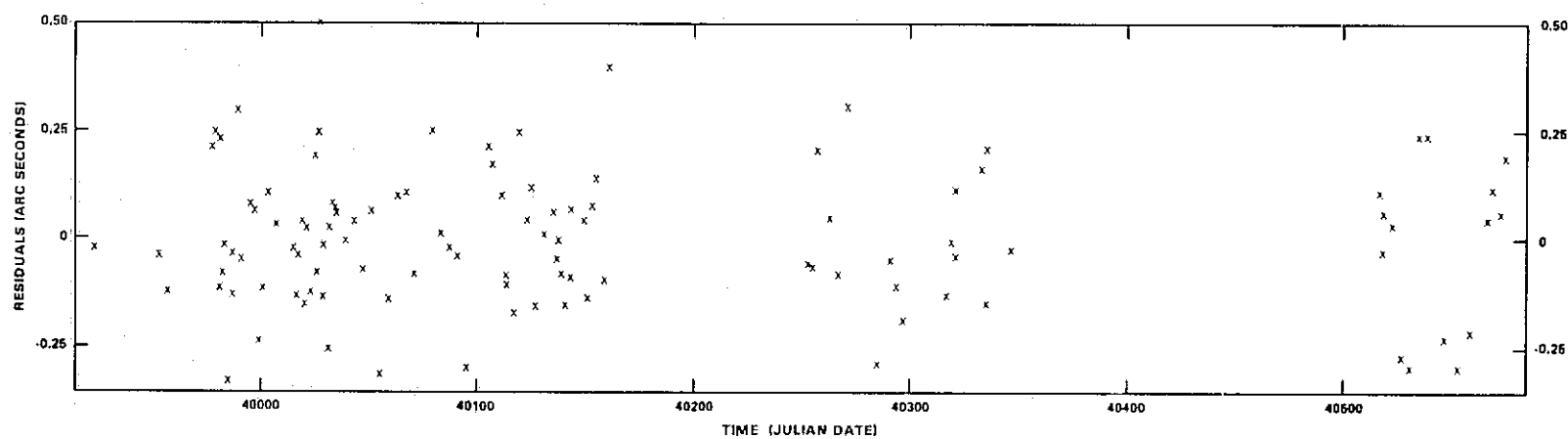


Figure 6. Residuals for Regression Curve Shown in Figure 5.  
Standard Error of Estimate: 0.175

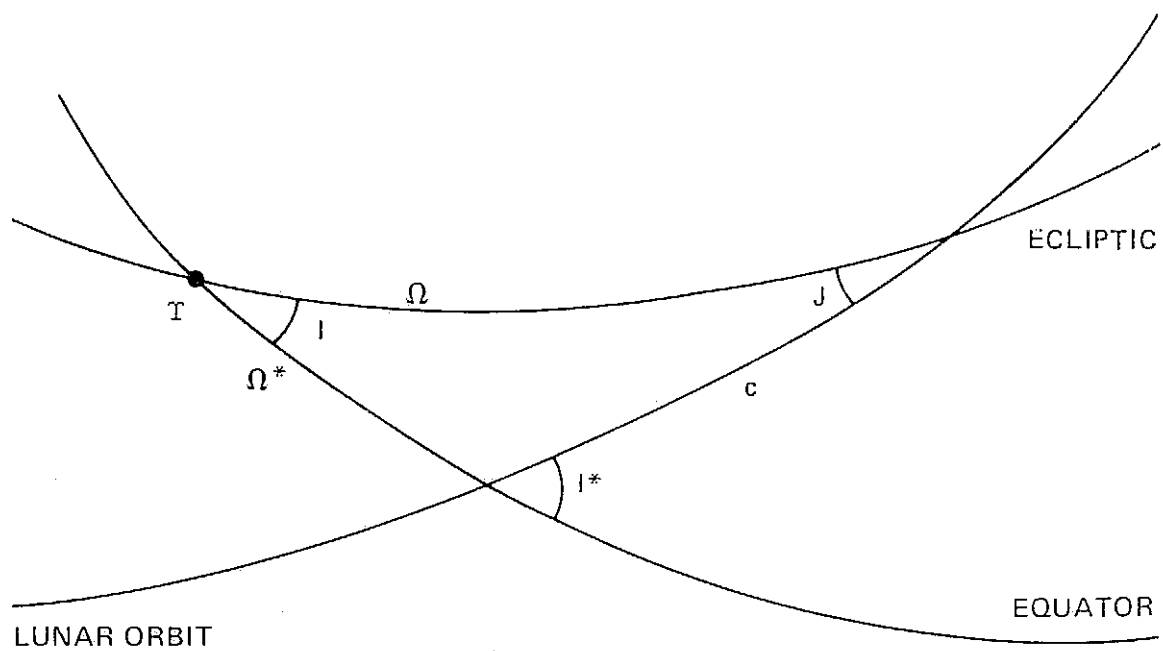


Figure 7. Spherical Triangle Used for Computing the Moon's Position With Respect to the Earth's Equator